

Towards low-energy tests of quantum gravity

From quantum gravity phenomenology to graviton detection



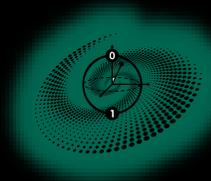
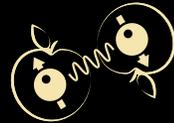
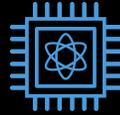
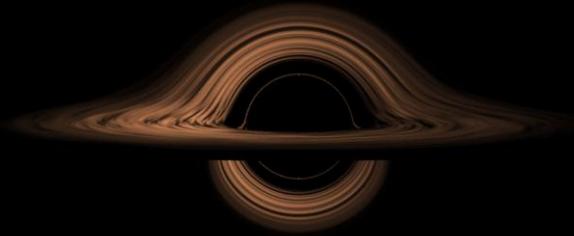
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Bad Honnef School
May 12, 2025

PIKOVSKI GROUP: INTERFACE OF QUANTUM & GRAVITY



Where do gravity &
quantum meet?
Experiments?



Theory of:

- Quantum optics & information
- Quantum sensing
- Macroscopic quantum systems
- Gravity effects in QM
- Quantum signatures of gravity
- Foundations of QM and GR

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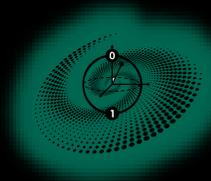
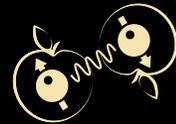
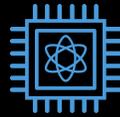
PIKOVSKI GROUP: INTERFACE OF QUANTUM & GRAVITY



Alex Johnson
Poster on:
“Quantum
Sensing through
Quantum Error
Correction”



Thomas Beitel:
Poster on
“Graviton
Detection and
Its Quantum
Aspects”



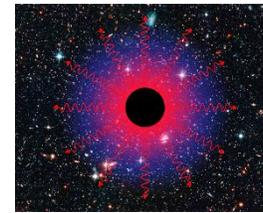
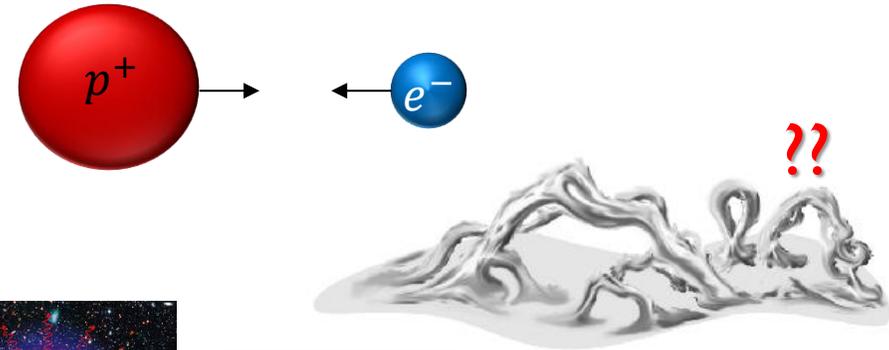
Theory of:

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DEMOTIVATION: NO HOPE OF TESTING QUANTUM GRAVITY?

- Gravity is extremely weak. Compare F_E to F_G between e^- and p^+ : $\frac{F_E}{F_G} = 10^{39}$
- Planck-scale on extreme scales:
 $10^{-35}m \sim 10^{44}Hz \sim 10^{19}GeV \sim 22\mu g$
- Hawking radiation: $T \sim 1 nK \left[\frac{M}{60M_\odot}\right]^{-1}$
- Graviton cross-section: $\sigma \sim L_p^2 \cong 10^{-70}m^2$
- Detecting a single graviton with Ligo: $\frac{\Delta L}{L} \sim 10^{-40}$
- Maximum information: Bekenstein bound $I \sim 10^{43} \left[\frac{r}{1km}\right] \left[\frac{M}{1kg}\right]$ bits



Until recently: common wisdom that no table-top experiment can test QGR

OVERVIEW: TOWARDS LOW-ENERGY TESTS OF QUANTUM GRAVITY

- **First steps to testing quantum gravity: gravitational “decoherence”**

*W. Marshall, C. Simon, R. Penrose, D. Bouwmeester. PRL 91, 130401 (2003);
D. Kleckner*, I. Pikovski* et al. NJP 10, 095020 (2008)*

- **New domain: quantum gravity phenomenology in table-top experiments**

*I. Pikovski, M. Vanner, M. Aspelmeyer, M. Kim, Č. Brukner. Nature Physics 8, 393-397 (2012)
P.A. Bushev et al., PRD ,066020 (2019)*

- **Indirect test of expected quantum gravity: gravitational entanglement**

*Bose et al. PRL 119, 240401 (2017), Marletto, Vedral. PRL 119, 240402 (2017)
V. Fragkos*, M. Kopp*, I. Pikovski. AVS Quantum Sci. 4, 045601(2022)*

- **Direct probe of (linear) quantum gravity: Graviton detection**

*S. Boughn, T. Rothman. Classical and quantum gravity, 23, 5839 (2006)
G. Tobar*, S. Manikandan*, T. Beitel, I. Pikovski. Nature Commun. 15, 7229 (2024)*

GRAVITATIONAL COLLAPSE OF THE WAVE FUNCTION

- Traditionally: search for a *quantum* theory of gravity

Canonical

$$H \psi[g_{ij}] = 0$$

Hamiltonian
quantization

Wheeler-DeWitt

Loop quantum gravity

Covariant

$$g_{\mu\nu} = \tilde{g}_{\mu\nu} + h_{\mu\nu}$$

Perturbative QFT on
a background

Supergravity

String theory

Path integral

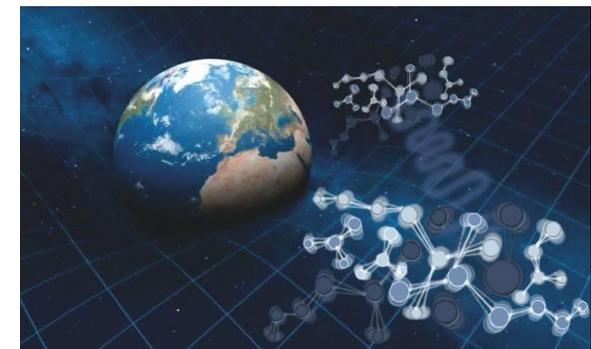
$$\int \mathcal{D}[\text{field histories}] e^{\frac{i}{\hbar} \text{Action}}$$

Functional integral
quantization

Discrete quantum gravity

Spin foam

- But could quantum mechanics be incorrect?
- Penrose: “Classicalize” quantum mechanics: postulated collapse of the superposition principle



GRAVITATIONAL COLLAPSE OF THE WAVE FUNCTION ARGUMENT

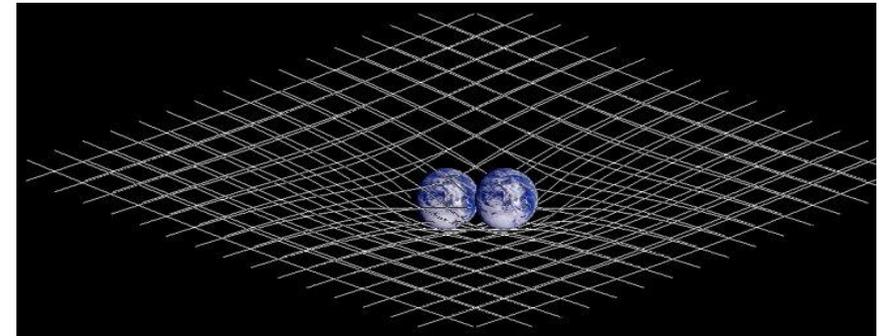
Penrose's proposal: Gravity responsible for **breakdown** of unitarity. His argument:

- A massive object in a superposition: Include its gravitational field. *R. Penrose. General relativity and gravitation, 28, 581-600 (1996)*
- Two different space-times provide different time evolution "d/dt" in evolution equation
- In GR one cannot compare two distinct space-time structures
- Cannot find *single* time evolution operator - unitary evolution of superposition will have intrinsic error.
- Try to quantify error in identification of the two spacetimes:

$$\Delta E = -G \int d^3x \int d^3y \frac{(\rho(x) - \rho'(x))(\rho(y) - \rho'(y))}{|x - y|}$$

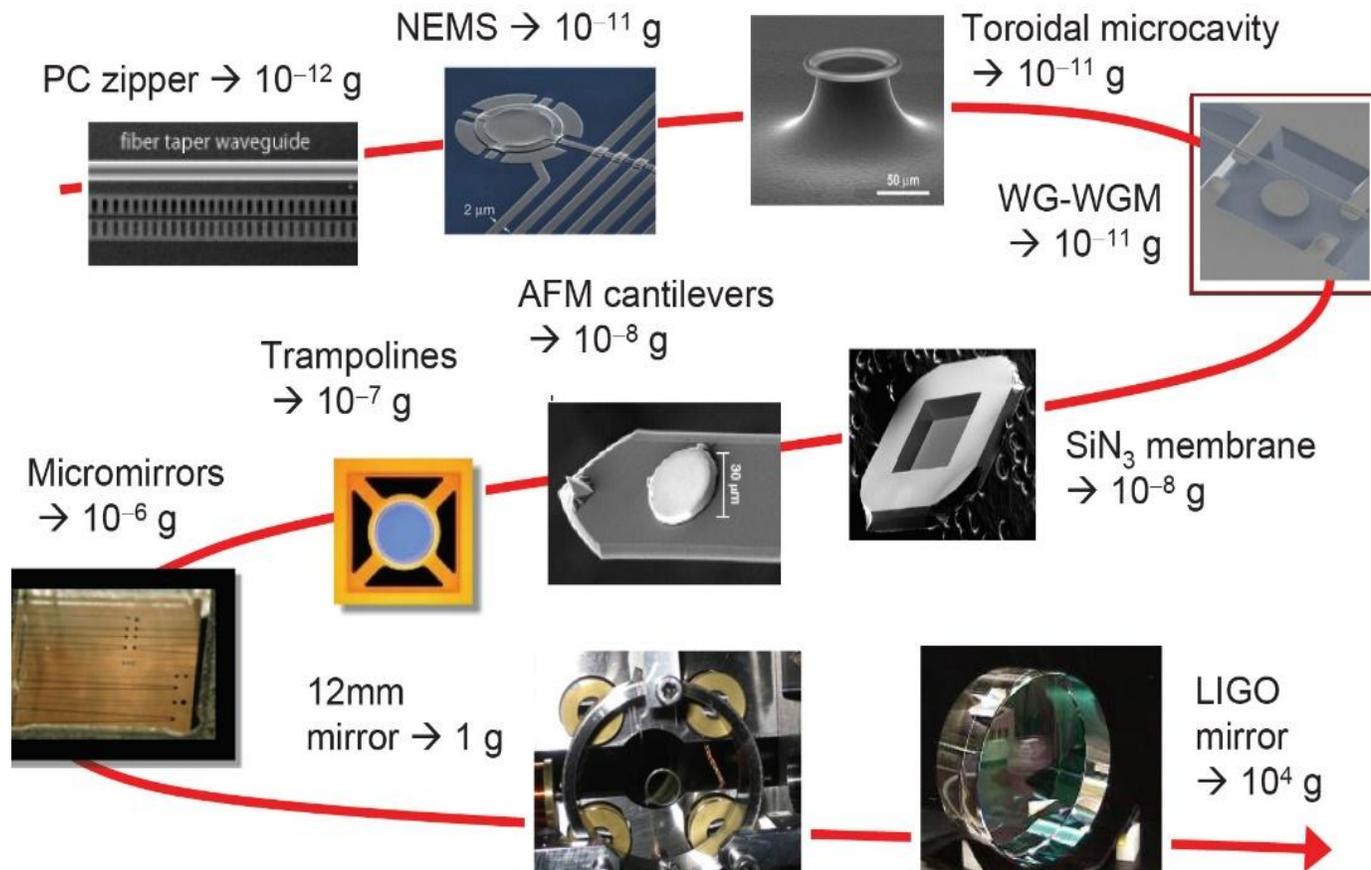
$$\tau_G \approx \hbar / \Delta E$$

Significant for masses
 $m \gtrsim 1ng$
- Hopeless to reach such massive superpositions?



BIRTH OF OPTOMECHANICS

Quantum optomechanics



- 1995-1999: optomechanics theory developed
- New physical regime of quantum mechanics
- Enables the study of macroscopic quantum systems

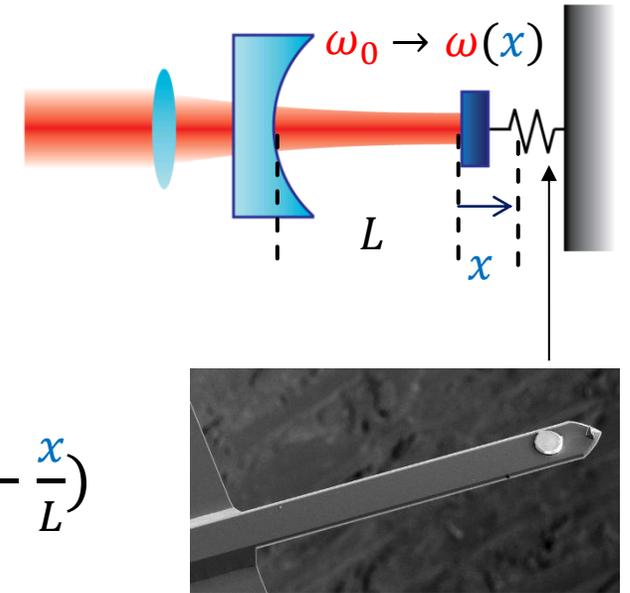
OPTO-MECHANICS

Light in a cavity displaces a small mirror by radiation pressure:
Massive mechanical oscillator interacts with light.

Opto-mechanical interaction:

- i. Free cavity: $\hat{H} = \hbar\omega_0\hat{n}_L$, $\omega_0 = \frac{4\pi c}{nL}$
- ii. Radiation pressure changes $L \rightarrow L + x$: $\omega_0 \rightarrow \omega_0 \left(1 - \frac{x}{L}\right)$
- iii. Quantize $x \rightarrow \hat{x}_m$

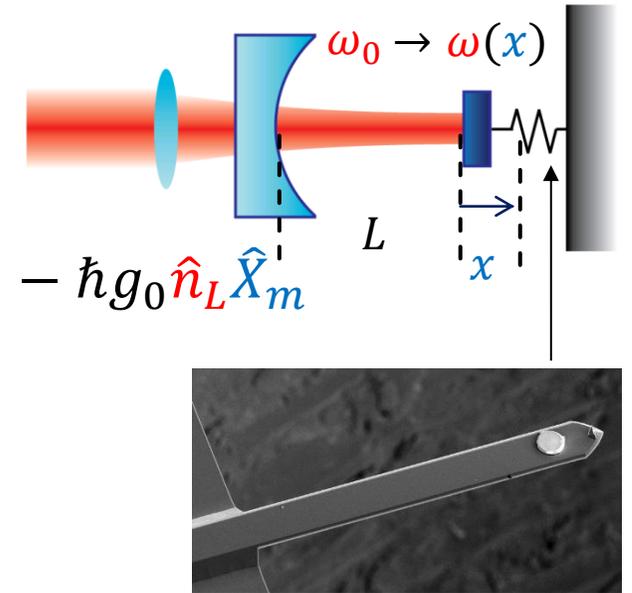
$$\hat{H} = \hbar\omega_m\hat{n}_m + \hbar\omega_L\hat{n}_L - \hbar g_0\hat{n}_L\hat{X}_m, \quad g_0 = \frac{\omega_L}{L} \sqrt{\frac{\hbar}{m\omega_m}} \text{ coupling rate}$$



- ▶ Quantum mechanics with macroscopic and massive objects. Mirrors can have mass of pg – kg
- ▶ Possibility to explore quantum physics on a novel scale.

