Motional ground-state cooling of single atoms in state-dependent optical tweezers

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(Received 7 February 2023; accepted 22 June 2023; published 9 August 2023)

Laser cooling of single atoms in optical tweezers is a prerequisite for neutral atom quantum computing and simulation. Resolved sideband cooling comprises a well-established method for efficient motional ground-state preparation, but typically requires careful cancellation of light shifts in so-called magic traps. Here, we study a novel laser cooling scheme which overcomes such constraints, and applies when the ground state of a narrow cooling transition is trapped stronger than the excited state. We demonstrate our scheme, which exploits sequential addressing of red sideband transitions via frequency chirping of the cooling light, at the example of ⁸⁸Sr atoms and report ground-state populations compatible with recent experiments in magic tweezers. The scheme also induces light-assisted collisions, which are key to the assembly of large atom arrays. Our work enriches the toolbox for tweezer-based quantum technology, also enabling applications for tweezer-trapped molecules and ions that are incompatible with resolved sideband cooling conditions.

DOI: 10.1103/PhysRevResearch.5.033093

I. INTRODUCTION

Quantum control of individual atoms trapped in optical tweezers has seen a very rapid development in the last years [1], which has opened routes for applications such as quantum computing and simulation [2–4], precision metrology [5,6], or ultracold chemistry [7,8]. The quest for high-fidelity operations on the internal states of the atoms, for example, logic gate operations or optical clock interrogation, also requires cooling of the external motion, ideally down to the quantum mechanical ground state of the tweezer trap [9,10]. Efficient ground-state preparation is also key for assembling Hubbard-type lattice models atom by atom with optical tweezers [11,12], or for realizing ultrafast quantum gate protocols via resonant Förster interactions [13].

Large motional ground-state occupation is typically achieved using well-established sideband-resolved cooling protocols [9,10], which more recently also became available for alkaline-earth(-like) atom arrays exploiting their narrow intercombination transitions [14–16]. Sideband laser cooling, however, poses tight constraints on the trapping condition, as it requires careful cancellation of differential light shifts for the internal atomic states involved in the cooling cycle, a situation referred to as magic trapping. Consequently,

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many of the applications mentioned above, including optical tweezer-based atomic clocks [5,6] or novel concepts for qubit implementations in gate-based quantum processors [17,18], are incompatible with such constraints. Novel laser cooling mechanisms that work at more general conditions thus not only expand the toolbox for neutral atom quantum technology, but may also find applications in controlling optically trapped molecules or even ions [19–21].

In this paper, we demonstrate a method for motional ground-state cooling at the example of single trapped ⁸⁸Sr atoms which is applicable in the generic situation of sizable differential light shifts between the relevant atomic states. The strategy relies on a frequency chirp of the cooling light to quench the population of initially occupied motional states towards the trap ground state. A detailed theoretical proposal and analysis thereof has been reported recently in Ref. [22]. Optimizing the cooling parameters, we measure ground-state populations exceeding 80% along the radial (more strongly confined) tweezer axis. At the same time, the cooling protocol efficiently removes pairs of atoms from the trap via light-assisted collisions resulting in a final 50% filling probability with exactly one atom, prerequisite for the systematic assembly of large atom arrays [23,24].

II. GROUND-STATE COOLING SCHEME FOR STATE-DEPENDENT TWEEZERS

We consider an atom with two internal electronic states $|g\rangle$ and $|e\rangle$ trapped in the Gaussian-shaped potential formed by an optical tweezer [Fig. 1(a)]. Sufficiently close to the trap bottom, the atom is harmonically confined with state-dependent oscillator frequencies ω_g and ω_e , respectively. Standard side-

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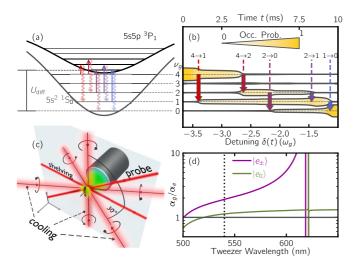