OPTO-MECHANICS

Light in a cavity displaces a small mirror by radiation pressure:
Massive mechanical oscillator interacts with light.



Opto-mechanical Unitary: $\hat{U} = e^{-i\hat{H}t/\hbar}$ $\hat{H} = \hbar\omega_m\hat{n}_m + \hbar\omega_L\hat{n}_L - \hbar g_0\hat{n}_L\hat{X}_m$

Transform using: $\hat{S} = e^{-i\kappa\hat{n}_L(\hat{b}-\hat{b}^\dagger)}$ $\kappa = \frac{g_0}{\omega_L}$

$$\hat{S}\hat{b}_m\hat{S}^\dagger = \hat{b}_m + \kappa\hat{n}_L$$

$\hat{U} = \hat{S}^\dagger\hat{S}\hat{U}\hat{S}^\dagger\hat{S} = e^{-i\omega_L t\hat{n}_L} e^{-i\kappa^2\omega_L t\hat{n}_L^2}\hat{S}^\dagger e^{-i\omega_m t\hat{n}_m}\hat{S}$ Use BCH to swap \hat{S}^\dagger and $e^{-i\omega_m t\hat{n}_m}$

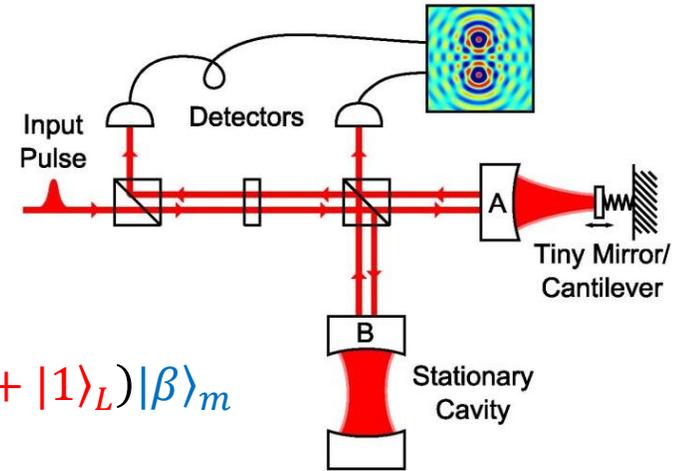
$$= e^{-i\omega_L t\hat{n}_L} e^{-i\kappa^2\hat{n}_L^2(\omega_L t - \sin(\omega_L t))} e^{-i\kappa\hat{n}_L(\hat{b}^\dagger(1 - e^{i\omega_m t}) - \hat{b}(1 - e^{-i\omega_m t}))} e^{-i\omega_m t\hat{n}_m}$$

Photon-dependent displacement $\hat{D}(\kappa\hat{n}_L(1 - e^{i\omega_m t}))$

PROPOSED EXPERIMENT TO TEST PENROSE COLLAPSE

Idea: Use single photon in superposition to create and read out quantum superposition of a much larger system.

*W. Marshall, C. Simon, R. Penrose, D. Bouwmeester. PRL 91, 130401 (2003);
D. Kleckner, I. Piovski et al. NJP 10, 095020 (2008)*



In one arm, a tiny mirror is displaced by the photon: $|\psi(0)\rangle = \frac{1}{\sqrt{2}} (|0\rangle_L + |1\rangle_L) |\beta\rangle_m$

$$|\psi(t)\rangle = \frac{1}{\sqrt{2}} \left(|0\rangle_L |\beta e^{-i\omega_m t}\rangle_m + e^{i\varphi} |1\rangle_L |\beta e^{-i\omega_m t} + \kappa(1 - e^{-i\omega_m t})\rangle_m \right) \quad \kappa = \frac{g_0}{\omega_L} \text{ single photon coupling rate}$$

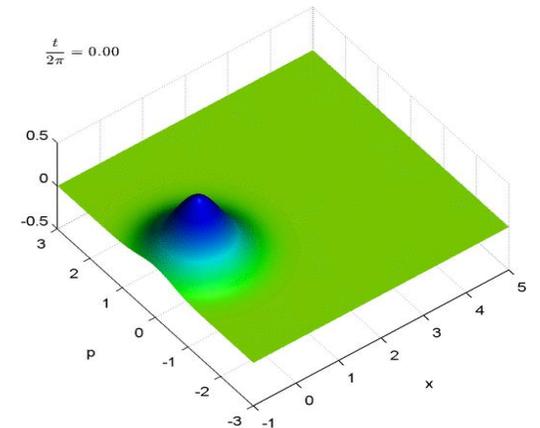
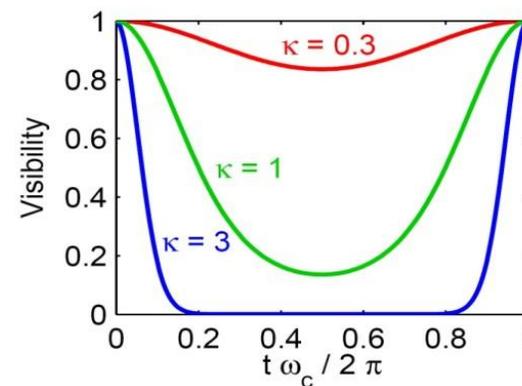
Mirror is probed by measuring quantum interference of the photon:

Interference periodically vanishes due to which-path-information:

path-information: $V = e^{-\kappa^2(1-\cos(\omega_m t))}$

Macroscopic superposition if: $\kappa \gtrsim 1/\sqrt{2}$

(One photon displaces mirror strongly enough)



PROPOSED EXPERIMENT TO TEST PENROSE COLLAPSE

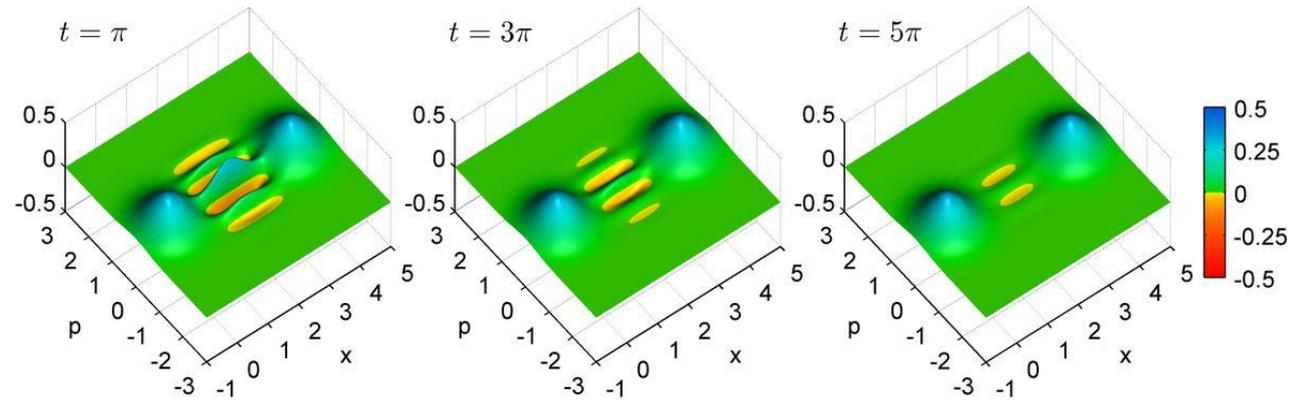
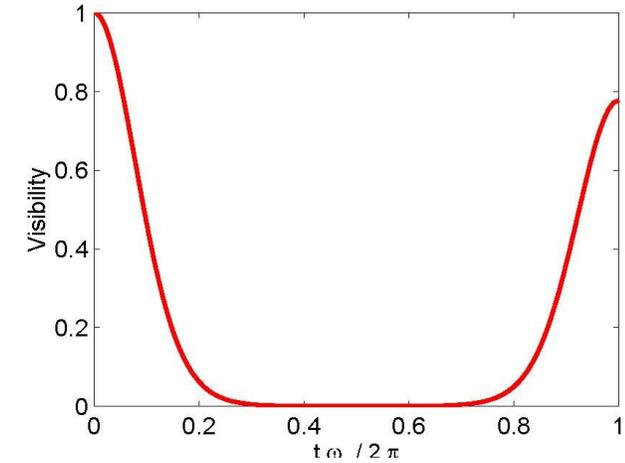
Signature of Penrose collapse: No full revival!

Effect: Reduction of visibility revival peaks. But so does decoherence:

- Phonon dissipation
- Thermal bath
- Scattering of surrounding particles
- Impurities in cantilever
- ...

Penrose collapse estimate
(granular mass of size a) :

$$\Delta E = 2Gmm_1 \left(\frac{6}{5a} - \frac{1}{\Delta x} \right) \quad (\text{given: } \Delta x \geq 2a) \quad \tau_G \approx \begin{cases} 1ms & a = 10^{-15}m \\ 1s & a = \sqrt{\frac{\hbar}{m\omega_c}} \end{cases}$$



Hard to this day, but lots
of experimental effort

FROM COLLAPSE TO QUANTUM GRAVITY PHENOMENOLOGY

- Much work has been done towards testing gravitational collapse
- From around ~2012: New ideas on testing *other* aspects of quantum gravity

Testing *speculative* models of quantum gravity

Marshall et al 2003

Pikovski et al 2012

Bekenstein 2012

Kafri et al 2014

Belenchia et al 2016

Oppenheim 2023

...



High-precision test of new physics beyond QM, GR.

Caveat:
Tests only *speculative* models.
Likely only null-measurements (?)

MODIFIED UNCERTAINTY RELATIONS

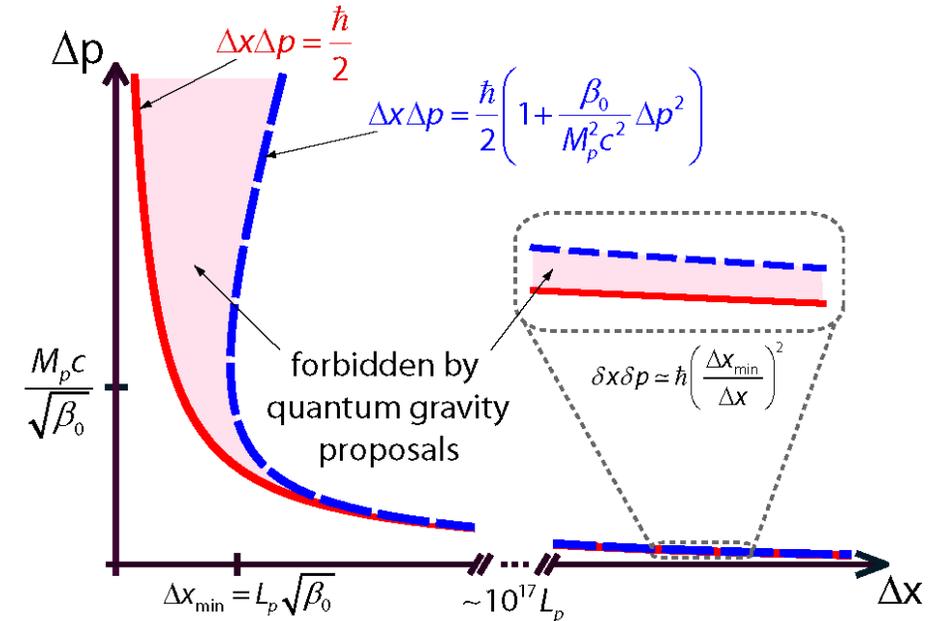
No complete theory of quantum gravity to date. Few known concrete predictions.

Modified uncertainty relations common to most approaches to quantum gravity:

$$\Delta x \Delta p \geq \frac{\hbar}{2} \left(1 + \beta_0 \frac{\Delta p^2}{M_{Pl}^2 c^2} \right) \quad \begin{array}{l} \text{(L. Garay, Int. J. Mod. Phys. A10, 145 (1995))} \\ \text{E. Witten, Physics Today 49, 24 (1996)} \end{array}$$

- Key features:
- Restricts allowed state-space
 - Minimal physical length $\Delta x_{min} = L_{Pl} \sqrt{\beta_0}$
 - Parametrized by free parameter β_0
 - Planck-length effect for $\beta_0 \sim 1$

Phenomenologically: can be incorporated into quantum theory through modified algebra



MODIFIED UNCERTAINTY RELATIONS

Many suggested canonical commutator deformations, e.g.:

$$[\hat{X}, \hat{P}]_{\beta} = i \left(1 + \beta_0 \frac{p_0^2 \hat{P}^2}{M_{Pl}^2 c^2} + \dots \right)$$

(A. Kempf, G. Mangano and R. Mann, *PRD*, 52, 2 (1995))

$$[\hat{X}, \hat{P}]_{\mu} = i \sqrt{1 + 2\mu_0 \frac{(p_0 \hat{P} / c)^2 + m^2}{M_{Pl}^2}} + \dots$$

(M. Maggiore, *Phys. Lett. B*, 319 (1993))

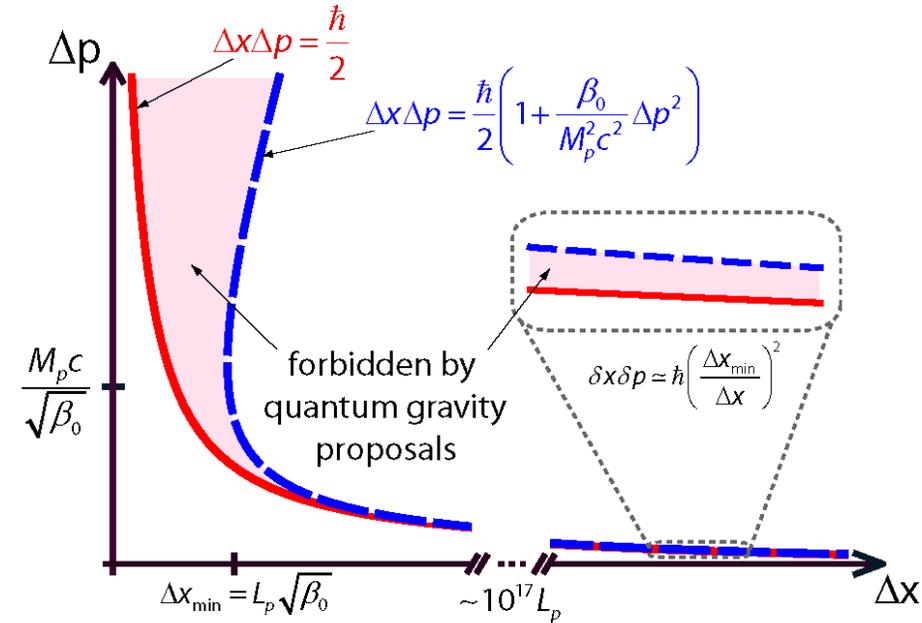
$$[\hat{X}, \hat{P}]_{\gamma} = i \left(1 - \gamma_0 \frac{p_0 \hat{P}}{M_{Pl} c} + \gamma_0^2 \frac{p_0^2 \hat{P}^2}{M_{Pl}^2 c^2} + \dots \right)$$

(A. F. Ali, S. Das and E. C. Vagenas, *Phys. Lett. B*, 678 (2009))

Examples:

Ions in harmonic trap: $\frac{p_0^2}{M_{Pl}^2 c^2} \sim 10^{-60}$

Optomechanics: $\frac{p_0^2}{M_{Pl}^2 c^2} \sim 10^{-40}$



Experimental bound from quantum systems as of 2012: $\beta_0 < 10^{33}$

OPTOMECHANICAL SCHEME

Based on displacements in phase space:

$$\hat{D}(\alpha) = e^{\alpha \hat{a}^+ - \alpha^* \hat{a}} = e^{i\sqrt{2}\text{Re}[\alpha] \hat{X} - i\sqrt{2}\text{Im}[\alpha] \hat{P}}$$

$$\hat{D}(\beta)\hat{D}(\alpha) = \hat{D}(\alpha + \beta) e^{i \text{Im}[\alpha^* \beta]}$$

$$\hat{D}(-\beta)\hat{D}(-\alpha)\hat{D}(\beta)\hat{D}(\alpha) = e^{2i \text{Im}[\alpha^* \beta]}$$