FIG. 1. Chirp-cooling in state-dependent optical tweezers. (a) Radial tweezer potential for the $|g\rangle = |{}^1S_0\rangle$ and $|e\rangle = |{}^3P_1\rangle$ states of the cooling transition. The state-dependent trap depth enables transfer of excited motional states into the trap ground-state via strong red sideband transitions, reducing ν_{σ} by $\Delta\nu > 1$ vibrational quanta (arrows denote excitation and subsequent spontaneous decay). The potential curves are offset vertically so that $U_{\rm diff}$ indicates the (positive) light shift of the electronic transition between the motional ground states from the free-space resonance. (b) Numerical simulations of the cooling dynamics, demonstrating ground-state transfer when the laser detuning δ (measured from the trap shifted resonance at $U_{\rm diff}$) is ramped from a large red detuning towards $\delta \approx -\omega_{\rm g}$. The thickness of the yellow areas is proportional to the population in $|v_g\rangle$. Arrows indicate population transfer when the resonance condition for the sideband transitions drawn in (a) is matched. (c) Experimental realization: Single ⁸⁸Sr atoms are trapped in an optical tweezer (green), using a high-NA objective. The polarization of the tweezer light is indicated by the arrow in the NA cone. Chirpcooling is realized with three pairs of counter-propagating, circularly polarized 689 nm MOT beams (cooling). Additional laser beams (probe and shelving) are used for sideband thermometry. (d) Ratio of the AC polarizability (and hence of the trap depths) between $|{}^{1}S_{0}\rangle$ and the light-shifted substates $|e_0\rangle$ and $|e_+\rangle$ of $|^3P_1\rangle$ as a function of trapping wavelength. The dotted line indicates the wavelength used in the experiment.

band cooling (Raman- or single-photon scheme) requires equal AC polarizabilities α_e and α_g for the electronic levels, yielding identical ladders of motional states independent of the atom's internal state. Provided a narrow laser transition between $|g\rangle$ and $|e\rangle$ with linewidth $\gamma\ll\omega_g$ (festina lente regime, see Refs. [25,26] for its importance in all-optical cooling schemes to Bose-Einstein condensation), one can then cool the atomic motion in the trap by setting the laser to a fixed frequency resonant with the first red sideband, i.e., detuned by $-\omega_g$ from the free-space transition frequency. Magic trapping($\alpha_e=\alpha_g$) ensures, that the condition for addressing the red sideband is independent of the harmonic oscillator level

Such persistent cooling conditions are no longer given when the trapping potential is state-dependent ($\alpha_e \neq \alpha_g$). Only very recently, it has been demonstrated that efficient cooling into the trap ground state can still be realized with

a fixed laser frequency for $\alpha_g/\alpha_e < 1$, i.e., when the excited state $|e\rangle$ is trapped stronger than the ground state $|g\rangle$ [27,28]. Here, we investigate the opposite case, $\alpha_{\sigma}/\alpha_{\rho} > 1$, for which cooling with a fixed frequency cannot work. This can be seen in Fig. 1(a), which depicts the situation we study in our experiment. Specifically, we employ the narrow $(\gamma = 2\pi \times 7.4 \text{ kHz})^{-1}S_0$ to 3P_1 intercombination transition at a laser wavelength of about 689 nm for in-trap cooling. It is convenient to define the laser detuning δ with respect to the trap-shifted resonance condition $U_{\rm diff}/\hbar$ [see Fig. 1(a)] for driving the electronic transition with the atom in the motional ground state, i.e., $|g, v_g = 0\rangle$ to $|e, v_e = 0\rangle$. Here, $v_g(v_e)$ is the harmonic oscillator quantum number of the ground (excited) state vibrational ladder. In our scenario where $\omega_e < \omega_e$, the resonance condition to drive the red sideband $\delta \approx (\nu_g - 1)\omega_e - \nu_g \omega_g$ now depends on ν_g . An attempt to cool the lowest-lying vibrational excitations requires to set δ close to the red sideband condition for $v_g = 1$, i.e., $\delta \approx -\omega_g$. Such a laser frequency, however, causes heating of higherlying vibrational states. Consequently, cooling with a fixed frequency would not succeed. This problem can be resolved by using a time-dependent chirp of δ which compensates for the ν_{g} -dependence of the condition to address red sidebands one after the other. Such a frequency chirp then dissipates motional quanta without concurrent heating, since the protocol assures that higher vibrational states are first transferred to lower energy, before states closer to the trap bottom are addressed (see also Ref. [22] for a recent proposal). Note that a fixed laser frequency provides an effective repulsive energy cap in the trap, which was exploited in Ref. [14] to prevent atom loss during imaging and which was interpreted by a classical Sisyphus effect.