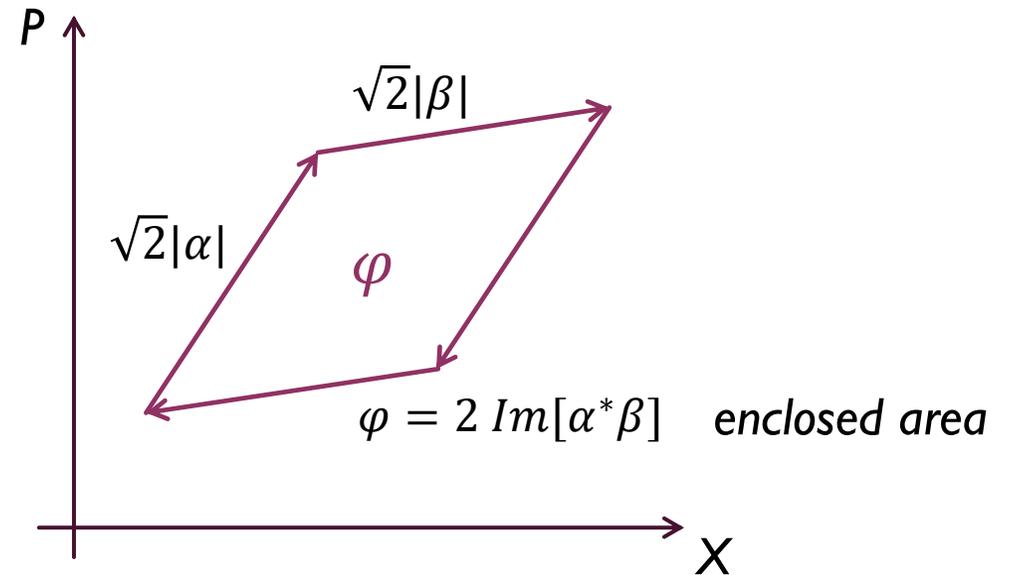
- Results in an overall phase
- State independent
- Arises due to $[\hat{X}, \hat{P}] \neq 0$

Can be used for quantum computing

*Milburn, Schneider, James, Fortschr. Phys. 48, 801 (2000),
Sørensen, Mølmer, Phys. Rev.A 62, 022311 (2000)*

Phase space quadratures:

$$\hat{X} = \frac{1}{\sqrt{2}}(\hat{a} + \hat{a}^+), \quad \hat{P} = \frac{1}{\sqrt{2}i}(\hat{a} - \hat{a}^+)$$



Implemented to create a phase gate for ions

Leibfried et al., Nature 422, 27 (2003)

OPTOMECHANICAL SCHEME

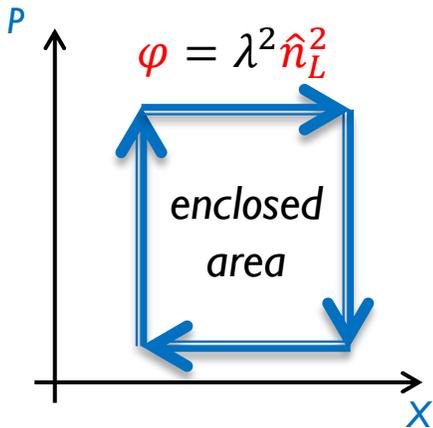
Light in a cavity displaces a small mirror by radiation pressure:

Pulsed opto-mechanical setting:

M. Vanner, I. Pikovski et al. PNAS 108, 16182 (2011)

Single quadrature displacement

Free evolution after interaction:



4 iterations:

$$\hat{\xi} = e^{i\lambda \hat{n}_L \hat{P}} e^{-i\lambda \hat{n}_L \hat{X}} e^{-i\lambda \hat{n}_L \hat{P}} e^{i\lambda \hat{n}_L \hat{X}} = e^{-i\lambda^2 \hat{n}_L^2}$$

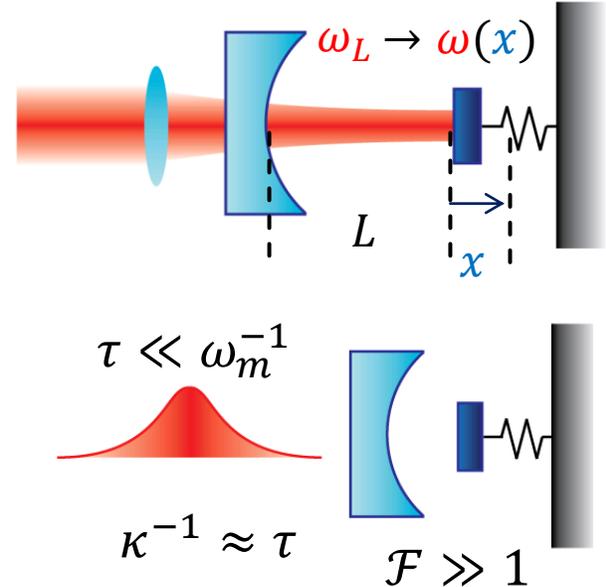
Self-Kerr non-linearity on the light, independent of the mechanics

$$\hat{H} = \hbar\omega_m \hat{n}_m + \hbar\omega_L \hat{n}_L - \hbar g_0 \hat{n}_L \hat{X}_m$$

$$\hat{H} \approx \hbar\omega_L \hat{n}_L - \hbar g_0 \hat{n}_L \hat{X}_m$$

$$\hat{U}(\tau) \approx e^{i\lambda \hat{n}_L \hat{X}_m} \quad \lambda = g_0 \tau \propto \mathcal{F}$$

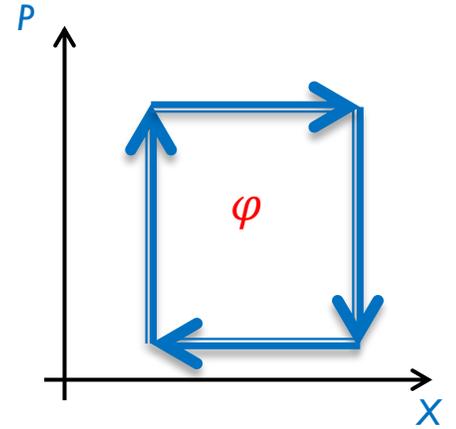
$$\hat{U}(t + \tau) = e^{i\lambda \hat{n}_L (\hat{X}_m \cos \omega_m t - \hat{P}_m \sin \omega_m t)}$$



OPTOMECHANICAL SCHEME

$$\hat{\xi} = e^{i\lambda\hat{n}_L\hat{P}} e^{-i\lambda\hat{n}_L\hat{X}} e^{-i\lambda\hat{n}_L\hat{P}} e^{i\lambda\hat{n}_L\hat{X}} = e^{-\sum_{k=1}^{\infty} \frac{(\lambda\hat{n}_L)^{k+1}}{k!} [\hat{X}, \hat{P}]_k}$$

- In quantum mechanics: $[\hat{X}, \hat{P}] = i$ $\hat{\xi}_{QM} = e^{-i\lambda^2\hat{n}_L^2}$
- Alternative theories: $[\hat{X}, \hat{P}] = iF(\hat{X}, \hat{P})$ $\hat{\xi} = e^{-i\lambda^2\hat{n}_L^2 + \epsilon(\hat{n}_L^k)}$



Any arbitrary deformed algebra will show in $\hat{\xi}$

$$\beta = \beta_0 \frac{\hbar\omega_m m}{(M_{Pl}c)^2} \ll 1$$

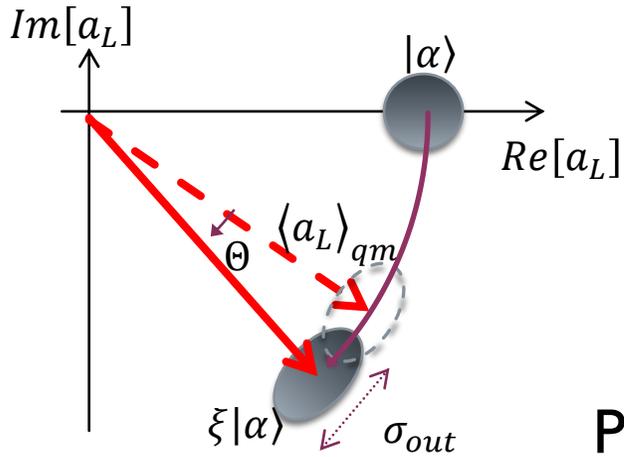
- $[\hat{X}, \hat{P}]_1 = i(1 + \beta\hat{P}^2)$
- $[\hat{X}, \hat{P}]_2 = i^2 2\beta\hat{P} + O(\beta^2)$
- $[\hat{X}, \hat{P}]_3 = i^3 2\beta + O(\beta^2)$
- $[\hat{X}, \hat{P}]_4 = O(\beta^2)$

Example: β -modification

$$[\hat{X}, \hat{P}] = i\left(1 + \beta_0 \frac{p_0^2 \hat{P}^2}{M_{Pl}^2 c^2}\right),$$

Hence:
$$\hat{\xi}_\beta = e^{-i\lambda^2\hat{n}_L^2} e^{-i\beta(\lambda^2\hat{n}_L^2\hat{P}^2 + \lambda^3\hat{n}_L^3\hat{P} + \frac{1}{3}\lambda^4\hat{n}_L^4)}$$

OPTOMECHANICAL SCHEME



Measurement on the light: detect the mean phase change

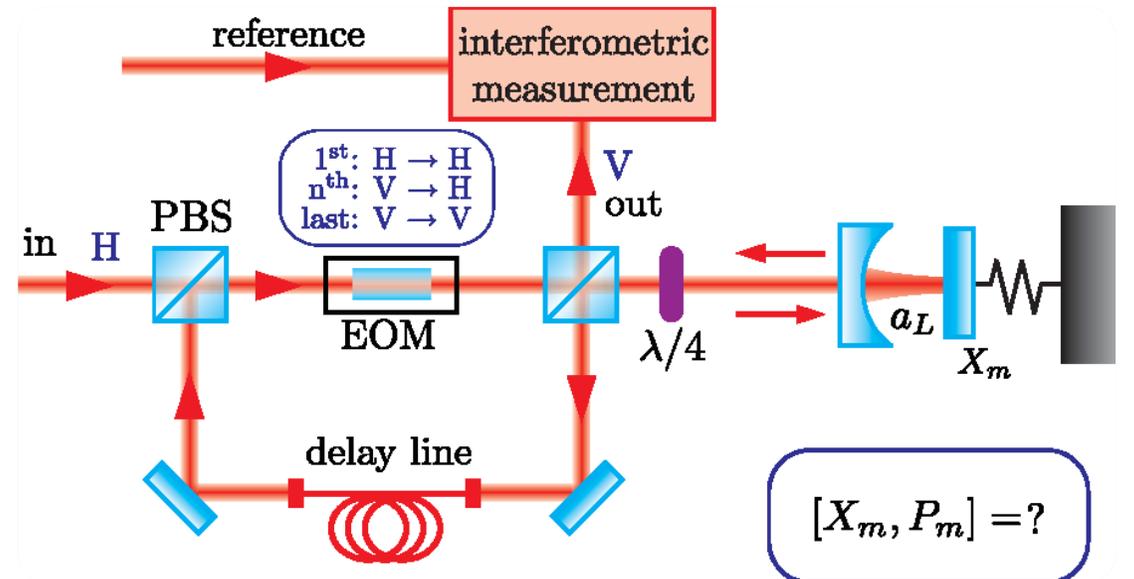
$$\langle \hat{a}_L \rangle = \langle \alpha | \hat{\xi}^\dagger \hat{a}_L \hat{\xi} | \alpha \rangle \cong \langle \hat{a}_L \rangle_{QM} e^{-i \Theta([\hat{X}, \hat{P}]_{mod})}$$

Θ for various models:

$\mu_0 \frac{32 \hbar \mathcal{F}^2 m N_p}{M_p^2 \lambda_L^2 \omega_m}$	$\gamma_0 \frac{96 \hbar^2 \mathcal{F}^3 N_p^2}{M_p c \lambda_L^3 m \omega_m}$	$\beta_0 \frac{1024 \hbar^3 \mathcal{F}^4 N_p^3}{3 M_p^2 c^2 \lambda_L^4 m \omega_m}$
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Proposed experimental setup:

- Single optical pulse
- Short opto-mechanical interaction
- Pulse storage for 1/4 mechanical period
- 4 iterations
- Homodyne readout



Deformations of center-of-mass observable even for $\beta_0, \mu_0, \gamma_0 \lesssim 1$

NEW EXPERIMENTAL BOUNDS WITH HIGH-Q RESONATORS

Tests of commutator deformations by F. Marin et al (AURIGA collaboration):

- Change in normal modes: anomalous ground state energy $E = \frac{\beta}{2} \hbar \omega$
- Experiment: compare to measured modal temperature in AURIGA

F. Marin et al., Nature Physics 9, 71–73 (2013)

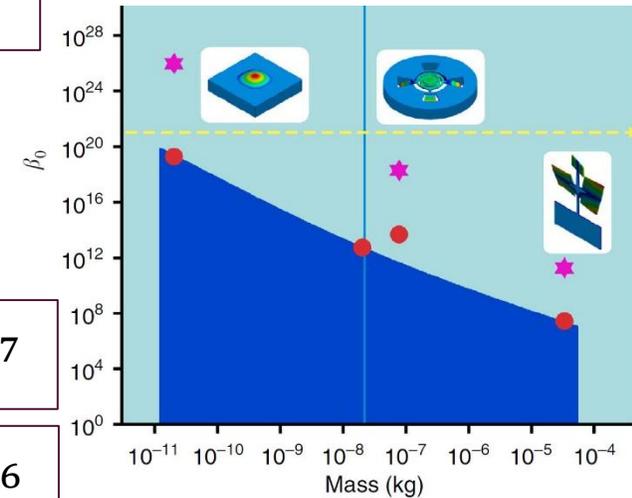
Measured: $\beta_0 < 10^{33}$

- Change in harmonic motion: Modified amplitude and frequency of motion $A(t) = A_0 \left(\sin \omega t + \frac{\beta}{8} A_0 \cos 3 \omega t \right)$ $\omega = \left(1 + \frac{\beta}{2} A_0 \right) \omega_0$

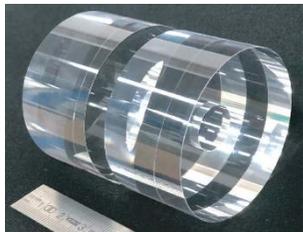
M. Bawaj et al, Nature Comm. 6, 7503 (2015)

Measured: $\beta_0 < 3 \times 10^7$

Measured: $\beta_0 < 5 \times 10^6$



Using Sapphire bar in Bushev & Tobar groups:



P.A. Bushev et al., PRD ,066020 (2019)

So far only classical systems! Also stringent bounds from classical dynamics

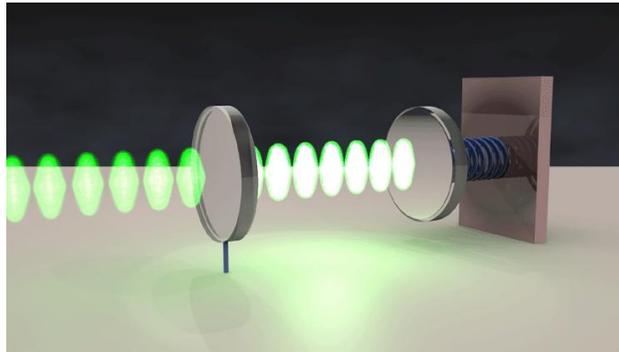
C. Quesne, V. Tkachuk. PRA 81, 012106 (2010); S. Kumar, M. Plenio. Nat. commun. 11, 1-8 (2020)

SUMMARY: QUANTUM GRAVITY PHENOMENOLOGY

Table-top tests of quantum gravity start to become possible

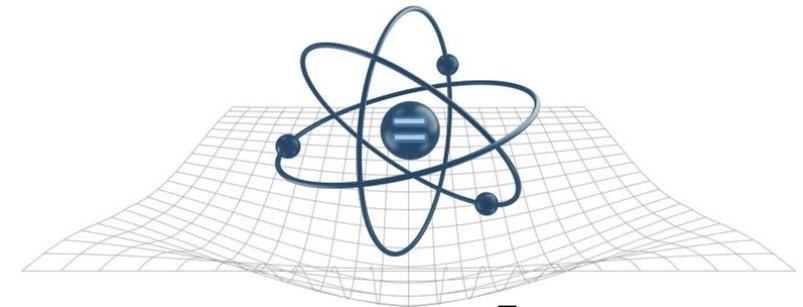


Relies on novel technology and creativity



Could we also observe “conservative” quantum gravity as expected?