Before we turn to the experimental results, we briefly analyze the chirp-cooling approach numerically. To this end, we compute the quantum dynamics of a harmonically confined and laser-coupled (Rabi frequency Ω) two-level atom in 1D including state-dependent trapping. The time evolution is obtained by integrating the Liouville-von Neumann equation for the density matrix with a finite basis set of oscillator levels accounting for decay of the excited state (decay rate γ) via the Lindblad operators (see Appendix E). Results for typical experimental parameters are shown in Fig. 1(b) for a linear (10 ms long) ramp of δ from $\delta_i/\omega_g = -3.7$ to $\delta_f/\omega_g = -1$ and for the atom initially prepared in $|\nu_g = 4\rangle$. The data reveal that chirping allows for efficient transfer into the motional ground state. For the chosen parameters $[(\omega_g, \omega_e, \Omega)]$ $2\pi(150, 110, 20)$ kHz], the final ground-state population is >94%. Cooling occurs due to resonant addressing of various red sidebands during the chirp, coupling states of different motional quantum numbers $v_g > v_e$ [arrows in Figs. 1(a) and 1(b)]. Note that in contrast to magic trapping conditions, where couplings between different oscillator levels with $\Delta \nu =$ $|v_g - v_e| > 1$ are strongly suppressed for tight confinement by the Lamb-Dicke effect, here, they play a vital role in the cooling dynamics due to direct wave-function overlaps $\langle v_g | v_e \rangle$ between levels of equal parity [29]. The simulations also reveal optimal ground-state population when $\delta_f \approx -\omega_g$, i.e., when the laser frequency chirp ends near the resonance condition for driving the first red sideband from $|v_g = 1\rangle$. Note that the simulation parameters for Fig. 1(b) are chosen in a way that the underlying mechanism of the cooling scheme is well visible and are not optimized for highest ground-state transfer.

III. COOLING AND THERMOMETRY

Our experiments start with loading a single optical tweezer with wavelength $\lambda = 539.91$ nm and a waist of 564(5) nm from a 88 Sr magneto-optical trap (MOT) operated on the $^{1}S_{0}$ to ${}^{3}P_{1}$ intercombination line [Fig. 1(c)] (see Appendix A). After loading, the tweezer is typically occupied by more than one atom in the electronic ground state ${}^{1}S_{0}$ (trap depth ≈ 0.5 mK). At the trapping wavelength, the tweezer potential for ${}^{1}S_{0}$ is deeper than for the excited ${}^{3}P_{1}$ state of the cooling transition, i.e., realizing the situation $\alpha_g/\alpha_e > 1$ discussed above. More precisely, we perform all experiments at nominally zero magnetic field and with a linearly polarized tweezer. In that case, the three magnetic substates of the ${}^{3}P_{1}$ level $(m_{J}=0,\pm1)$ are shifted by the AC-Stark interaction with the trap light. We label the AC-Stark-shifted eigenstates $|e_0\rangle$, $|e_-\rangle$, and $|e_+\rangle$. The latter two are energetically degenerate (see Ref. [14] and Appendix C). The wavelength dependence of the ratio α_g/α_e for all three levels is shown in Fig. 1(d). This allows us to perform experiments using two different transitions with vastly different values α_g/α_e (~ 1.13 for $|e_0\rangle$ and ~ 1.90 for $|e_{\pm}\rangle$).

We start investigating the cooling dynamics on the transition to $|e_{\pm}\rangle$, which exhibits the stronger differential light shift, measured to be $U_{\rm diff}^{|e_{\pm}\rangle}/\hbar = 2\pi \times 5.50(5)\,{\rm MHz}$ for the tweezer's optical power of about 1.70(2) mW set throughout this work. The cooling protocol starts by switching on the 689 nm MOT beams with an initial detuning $\delta_i = -2\pi \times 4.1\,{\rm MHz}$. We estimate the Rabi frequency to about $2\pi \times 50\,{\rm kHz}$. The beams are kept on for 100 ms, during which the laser frequency is ramped linearly to a variable final detuning δ_f .

The temperature after the ramp is measured via the releaseand-recapture technique [30]. Briefly, the trap is turned off diabatically for a variable release time t_r before it is suddenly switched on again. We then image the atoms on the ${}^{1}S_{0} - {}^{1}P_{1}$ transition at 461nm by collecting fluorescence photons on a sCMOS camera. From the photon signal on the camera, we deduce the survival probability of a single atom in the trap (see Appendix B and below for more details). Exemplary data of such measurements are shown in Fig. 2(a) for different values of δ_f and compared to data taken without the cooling protocol (circles). A slower decay of the measured survival probability with t_r is indicative for lower temperature, as hotter atoms escape faster from the trap volume. The results reveal a reduction of temperature with decreasing $|\delta_f|$, i.e., when the frequency is chirped closer to the light-shifted resonance at $U_{\text{diff}}^{|e_{\pm}\rangle}/\hbar$.

To extract a classical temperature $T_{\rm cl}$ at the end of the chirp from datasets as shown in Fig. 2(a), we fit classical Monte-Carlo simulations of the release-and-recapture sequence to the data, assuming a thermal energy distribution with mean energy $\bar{E} = k_B T_{\rm cl}$ in each spatial direction (solid lines) [30]. Results of this analysis are plotted in Fig. 2(b) as a function of δ_f (triangles). The data reveal a minimum temperature of 4.17(6) μ K in the vicinity of $\delta_f \approx -\omega_g$. Throughout this work $\omega_g = 2\pi \times 126(5)$ kHz, as measured via sideband spectroscopy (see below). Compared to the data taken without

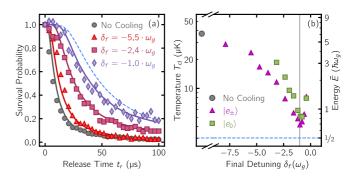


FIG. 2. Thermometry after chirp-cooling via release-andrecapture. (a) Atom-survival probability as a function of the release time t_r is shown for three different values of δ_f as indicated (triangles, squares, diamonds) after cooling on the transition to $|e_{\pm}\rangle$, and compared to a measurement with no cooling applied (circles). Solid lines are fits of a classical particle trajectory simulation to the data to extract the temperature. The blue-dashed line shows the prediction of a quantum mechanical simulation for an atom in the motional ground state (see Appendix D). (b) Temperature $T_{\rm cl}$ extracted from classical trajectory simulations of data as shown in (a) as a function of the detuning δ_f at the end of the frequency chirp. Triangles (squares) are results for cooling on the transition to $|e_{\pm}\rangle$ $(|e_0\rangle)$. The circle denotes the temperature without cooling applied. The vertical line indicates the resonance condition $(\delta_f = -\omega_g)$ for the lowest red sideband $|g, v_g = 1\rangle \rightarrow |e, v_e = 0\rangle$. At this point, the minimal temperature is achieved. The dashed line depicts the temperature-equivalent $T_{\rm gs}$ of the radial zero-point motion energy in the trap. Error bars in all figures show one standard deviation and are mostly smaller than the data points.

cooling, we achieve a reduction in temperature by about one order of magnitude. Chirping further down in $|\delta_f|$ again leads to heating, as the cooling light approaches the resonance condition for driving the carrier transition from the ground state $(\delta=0)$.

The minimal measured temperature is found close to the temperature-equivalent of the zero-point motion energy of the radial tweezer ground state $T_{\rm gs} = \hbar \omega_g/2k_B = 3.04~\mu {\rm K}$ (dashed line), indicating sizeable radial ground-state population. Since the classical analysis does not account for the zero-point motion in the trap, we also analyze the experimental data with the lowest-measured temperature quantum mechanically. As the release-and-recapture method is only weakly dependent on the axial tweezer direction, it is sufficient to model the recapture probability along the radial direction. To this end, we time-evolve the wave functions of the first few states of a 2D harmonic oscillator numerically. After time t_r of free expansion, the Gaussian tweezer potential is added to deduce the probability of recapture (see Appendix D). The result of this analysis for the 2D ground state [dashed line in Fig. 2(a)] is already close to the lowesttemperature experimental data ($\delta_f = -\omega_g$). Next, the analysis is extended to a thermal distribution of the first few 2D harmonic oscillator states. A fit of this model to the data for $\delta_f = -\omega_g$ yields 82(3)% ground-state population along one radial direction. To demonstrate the robustness of the chirp-cooling, we finally repeat the measurements on the transition to $|e_0\rangle$, for which the differential light shift $U_{
m diff}^{|e_0\rangle}/\hbar=$

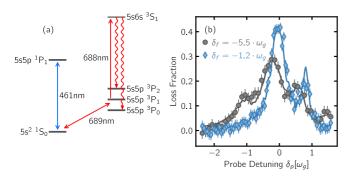


FIG. 3. (a) Scheme for sideband thermometry via shelving into metastable states. The atom in the ground state 1S_0 is excited to the 3P_1 ($|e_0\rangle$) state by a short probe laser pulse. The population transferred to 3P_1 is hidden from the imaging cycle (${}^1S_0 - {}^1P_1$) by optically pumping into the metastable 3P_0 and 3P_2 states via 3S_1 . (b) Measured loss fraction from 1S_0 due to shelving as a function of probe detuning δ_p after cooling on the transition to $|e_\pm\rangle$ to $\delta_f = -1.2\omega_g$ (diamonds) and $\delta_f = -5.5\omega_g$ (circles). Solid lines are numerical simulations fitted to the data to extract the ground-state fraction (see text).