Surprisingly, **yes!**



COUPLING OF MATTER TO GRAVITY

Newtonian gravity: mass couples to potential $\phi(x)$

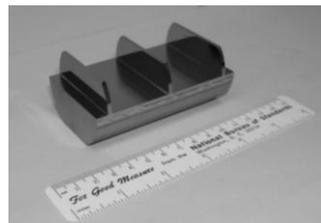
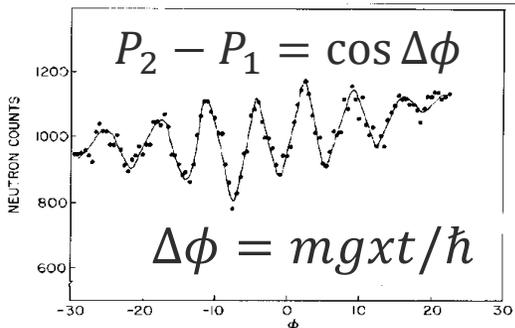
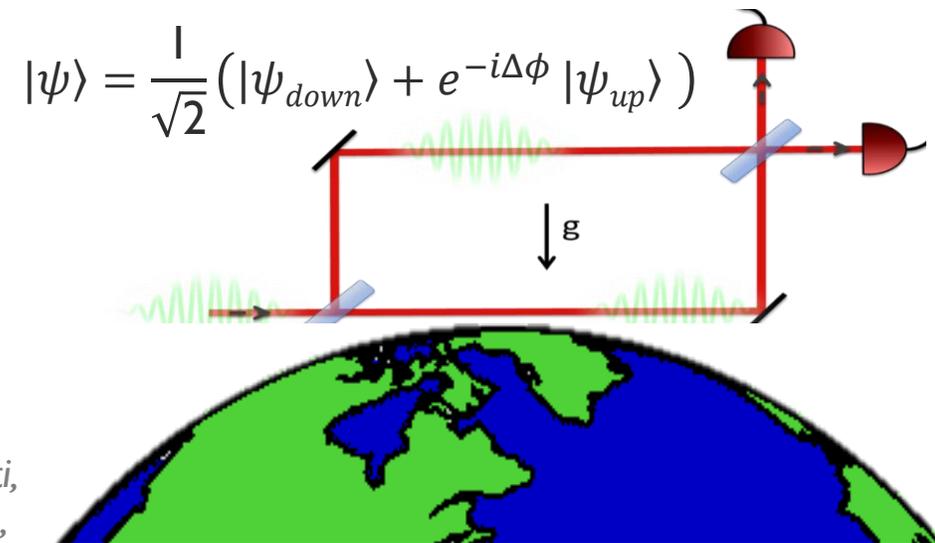
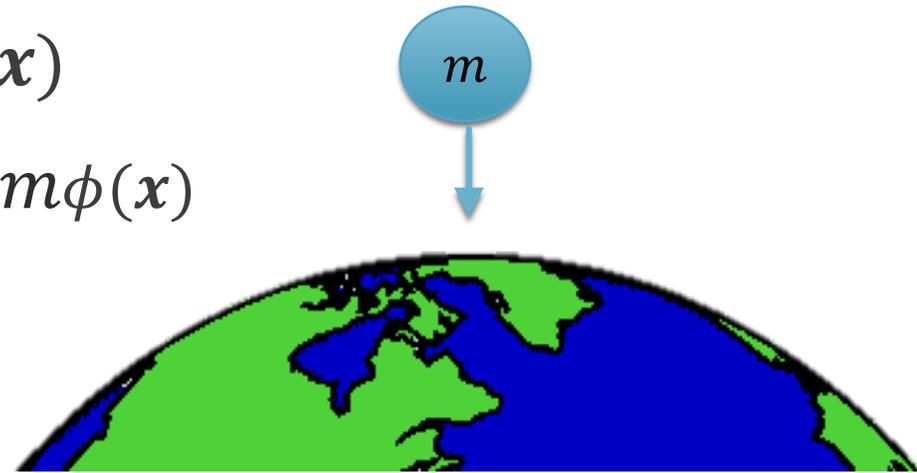
- Simple coupling captured by Hamiltonian $H = m\phi(x)$

Well tested also for quantum systems:

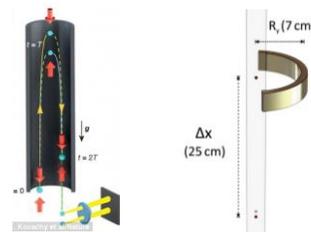
- Matter-wave superpositions acquire a phase

$$\Delta\phi = m\Delta\phi t/\hbar$$

Observed in COW (neutrons) & atomic fountains



Colella, Overhauser, Werner, PRL 34, 1472-1474 (1975)



Overstreet, Asenbaum, Curti, Kim, Kasevich. Science 375, 226-229 (2022)

HAMILTONIAN FOR INTERACTION WITH GRAVITY

Coupling between matter and linear general relativity:

$$H_{int} = - \int d^3x \frac{1}{2} T_{\mu\nu} h^{\mu\nu}$$

Why?

Einstein's equations:
$$R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

Equivalent action:
$$S = S_{EH} + S_M = \frac{c^4}{16\pi G} \int d^4x \sqrt{-g} R + S_M$$

Variation in general:
$$\delta S(a, b, \dots) \equiv \int d^4x \frac{\delta S}{\delta a} \delta a + \int d^4x \frac{\delta S}{\delta b} \delta b + \dots$$

Only gravity:
$$\frac{\delta S_{EH}}{\delta g^{\mu\nu}} = \frac{c^4}{16\pi G} \int d^4x \sqrt{-g} (R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu}) \equiv 0 \quad \text{Euler-Lagrange}$$

With matter:
$$\delta S \equiv \int d^4x \frac{\delta S_{EH}}{\delta g^{\mu\nu}} \delta g^{\mu\nu} + \int d^4x \frac{\delta S_M}{\delta g^{\mu\nu}} \delta g^{\mu\nu} \equiv 0 \quad \rightarrow \quad T_{\mu\nu} \equiv \frac{-2}{\sqrt{-g}} \frac{\delta S_M}{\delta g^{\mu\nu}}$$

HAMILTONIAN FOR INTERACTION WITH GRAVITY

Coupling between matter and linear general relativity:

$$H_{int} = - \int d^3x \frac{1}{2} T_{\mu\nu} h^{\mu\nu}$$

Why?

$$T_{\mu\nu} \equiv \frac{-2}{\sqrt{-g}} \frac{\delta S_M}{\delta g^{\mu\nu}}$$

Linearize gravity: $g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}$ $|h_{\mu\nu}| \ll |\eta_{\mu\nu}|$

flat Minkowski

Perturbation: "gravity"

Keep only linear terms in $h_{\mu\nu}$

Linearized GR equations look a lot like Maxwell's E&M! Here: only coupling to matter

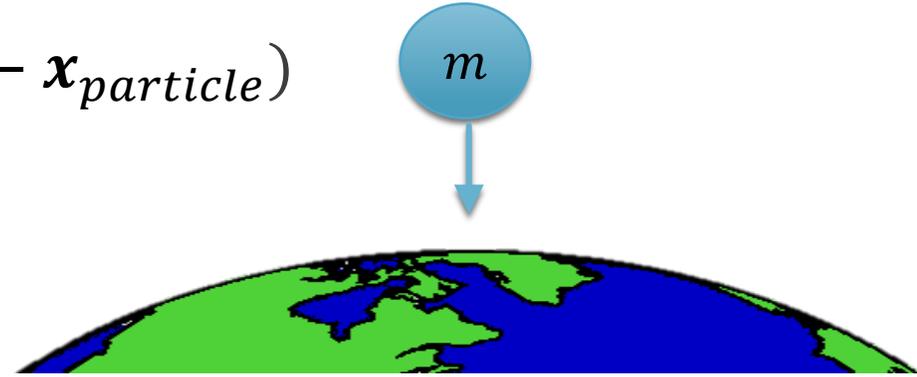
$$S_M \text{ now linear in } h^{\mu\nu} \text{ (} g^{\mu\nu} = \eta^{\mu\nu} - h^{\mu\nu} \text{): } T_{\mu\nu} \equiv 2 \frac{\delta S_M}{\delta h^{\mu\nu}} \Leftrightarrow S_M \equiv \frac{1}{2} \int d^4x T_{\mu\nu} h^{\mu\nu}$$

$$\text{Lagrange density } \mathcal{L} = \frac{1}{2} T_{\mu\nu} h^{\mu\nu} \Leftrightarrow \text{Hamiltonian } H = - \int d^3x \mathcal{L} \text{ (small velocities)}$$

COUPLING OF MATTER TO GRAVITY

E.g.: Newtonian $h_{00} = -2 \frac{\phi(\mathbf{x})}{c^2}$ $T_{00} = mc^2 \delta(\mathbf{x} - \mathbf{x}_{particle})$

$$H_{int} = m\phi(\mathbf{x}_{particle})$$



E.g.: Gravitational wave in local frame

$$T_{00} = mc^2 \delta(\mathbf{x} - \mathbf{x}_{cm}) \quad h_{00} = -R_{0i0j} x^i x^j$$

Fermi normal coordinates \rightarrow tidal force $R_{0i0j} = -\frac{1}{2c^2} \partial_0 \partial_0 h_{ij}$

$$H_{int} = \frac{h_0}{4} m \omega^2 \epsilon_{ij} x^i x^j e^{i(\vec{k} \cdot \vec{x} - \omega t)} \quad \vec{k} \cdot \vec{x} \ll 1$$

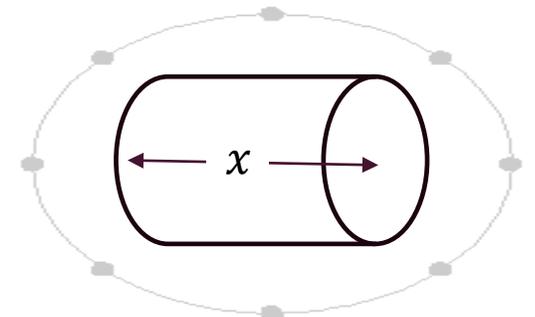
Long wavelength

$$\epsilon_{ij} = \delta_{ix} \delta_{jx}$$

Perpendicularly polarized

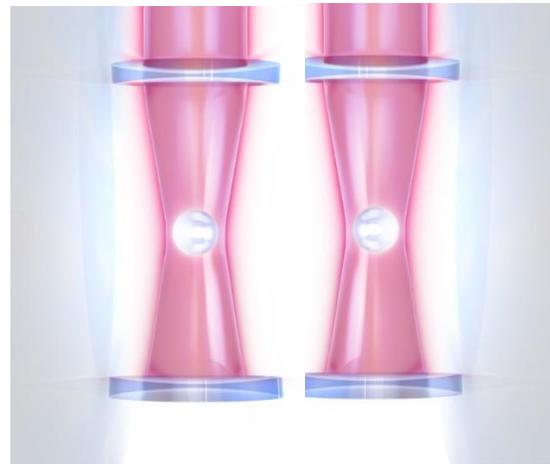
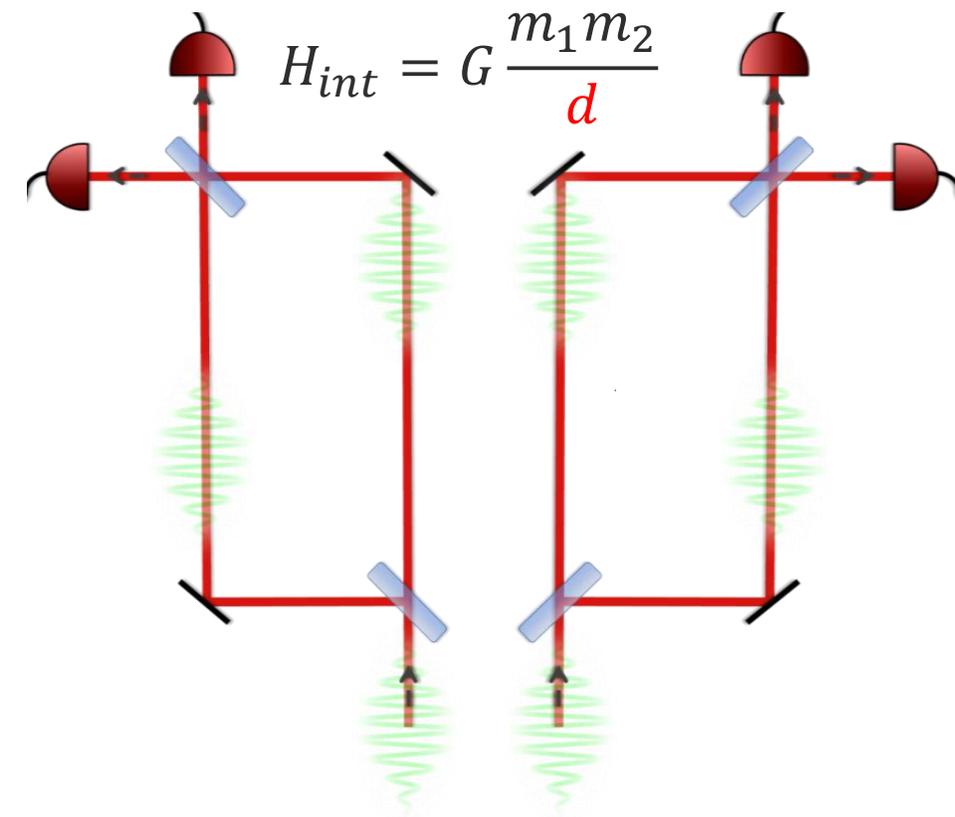
$$h_{ij} = \epsilon_{ij} h_0 e^{i(\vec{k} \cdot \vec{x} - \omega t)}$$

GW polarization \swarrow \nwarrow Plane wave, amplitude h_0



$$H_{int} \approx \frac{h_0}{4} m \omega^2 x^2$$

EXPERIMENTAL PROPOSAL: INDIRECT SIGNATURE OF GRAVITONS?



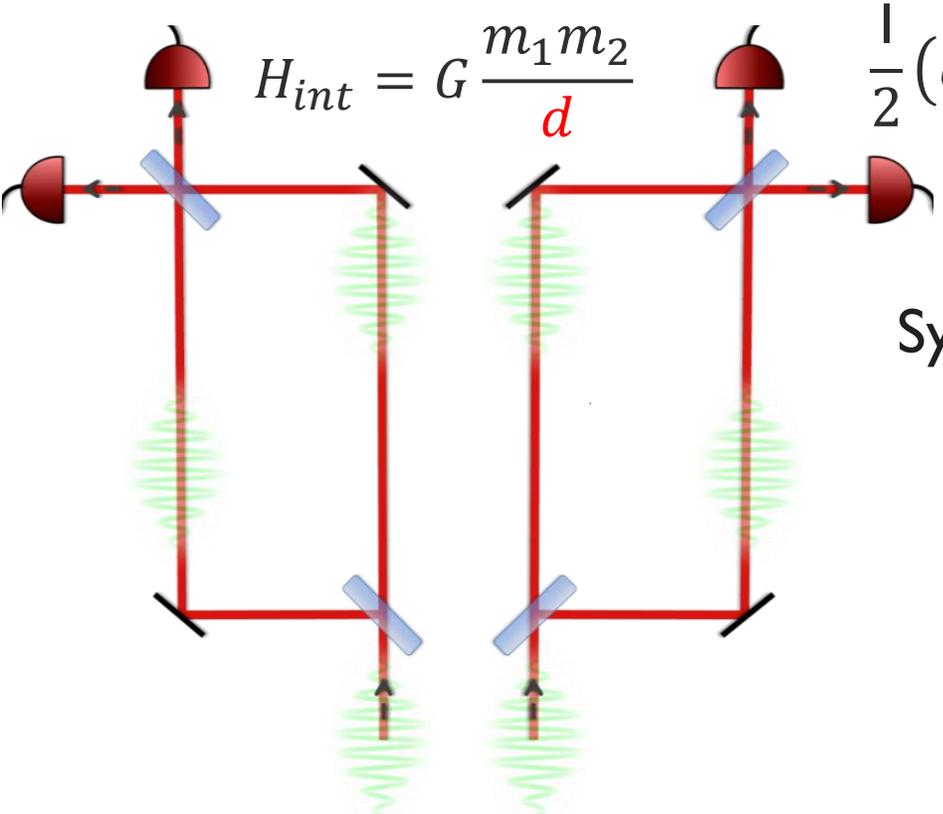
Basic idea:

- Probe if gravity can *generate* entanglement
- Sources of gravity are themselves in superposition
- Entanglement is between the masses, not entanglement of gravity

Bose et al. "Spin entanglement witness for quantum gravity." PRL 119, 240401 (2017)

Marletto, Vedral. "Gravitationally induced entanglement between two massive particles is sufficient evidence of quantum effects in gravity." PRL 119, 240402 (2017)

EXPERIMENTAL PROPOSAL: INDIRECT SIGNATURE OF GRAVITONS?



$$H_{int} = G \frac{m_1 m_2}{d}$$

$$\frac{1}{2} (e^{i\varphi_{LL}} |\psi_L\rangle |\chi_L\rangle + e^{i\varphi_{LR}} |\psi_L\rangle |\chi_R\rangle + e^{i\varphi_{RL}} |\psi_R\rangle |\chi_L\rangle + e^{i\varphi_{RR}} |\psi_R\rangle |\chi_R\rangle)$$

$$\varphi_{ii} = G \frac{m_1 m_2 t}{d_{ii} \hbar} \quad \text{Entangled state, maximal:} \quad t = \frac{\pi d_{LR} \hbar}{G m_1 m_2}$$

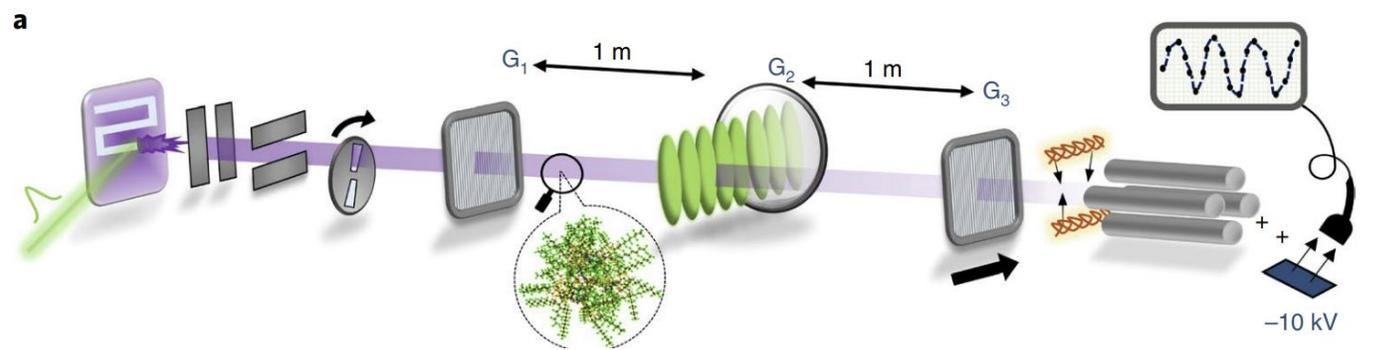
System parameters: $d_{LR} = 0.25 \text{ mm}$ $m = 10^{-14} \text{ kg}$ $t = 10 \text{ s}$

Extremely challenging

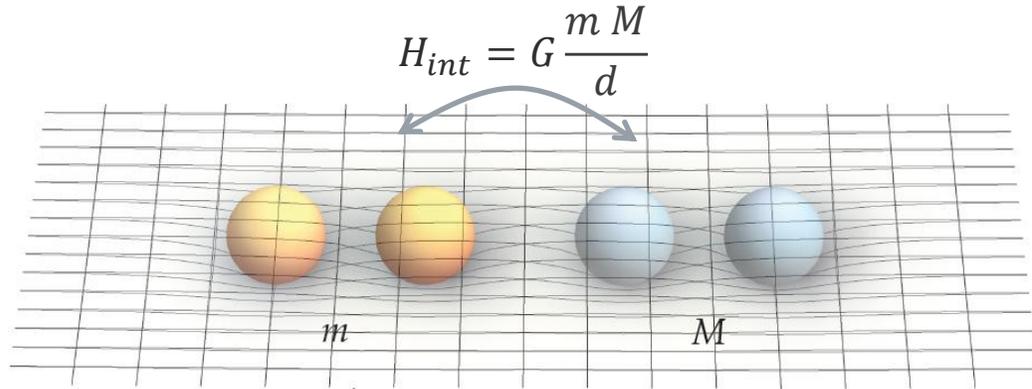
World-record today (Arndt group): 2,000 atoms

Y.Y. Fein et al. *Nature Physics* 15, 1242–1245 (2019)

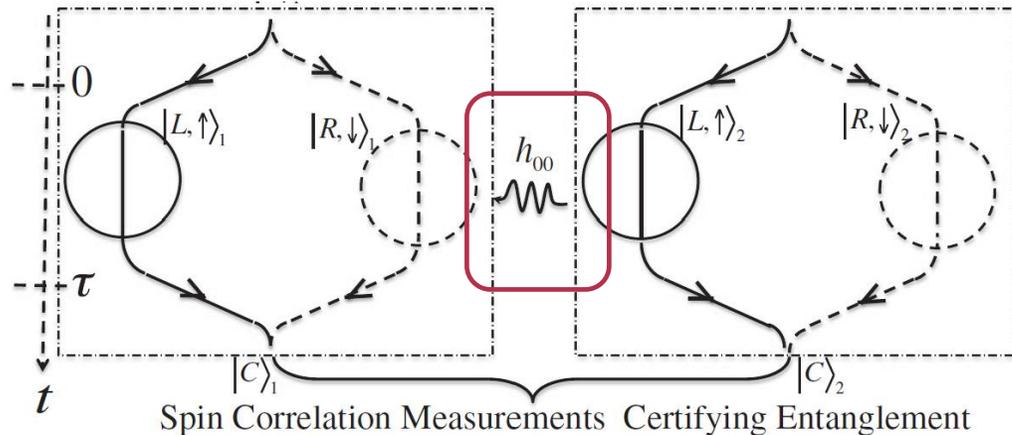
$$\frac{1}{\sqrt{2}} (|\psi_L\rangle + |\psi_R\rangle) \otimes \frac{1}{\sqrt{2}} (|\chi_L\rangle + |\chi_R\rangle)$$



EXPERIMENTAL PROPOSAL: INDIRECT SIGNATURE OF GRAVITONS?



Source of gravity is in superposition, creates superposed potential / space-time



Argument of authors:

Bose et al. PRL 119, 240401 (2017)

Marletto, Vedral. PRL 119, 240402 (2017)

If entanglement is mediated *locally*, then the mediator must be quantized

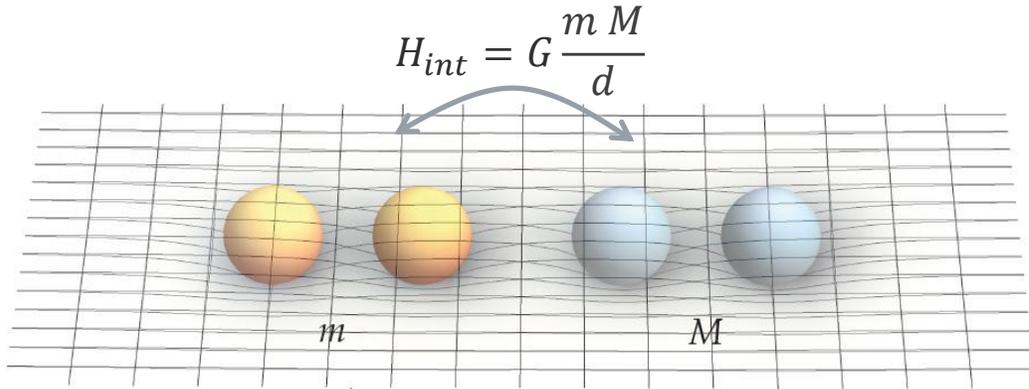
LOCC: Local operations and classical communication cannot increase entanglement

Why local operation? Exchange of a mediating particle \rightarrow graviton

But this depends on additional *assumptions*

V. Fragkos*, M. Kopp*, I. Pikovski. "On inference of quantization from gravitationally induced entanglement" *AVS Quantum Sci.* 4, 045601(2022)

NEWTONIAN VIEW: ACTION AT A DISTANCE



In what sense is gravity *in superposition*?

Use 2nd quantized language in this non-relativistic case:

Non-relativistic quantum field operator: $\hat{\psi}^\dagger(\vec{x}_1)|0\rangle = |\vec{x}_1\rangle$

$$\hat{H} = \int d^3x \left(\frac{\hbar^2}{2m} \nabla \hat{\psi}^\dagger(\vec{x}) \nabla \hat{\psi}(\vec{x}) + m \hat{\Phi}(\vec{x}) \hat{\psi}^\dagger(\vec{x}) \hat{\psi}(\vec{x}) \right)$$

$$\nabla^2 \hat{\Phi}(\vec{x}) = 4\pi G m \hat{\psi}^\dagger(\vec{x}) \hat{\psi}(\vec{x})$$

From Newtonian perspective:

Entanglement generated via instantaneous interaction

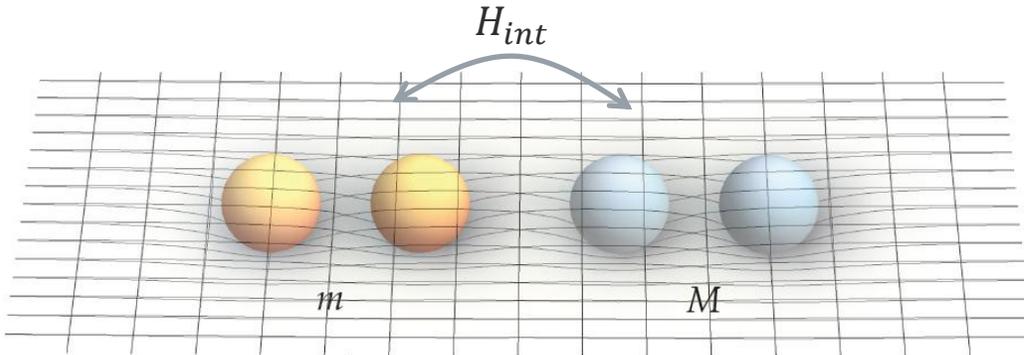
$$\hat{H} = \sum_{i=1}^N \left(\frac{\hat{p}_i^2}{2m} - \frac{m^2 G}{2} \sum_{j=1, j \neq i}^N \frac{1}{|\hat{x}_i - \hat{x}_j|} \right)$$

Gravitational potential
requires quantization:

$$\hat{\Phi}(\vec{x}, t) = -mG \int d^3x' \frac{\hat{\psi}^\dagger(\vec{x}') \hat{\psi}(\vec{x}')}{|\vec{x} - \vec{x}'|}$$

Shows: Insufficient to use mean field

RELATIVISTIC VIEW: FORMULATION #1



Relativistic perspective: $g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}$

$$H_{int} = -\frac{1}{2} \int d^3r h_{\mu\nu}(\vec{r}) T^{\mu\nu}(\vec{r})$$

How is entanglement generated? Quantize?

Gupta, Proc. Phys. Soc. A 65, 161 (1952)

In Lorentz / de Donder gauge:

$$\hat{h}_{\mu\nu}(\vec{r}) = \int d^3k \sqrt{\frac{\hbar G}{c^2 \pi^2 \omega_k}} \left[\hat{a}_{\mu\nu}(\vec{k}) e^{i\vec{k}\cdot\vec{r}} + \hat{a}_{\mu\nu}^\dagger(\vec{k}) e^{-i\vec{k}\cdot\vec{r}} \right]$$

$$\partial^\mu \bar{h}_{\mu\nu} = 0 \text{ with } \bar{h}_{\mu\nu} \equiv h_{\mu\nu} - 1/2 h_{\mu}^{\mu}$$

Has 10 quantized degrees of freedom $\hat{a}_{\mu\nu}$, not 2!

The 8 fictitious d.o.f are removed by imposing $\left[\hat{a}_{3\nu}(\vec{k}) - \hat{a}_{0\nu}(\vec{k}) + \kappa \int_{t=t'} d^3x' D^{(+)}(\vec{x} - \vec{x}') \hat{T}_{0\nu}(\vec{x}') \right] |\chi\rangle = 0$

But: these 'ghosts' contribute in virtual processes & entanglement

Simple toy model for entanglement: $|\Psi_0\rangle \equiv |0\rangle_A \otimes |0\rangle_B \otimes |\vec{0}\rangle_\gamma$

Franson, Phys. Rev. A 84, 033809 (2011)

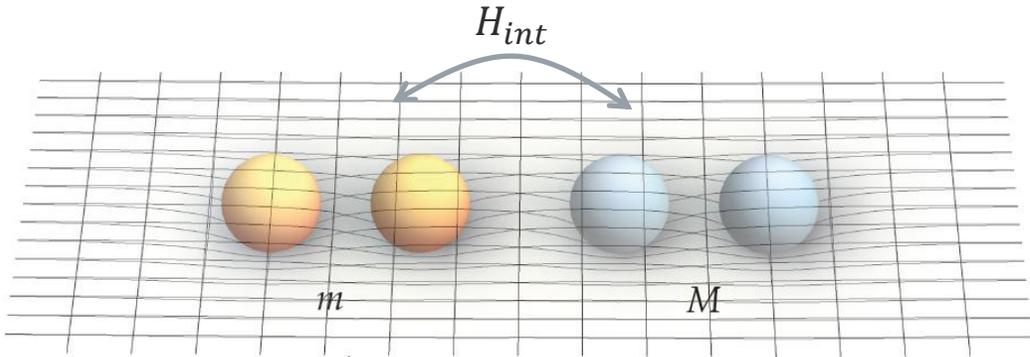
$$|\Psi\rangle \simeq |\Psi_0\rangle + \varepsilon_L |\Psi_2\rangle \quad |\Psi_2\rangle = |1\rangle_A \otimes |1\rangle_B \otimes |\vec{0}\rangle_\gamma$$

$$\varepsilon_L = \sum_l \frac{\langle \Psi_2 | \hat{H}_I | l \rangle \langle l | \hat{H}_I | \Psi_0 \rangle}{(E_0 - E_1)(E_0 - E_l)}$$

These fictitious mediators generate entanglement (not 'normal' gravitons)

Also in Bose et al. PRD 105, 106028 (2022)

RELATIVISTIC VIEW: FORMULATION #2



Relativistic perspective: $g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}$

$$H_{int} = -\frac{1}{2} \int d^3r h_{\mu\nu}(\vec{r}) T^{\mu\nu}(\vec{r})$$

How is entanglement generated? Quantize?

In Poisson gauge: $h_{00} = -2\phi$

$$h_{0i} = w_i$$

$$h_{ij} = -2\psi\delta_{ij} + 2s_{ij}$$

s_{ij} : real GWs!

$$\partial_j s_i^j = 0 \quad \text{and} \quad \partial_i w^i = 0$$

Bertschinger, MIT lecture notes (1999)

Quantization of only 2 physical d.o.f.: $s_{ij}^{TT} \rightarrow \hat{S}_{ij}^{TT}$

After some algebra (*Bertschinger, MIT lecture notes*)

$$\hat{H}_{int} = - \int d^3r (\hat{s}_{ij}^{TT} \hat{T}^{ij}) - \frac{G}{2} \int \frac{d^3r d^3r'}{|\vec{r} - \vec{r}'|} \left[-4\hat{f}_{\perp,i}(\vec{r}') \hat{T}^{0i}(\vec{r}) + \hat{T}_{00}(\vec{r}') (\hat{T}^{00}(\vec{r}) + \hat{T}_k^k(\vec{r}) - 2\hat{\Pi}^{\parallel}(\vec{r})) \right]$$

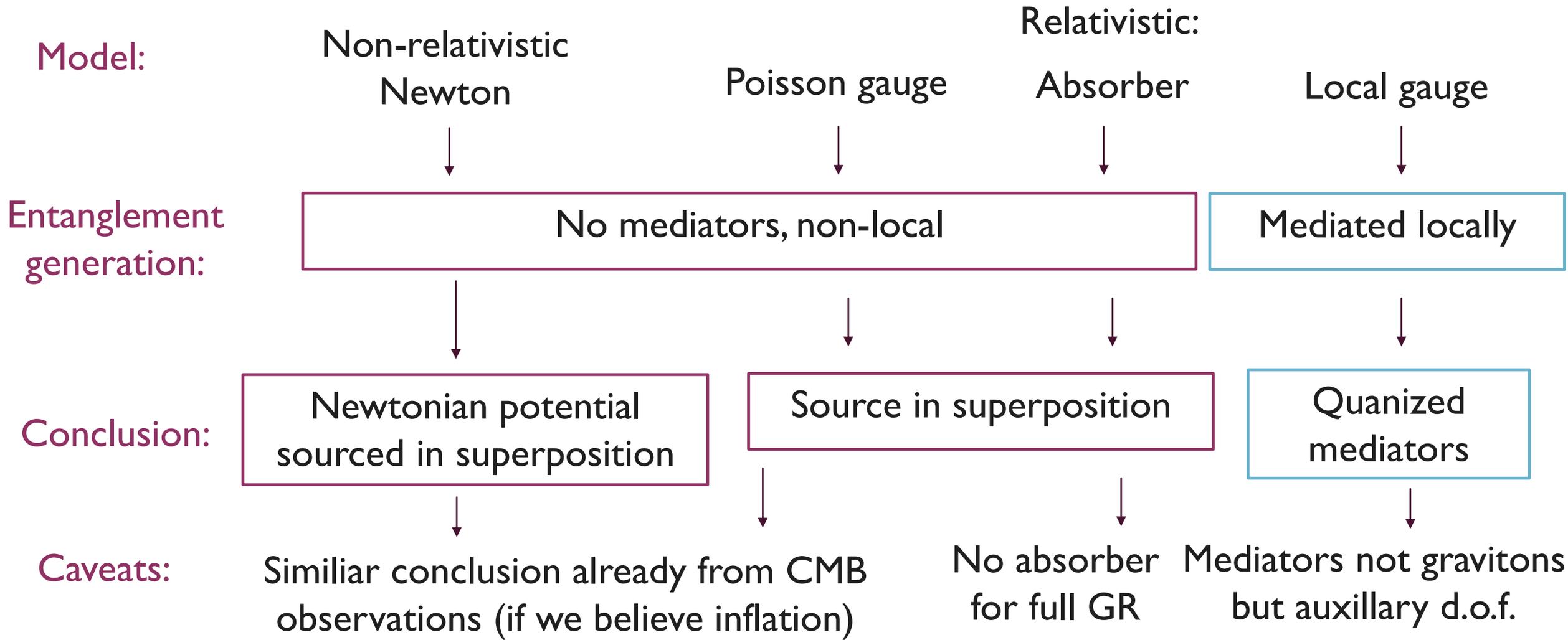
subdominant in GIE

$\propto \hat{T}_{\perp}^{0i}$
Dominant entangling term

\propto Traceless stress-energy tensor

Entanglement generated nonlocally without gravitational d.o.f., as in Newtonian case

SUMMARY OF CONCLUSIONS FROM ENTANGLEMENT

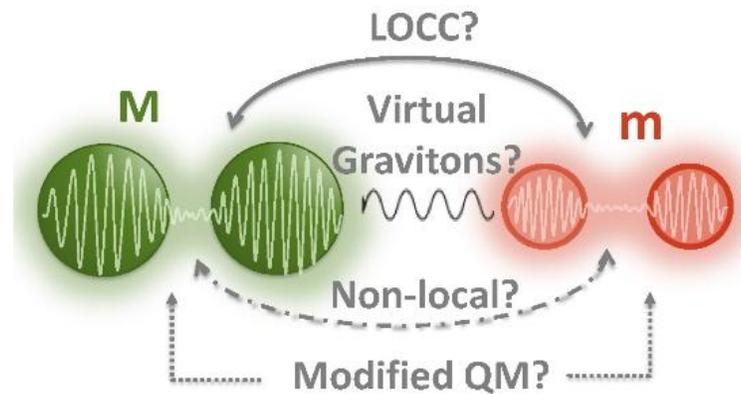
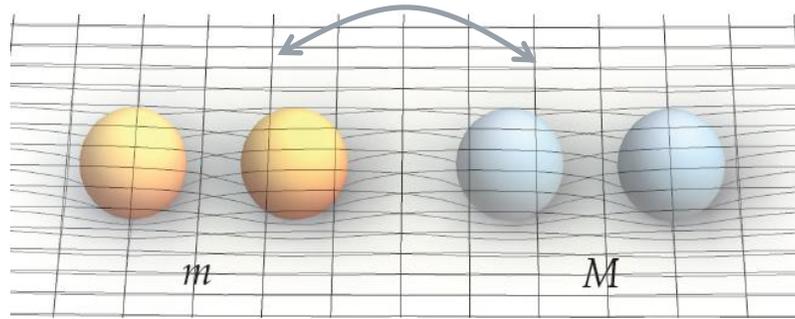


SUMMARY: GRAVITATIONALLY INDUCED ENTANGLEMENT (GIE)

GIE will show quantum sources of gravity

Only test of a virtual “graviton” if we describe in one specific gauge

Could we also observe a real graviton directly?



Surprisingly, **yes!**

G. Tobar*, S. Manikandan*, T. Beitel, I. Pikovski.
Nature Communications 15, 7229 (2024)

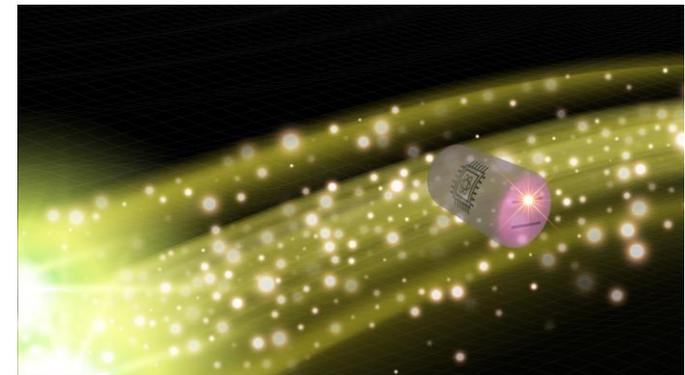


TABLE-TOP ROUTES TO QUANTUM GRAVITY

Testing **speculative** models



High-precision test of new physics beyond QM, GR.

Marshall et al 2003

Pikovski et al 2012

Bekenstein 2012

Kafri et al 2014

Belenchia et al 2016

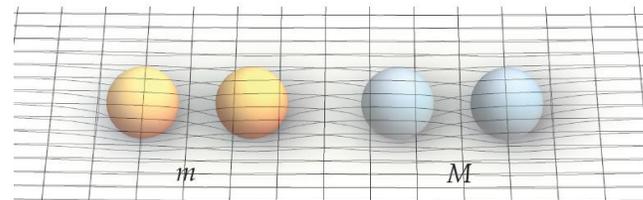
Oppenheim 2023

...

Caveats:

Tests only speculative models.

Detecting **entanglement** mediated by gravity



Indirect test of QGR, assuming local mediator of entanglement

Bose et al 2017

Marletto Vedral 2017

Lami et al 2024

...

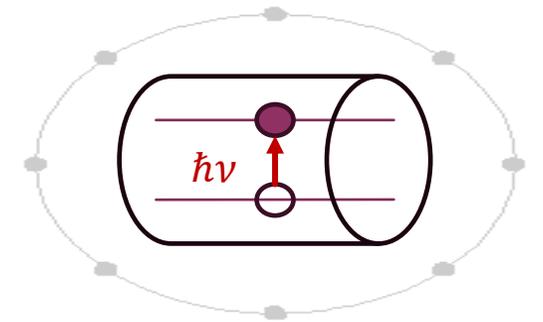
Caveats:

Interpretation ambiguous: no input on mediator quantization

Fragkos, Kopp, Pikovski. PRD 2022

Anastopoulos, Hu. C&QG, 2020

Detecting **gravitons**



Here: Observation of quantized energy exchange

G. Tobar*, S. Manikandan*, T. Beitel, I. Pikovski.
Nature Communications 15, 7229 (2024)

Probing expected single-graviton physics as predicted in linearized QGR

Caveats:

Cannot rule out some semi-classical models

DETECTING GRAVITONS: PHOTOELECTRIC ANALOGY

Dyson 2013, Journal of Modern Physics A 28, 1330041 (2013):

The simplest kind of graviton detector is an electron in an atom,

We have a splendid natural generator of thermal gravitons with energies in the kilovolt range, producing far more gravitons than any artificial source. It is called the sun.

Second, the gravitoelectric detector for kilovolt gravitons,

Rothman Boughn 2006, Classical and quantum gravity 23, 5839. (2006):

Because in RB we decided on the gravitational analogy of the photoelectric effect as a method for detecting gravitons, it was necessary to compute the gravito-ionization cross section for hydrogen in the ground state.



Discrete energy $E=hf$



Extracted from background

SINGLE GRAVITON PROCESSES IN QM

Weinberg, "Gravitation and Cosmology" 1972:

states. In particular, in the quadrupole approximation the total rate for an atom to make a transition $a \rightarrow b$ by emitting gravitational radiation is

$$\Gamma(a \rightarrow b) = \frac{2G\omega^5}{5\hbar} [D_{ij}^*(a \rightarrow b)D_{ij}(a \rightarrow b) - \frac{1}{3}|D_{ij}(a \rightarrow b)|^2] \quad (10.8.6)$$

where

$$D_{ij}(a \rightarrow b) \equiv m_e \int \psi_b^*(\mathbf{x})x_ix_j\psi_a(\mathbf{x}) d^3\mathbf{x} \quad (10.8.7)$$

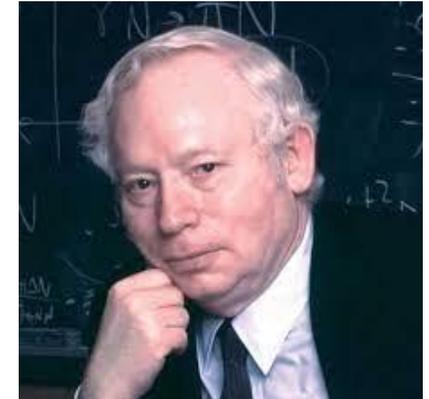
with ψ_a, ψ_b the initial and final state wave functions. For instance, the rate for decay of the $3d(m = 2)$ state of the hydrogen atom into the $1s$ state with emission of one graviton is

$$\Gamma(3d \rightarrow 1s) = \frac{2^{23}Gm_e^3c}{3^{75}15^{15}(137)^6\hbar^2} = 2.5 \times 10^{-44} \text{ sec}^{-1}$$

Actually $\Gamma = 5.7 \times 10^{-40} \text{ s}^{-1}$

Boughn & Rothman 2006

Needless to say, there is no chance of observing such a transition.



SINGLE GRAVITON PROCESSES IN QM

Bronstein 1935, Feynman 1963, Dyson 1969, Weinberg 1972, Lightman 1973, Boughn & Rothman 2006

Interaction in linearized gravity:
$$H_{int} = -\frac{1}{2} T_{\mu\nu} h^{\mu\nu}$$

Electron:
$$T_{\mu\nu} = m_e u_\mu u_\nu = \frac{1}{m_e} p_\mu p_\nu$$

GWs in TT-gauge:
$$h^{0\mu} = 0 \quad h^{ij} = \frac{1}{\sqrt{V}} \sum_{\mathbf{k}, \lambda} \epsilon_{\mathbf{k}, \lambda}^{ij} h_{\mathbf{k}, \lambda} e^{i(\mathbf{k} \cdot \mathbf{r} - \omega t)} + cc$$

Normalization Polarization Polarization tensor Fourier amplitudes

SINGLE GRAVITON PROCESSES IN QM

Quantize:
$$\hat{h}^{ij} = \sum_{\mathbf{k}, \lambda} e_{\mathbf{k}, \lambda}^{ij} h_{q\mathbf{k}, \lambda} \hat{a} e^{i(\mathbf{k} \cdot \mathbf{r} - \omega t)} + cc$$

$$h_{q\mathbf{k}, \lambda} = \sqrt{\frac{16\pi G \hbar}{c^2 \nu_{\mathbf{k}} V}}$$

Graviton transition rate:

$$\Gamma_{atom} (i \rightarrow f) = \frac{2\pi}{\hbar} |\langle i | \langle 0 | \hat{H}_{int} | 1 \rangle | f \rangle|^2 \rho$$

$$\rho = \frac{V \nu^2}{2\pi^2 \hbar c^3}$$

Density of graviton states

$$\Gamma_{atom} (3d \rightarrow 1s) = \frac{2\pi}{\hbar} \frac{m_e^2 \nu^4}{16c^2} \frac{8\pi G \hbar}{\nu V} \frac{V \nu^2}{2\pi^2 \hbar c^3} \int d^3r \psi_{3d} r^2 \psi_{1s} \approx 10^{-40} s^{-1}$$

RECALL: COUPLING OF MATTER TO GRAVITY

We found before: Hamiltonian for interaction with GW

$$H_{int} = \frac{h_0}{4} m \omega^2 \varepsilon_{ij} x^i x^j e^{i(\vec{k} \cdot \vec{x} - \omega t)}$$

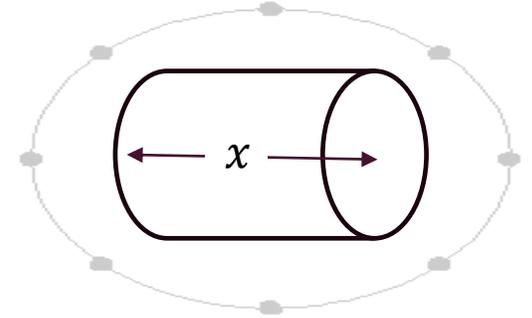
$$\vec{k} \cdot \vec{x} \ll 1$$

Long wavelength

$$\varepsilon_{ij} = \delta_{ix} \delta_{jx}$$

Perpendicularly polarized

$$H_{int} \approx \frac{h_0}{4} m \omega^2 x^2$$



- Coupling of GW to matter
- h_0 very, very small! $h_0 \lesssim 5 \times 10^{-22}$ (GW150914)
- $m x^2 = Q$: detector mass quadrupole moment



Joe Weber



Use big detector!

ACHIEVING OBSERVABLE GRAVITON PROCESSES

Three modifications make **gravitons** observable

G.Tobar*, S. Manikandan*, T. Beitel, I. Piovski. Nature Communications 15, 7229 (2024)

A. Focus on **acoustic** modes in **macroscopic** quantum systems: $\sigma \gg L_p^2$

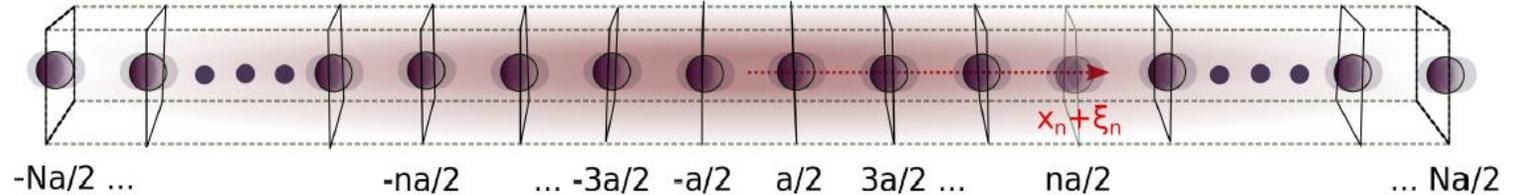
B. Focus on **stimulated** single graviton exchange during GW passage: $F \sim \frac{10^{28}}{m^2 s^1}$

C. Focus on **quantum sensing** of single discrete energy transitions: $\Delta E = hf$

When **all three** are met, one can achieve **single graviton detection**

A. MACROSCOPIC QUANTUM INTERACTION

$$H_{int} = -\frac{1}{2} h_{\mu\nu} T^{\mu\nu}$$



- $N + 1$ atoms with mass m , distance a apart, $M = m(N + 1)$
- Local inertial frame: $H_{int} = -\frac{1}{2} h_{00} T^{00}$. Tidal: $h_{00} = -R_{0a0b} x^a x^b = \frac{\ddot{h}_{xx}(t)}{2} (x_j + \xi_j)^2$
- $H_{int} = -\frac{m}{4} \ddot{h}_{xx} \sum_{j=-N}^N (2x_j \xi_j + \xi_j^2) = -\frac{ML\ddot{h}_{xx}}{\pi^2} \sum_{l=1,3,\dots}^N \left((-1)^{\frac{l-1}{2}} \frac{1}{l^2} \chi_l \right) - \frac{M}{8} \ddot{h}_{xx} \sum_{l=0}^N \chi_l^2$
- N individual atom quadrupoles, but collective modes χ_l scaled up with M and L
- Quantized dominant interaction: $\hat{H}_{int} = \sqrt{ML} \ddot{h}_{xx} \frac{\sqrt{\hbar}}{\sqrt{\omega_l} \pi^2} \sum_{l=1,3,\dots}^N \frac{(-1)^{\frac{l-1}{2}}}{l^2} \left(\hat{b}_l + \hat{b}_l^\dagger \right)$

B. STIMULATED EMISSION & ABSORPTION

$$\Gamma_{stim} (1 \rightarrow 0) = \frac{2\pi}{\hbar} \left| \langle 1 | \langle \alpha | \hat{H}_{int} | \alpha \rangle | 0 \rangle \right|^2 \rho = \frac{|\alpha|^2 8GM L^2 \omega_l^4}{l^4 \pi^4 c^5}$$

$$|\alpha|^2 \approx N = \frac{h_0^2 c^5}{32\pi G \hbar \omega_l^2}$$

$$\Gamma_{stim} = \frac{ML^2 \omega_l^2}{4l^4 \pi^5 \hbar} h_0^2 = \frac{M v_s^2}{4l^4 \pi^3 \hbar} h_0^2$$

ρ_m : mass density
 $v_s = \frac{L\omega_l}{l\pi}$: sound speed

Example: Aluminum bar $M = 1800 \text{ kg}$ $v_s = 5.4 \frac{\text{km}}{\text{s}}$

$$h_0 = 5 \times 10^{-22} \quad (\text{GWI50914})$$

$$\Gamma_{stim} = 1 \text{ Hz}$$

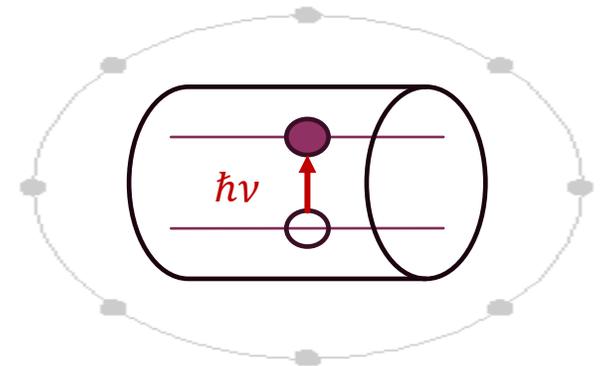
One graviton emitted/absorbed per second



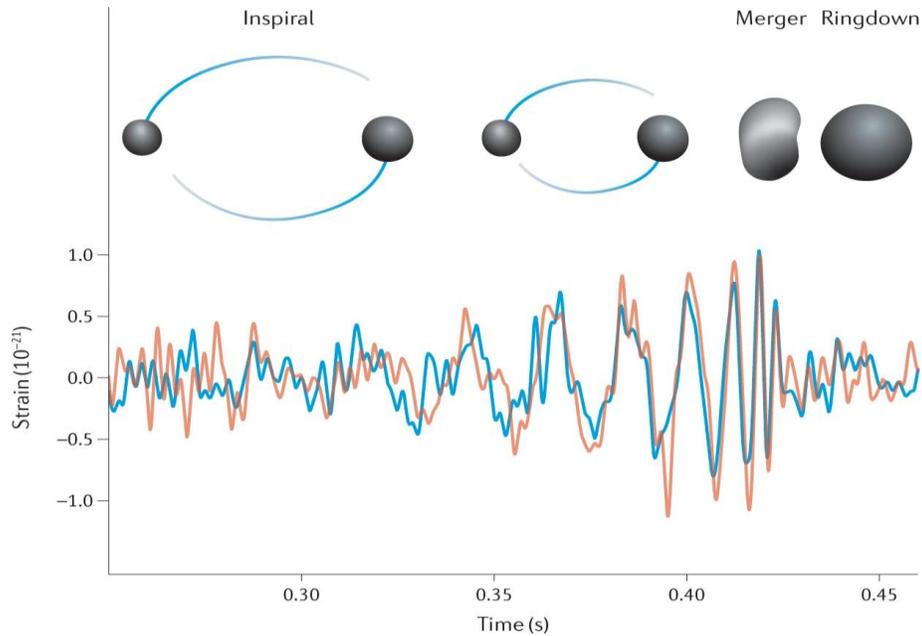
Joe Weber

QUANTUM HINTS FROM STIMULATED PROCESSES

- Can we see signatures of **discrete exchange** of energy between matter and gravity?
- **Individual** events indicate exchange of a **single** quantum of energy
- Resolve a single **quantum jump** by discrete energy due to absorption of single graviton
- Stimulated process, and discreteness: analogy to historic photoelectric effect



C. QUANTUM SENSING OF ENERGY



Bailes et al., Nat Rev Phys 3, 344–366 (2021)

Dynamics of quantum matter under GW:

$$\hat{H} = \hbar\omega\hat{b}^\dagger\hat{b} + \frac{L}{\pi^2} \sqrt{\frac{M\hbar}{\omega}} \ddot{h}(t)(\hat{b} + \hat{b}^\dagger)$$

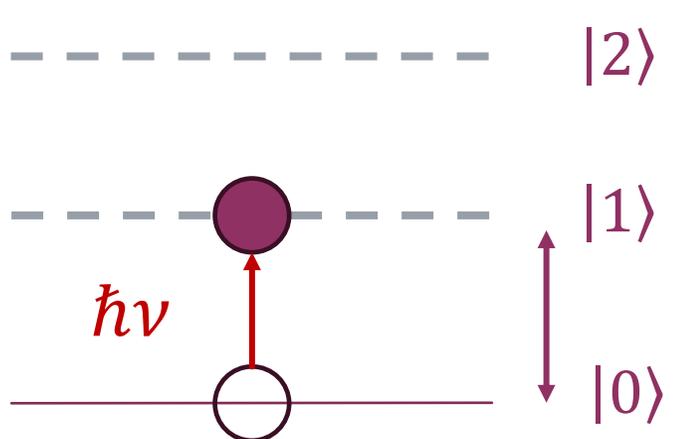
Results in the **exact** dynamics, found for example by Magnus expansion:

$$\hat{U} = e^{-i\varphi} e^{-\omega t\hat{b}^\dagger\hat{b}} \hat{D}(\beta)$$

(analogous to quantum optics case: Glauber 1965)

$$\beta = -i \frac{L}{\pi^2} \sqrt{\frac{M\hbar}{\omega}} \int_0^t ds \ddot{h}(s) e^{i\omega s}$$

C. QUANTUM SENSING OF ENERGY



$|2\rangle$ Single energy transition probability: $P = |\langle 1 | \hat{U} | 0 \rangle|^2$

Maximized: $P_{max} = 0.37$, for $|\beta|_{max} = 1$

$|\beta| = \frac{L}{\pi^2} \sqrt{\frac{M}{\omega \hbar}} \chi(h, \omega, t) \quad \chi(h, \omega, t) = \left| \int_0^t ds \dot{h}(s) e^{i\omega s} \right|$

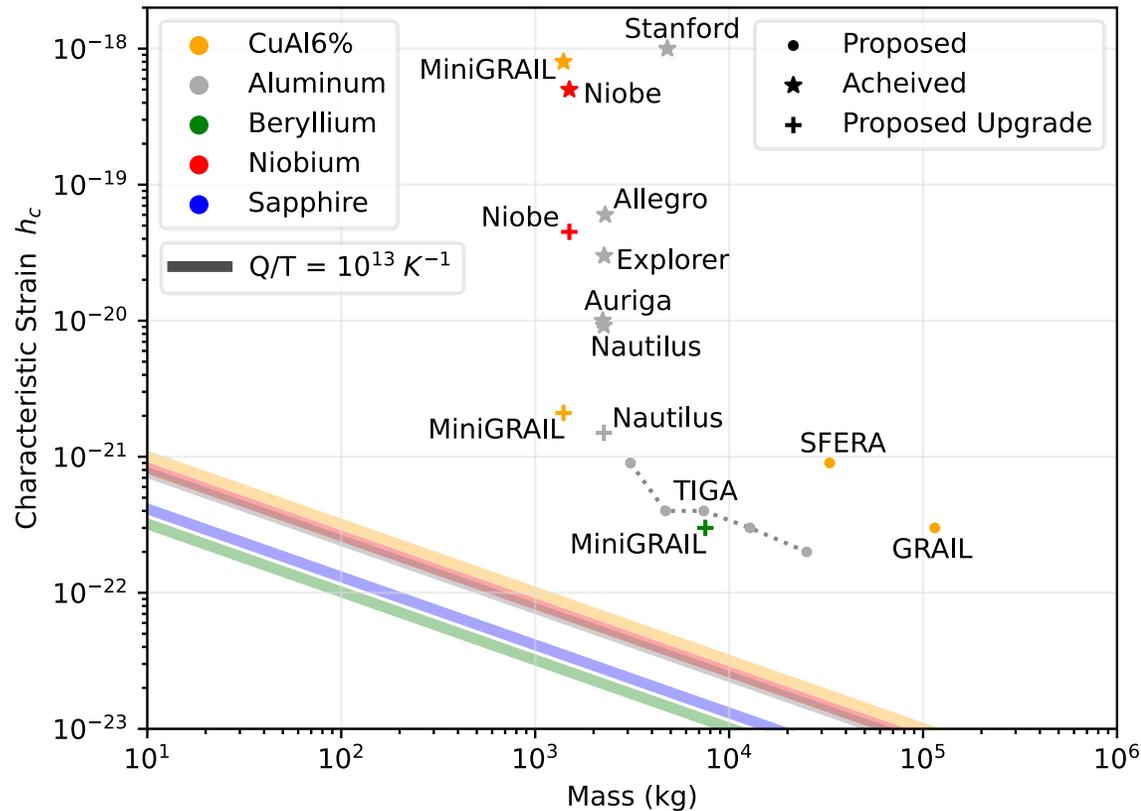
Ideal detector mass for **single** graviton detection:

$$M = \frac{\pi^2 \hbar \omega^3}{v_s^2 \chi(h, \omega, t)}$$

ESTIMATED PARAMETERS FROM GW SOURCES

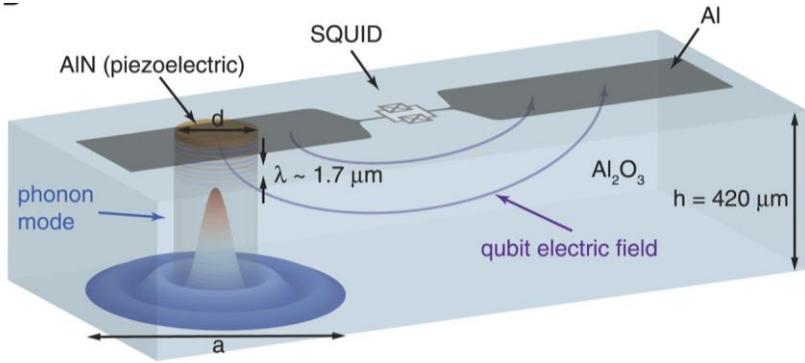
GW Source	GW170817 (NS-NS merger)	GW170817 (NS-NS merger)	GW170608 (BH-BH merger)	GW150914 (BH-BH merger)	J1301+0833 (black-widow pulsar)	J1748–2446ad (fast-spinning pulsar)	A0620-00 (BH Super-radiance)	Primordial (rare BH-BH merger)
$f = \frac{\omega}{2\pi}$	100 Hz	150 Hz	175 Hz	200 Hz	1085 Hz	1433 Hz	33 kHz	5.5 MHz
$h_0(f)$	2×10^{-22}	2×10^{-22}	2×10^{-22}	10^{-21}	$< 10^{-25}$	$< 10^{-25}$	3×10^{-21}	10^{-16}
M_c	$1.19 M_{\odot}$	$1.19 M_{\odot}$	$7.9 M_{\odot}$	$28.6 M_{\odot}$	Continuous	Continuous	Continuous	$5 \times 10^{-4} M_{\odot}$
Material	Beryllium	Aluminum	Niobium	CuAl6%	Niobium	Superfluid He-4	Sapphire	Quartz
v_0	13 km/s	5.4 km/s	5 km/s	4.1 km/s	5 km/s	238 m/s	10 km/s	6.3 km/s
T	1 mK	1 mK	1 mK	1 mK	0.1 μ K	0.1 μ K	0.6 K	0.6 mK
Q-factor	10^{10}	10^{10}	10^{10}	10^{10}	10^{10}	10^{13}	10^{10}	10^{10}
M	~ 15 kg	~ 250 kg	~ 9 t	~ 6 t	> 52 t	> 20 t	~ 100 kg	~ 10 g

COMPARISON TO PREVIOUS BAR DETECTORS

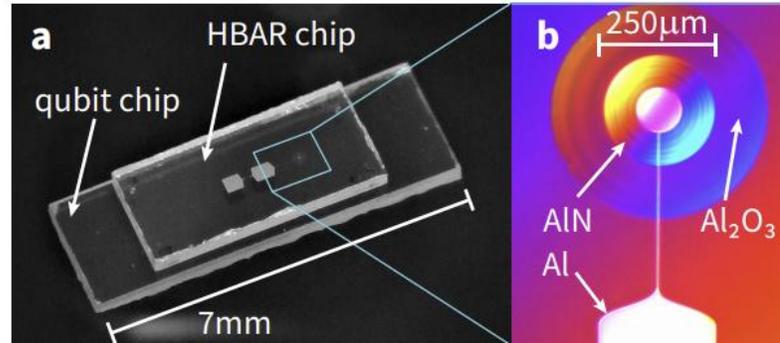


- If using the detector to simply detect gravitational waves: comparison to old and proposed bar detectors
- Lines show our envisioned strain sensitivity
- Need additional quantum sensing capability of energy levels

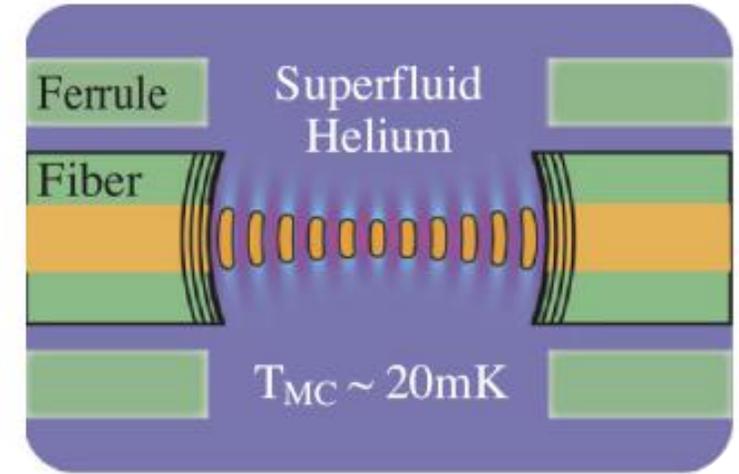
MEASURING INDIVIDUAL ACOUSTIC PHONONS



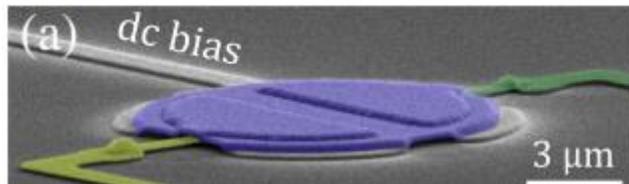
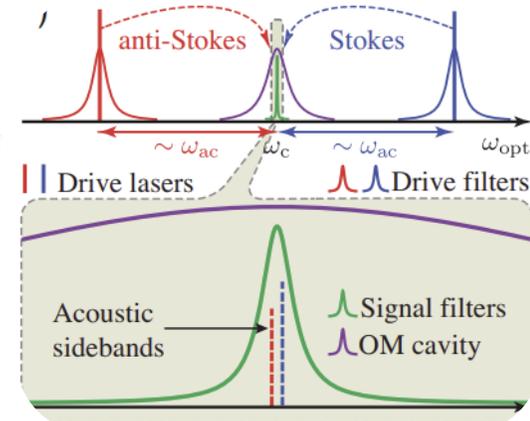
Chu, ... Schoelkopf. *Science* 358, 199-202 (2017)



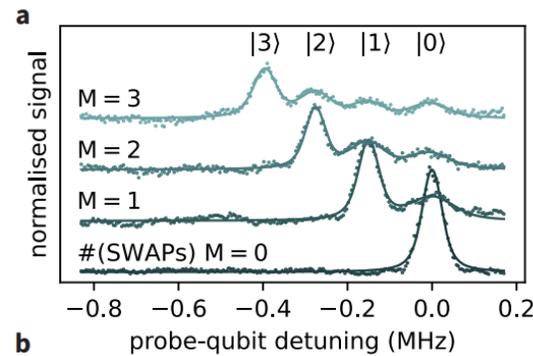
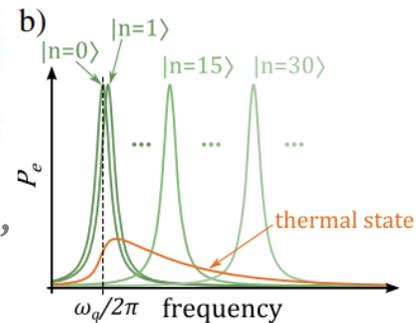
von Lüpke, ... Chu. *Nature Physics* 18, 794–799 (2022)



Patil, ... Harris. *PRL* 128, 183601 (2022)



Viennot, Ma, Lehnert. *PRL* 121, 183601 (2018)



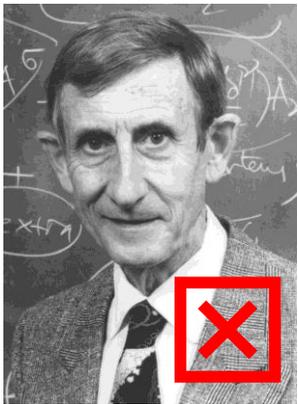
DETECTING SINGLE GRAVITONS WITH QUANTUM SENSING

Single graviton detection is possible

Tobar*, Manikandan*, Beitel, Pikovski.
Nature Communications 15, 7229 (2024)

- A. Focus on **macroscopic quantum** systems
- B. Focus on **stimulated emission/absorption** of single gravitons
- C. Focus on **quantum sensing** of quantum jumps
- D. Correlate to **classical detections** of gravitational waves

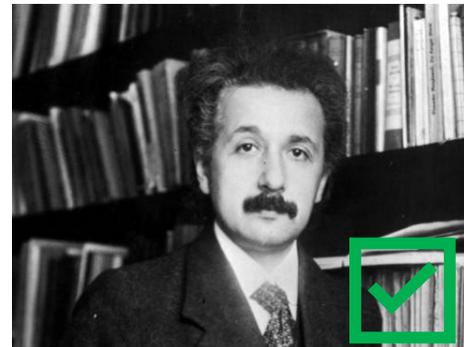
Single gravitons can be detected in realistic experiments!



Dyson. "Is a graviton detectable?" (2013)



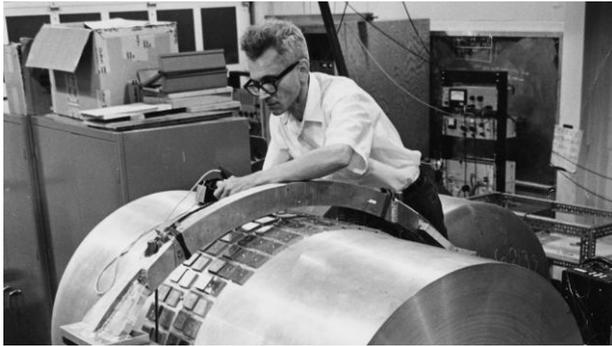
Weber. "Detection and Generation of Gravitational Waves" (1960)



Einstein. "Über einem die Erzeugung und Verwandlung des Lichtes betreffenden heuristischen Gesichtspunkt" (1905)

Gravito-phononic
analogue of photoelectric
effect, with quantum
acoustic resonators

COMPARISON TO PREVIOUS RESULTS



Well-known in other community: resonant GW detection

$$\sigma \sim L_p^2 \frac{v_s M L}{\hbar} = \frac{G M L^2 \omega}{c^3}$$

Maggiore, "Gravitational Waves" 2008

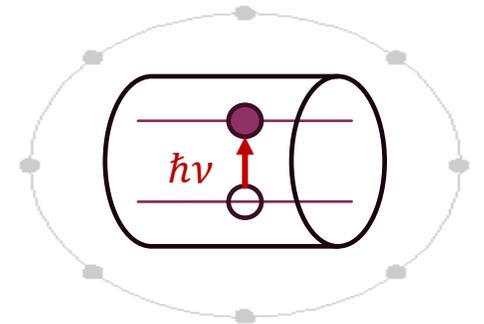
We therefore discover that the ultimate limitation for a resonant bar operating with a linear amplifier is given by the uncertainty principle,

$$\Delta E_{\min} \gtrsim \hbar \omega_0. \quad (8.164)$$

This is known as the *standard quantum limit*. It states that the best we can do (with a linear amplifier) is to detect an acoustic oscillation of the fundamental mode of the bar which, at the quantum level, corresponds to a single phonon.

In our work: Use **macro-system** coupling,
but still resolve **single quantum jumps as in atoms**

Bars aimed to operate "at quantum limit", but only on average with position measurements



GRAVITONS VS PROOF OF QUANTIZATION

Would the experiment **prove** quantization of gravity?

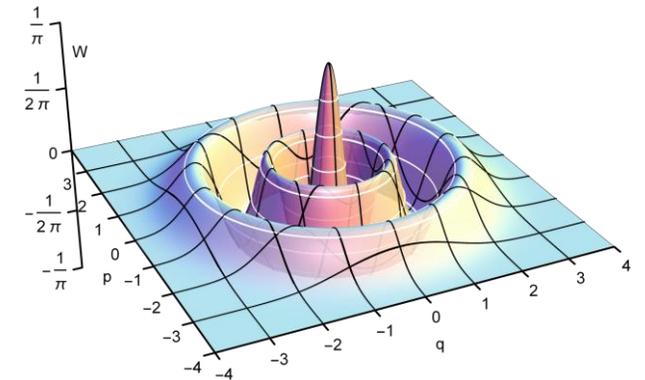
No!

A *semiclassical* description is possible, just like for the photoelectric effect

$$\hat{H}_{QGR} = g \ddot{\hat{h}}(t) \hat{x} \quad \text{vs} \quad H_{SC} = g \ddot{h}(t) \hat{x}$$

To rule out *this* semiclassical model, need more:

- Particle anti-bunching
- Sub-Poisson statistics
- HoM effect



GRAVITONS VS PROOF OF QUANTIZATION

We can't distinguish this semi-classical model, but that's **not the goal**

$$\hat{H}_{QGR} = g \ddot{\hat{h}}(t) \hat{x} \quad \text{vs} \quad H_{SC} = g \ddot{h}(t) \hat{x}$$

- A very specific model, violates energy conservation
- Artificial “test model”, not normal classical GR
- Many other models with “hybrid classical-quantum coupling”
- Even ruling out this model does not prove quantization
- Not a relevant benchmark

HISTORIC PERSPECTIVE: INSPIRATION FROM EARLY QM

What can we learn about quantization of gravity?



Mark Suppiah, Victoria Shenderov, Isabella Marotta
(high school interns)

“Stimulated absorption of single gravitons: First light on quantum gravity”

arXiv:2407.11929



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Roger W. Babson
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President

The trustees are pleased to announce the Awards for Essays for 2024.

Selected for Honorable Mention this year were (listed in alphabetical order): Francesco Alessio and Michele Arzano; Spyros Basilakos, Dimitri V. Nanopoulos, Theodoros Papanikolaou, Emmanuel N. Saridakis and Charalampos Tzerefos; Elmo Benedetto, Christian Corda and Ignazio Licata; Nigel T. Bishop, Vishnu Kakkat, Amos S. Kubeka, Monos Naidoo and Petrus J. van der Walt; Philippe Brax and Pierre Vanhove; Molly Burkmar and Marco Bruni; Juan A. Cañas, A. Martin-Ruiz and J. Bernal; Raúl Carballo-Rubio and Astrid Eichhorn; Juanca Carrasco-Martinez; Man Ho Chan; S. Mahesh Chandran and S. Shankaranarayanan; Hong Zhe Chen; RY Chiao, NA Inan, DA Singleton, ME Tobar; Sayantan Choudhury; A. A. Coley; Bruno Arderucio Costa; Jesse Daas, Cristobal Laporte, Frank Saueressig and Tim van Dijk; John Bruce Davies; Arthur E. Fischer; T. R. Govindarajan; Eduardo Guendelman; Yuan K. Ha; Shahar Hod; Viqar Husain, Irfan Javed, Sanjeev Seahra and Nomann X; Lawrence M. Krauss, Francesco Marino, Samuel L. Braunstein, Mir Faizal and Naveed A. Shah; Philip D. Mannheim; Alexander I. Nesterov; Fabrizio Pinto; Tom Rudelius; Jorge G. Russo; **Victoria Shenderov, Mark Suppiah, Thomas Beitel, Sreenath K. Manikandan and Igor Pikovski**; Tejinder P. Singh; Slava G. Turyshev; C.S. Unnikrishnan; Jenny Wagner

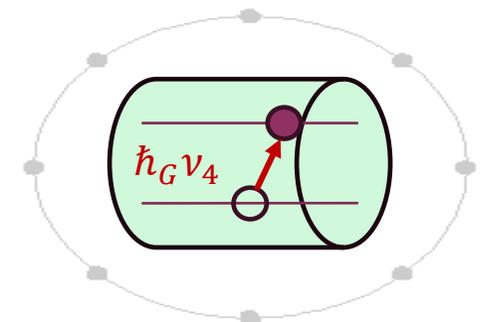
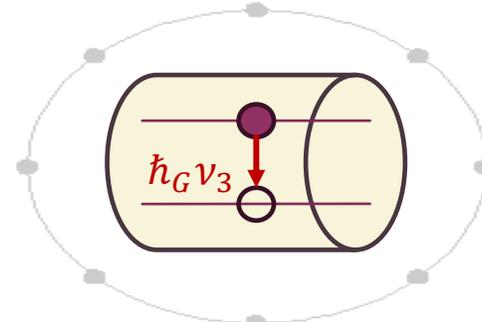
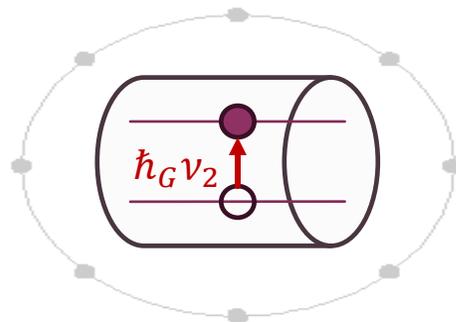
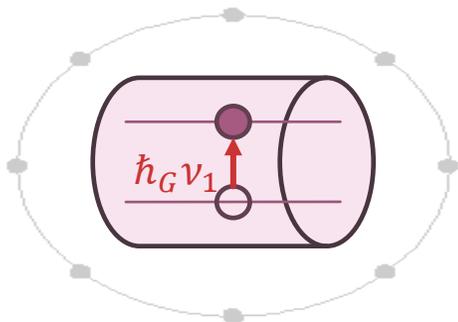
This announcement and abstracts of award-winning and honorable mention essays are posted on our web site, <http://www.gravityresearchfoundation.org>. The five award-winning essays are also posted on our website and will be published in the October 2024 SPECIAL ISSUE of the International Journal of Modern Physics D (IJMPD).

TESTING INTERACTION ON QUANTUM LEVEL

We propose **several simple tests** of linearized quantum gravity

$$H_{int} = -\frac{1}{2} \hat{T}_{\mu\nu} \hat{h}^{\mu\nu}$$

- Is energy content in graviton as expected? $\hbar_G = \hbar$?
- Is \hbar_G universal for all matter?
- Same stimulated emission and absorption rates?
- Is it a spin-2 transition?
- Combine with other experimental input?



SUMMARY

- New quantum technologies open possibility of QGR experiments
- Push towards tests of gravitationally induced collapse of the wavefunction
- Other QGR models also testable in table-top setups: empirical input (and exclusion plots) for QGR
- Indirect test can provide hints of QGR, use quantum information concepts to show nonclassicality
- Direct detection of single gravitons is possible: macroscopic quantum resonators + sensing