 $2\pi \times 1.30(2)$ MHz is much weaker. We obtain very similar results [squares in Fig. 2(b)] and attribute the slightly higher minimal temperature to the higher sensitivity required for tuning δ_f .

While the above results already provide evidence that the chirp-cooling method yields a large ground-state population, we complement the thermometry by resolved sideband spectroscopy on the ${}^{1}S_{0} - {}^{3}P_{1}$ transition to $|e_{0}\rangle$ along the radial direction of tweezer confinement. For spectroscopy, we apply a short (75 µs) probe pulse with the laser frequency set to the vicinity of the $|e_0\rangle$ resonance and the propagation direction perpendicular to the tweezer axis. Subsequently, the population transferred to $|e_0\rangle$ is rapidly shelved into the metastable states ${}^{3}P_{0}$ and ${}^{3}P_{2}$ [Fig. 3(a)]. The sequence is repeated three times before imaging on the ${}^{1}S_{0}$ - ${}^{1}P_{1}$ transition to increase the signal. Results are shown in Fig. 3(b) close to the lowest temperature achieved when cooling on the transition to $|e_{\pm}\rangle$ (diamonds). Compared to the case of less-deep cooling (circles), we observe strong sideband asymmetry, a hallmark for large ground-state population. Shift and broadening of the line with increasing temperature is due to the differential AC-Stark shift on the probe transition. Note that without cooling, the sidebands are completely unresolved. Such effects are absent in more conventional sideband thermometry, for which narrow optical lines with vanishing differential AC-Stark shifts are used.

Extracting the ground-state population from our data thus requires fitting with a full numerical simulation of the spectroscopy sequence. To this end, we compute the dynamics of the trapped two-level atom density matrix with an initial thermal trap population as above. The population in $|e_0\rangle$ is extracted at the end of the probe pulse and the loss fraction is determined assuming a fitted success probability p_s for shelving. Trap frequencies $\omega_{g,e}$ and the temperature of the initial state are also fit parameters (see Appendix E). Our lowest temperature data (diamonds) is found to be compatible with a ground-state fraction in the range of 73% to 97%, which

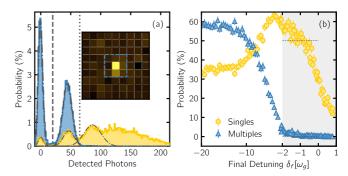


FIG. 4. Light-induced losses and parity projection during cooling. (a) Histograms of photon counts before (yellow) and after (blue) cooling on $|e_{\pm}\rangle$ to $\delta_f=-1.2\omega_g$. The vertical dashed (dotted) line indicates the lower threshold set for identifying N=1 ($N\geqslant 2$) atom(s). Dash-dotted lines are Gaussian fits to the data to guide the eye. The inset shows the fluorescence of a single atom imaged onto at 3x3 pixel array of the sCMOS camera. (b) Probability to detect N=1 (circles) and $N\geqslant 2$ (triangles) atom(s) in the tweezer after chirp-cooling to a final detuning δ_f . The dashed line indicates unity filling with 50% probability. Note the change in scaling of the axis of abscissas for $\delta_f/\omega_g>-2$ (shaded area).

is in agreement with the results extracted from release-and-recapture. This ground-state fraction is also comparable with sideband cooling in magic-wavelength tweezers reported for strontium [14,15].

Finally, we note that our data analysis neglects possible shifts and broadening of the carrier signal due to axial temperature orthogonal to the probe beam direction. Those can be present when probing at nonzero AC-Stark shift due to the dependence of the radial carrier transition frequency on the axial motional state, and allow us to infer also an upper limit estimate for the axial temperature. Indeed, since the observed linewidth is well compatible with our 1D analysis, we conclude that the axial temperature cannot be significantly higher than the measured radial temperature. This provides evidence that cooling acts simultaneously in axial trap direction, revealing additional information that is not accessible from release-and-recapture.

IV. PARITY PROJECTION DURING COOLING

Next, we study the dynamics of the atom number population in the tweezer during cooling. Most importantly, we find that chirp-cooling to low temperatures in the trap also causes light-induced losses which reliably remove pairs of atoms from the trap [31,32]. This can be readily seen from histograms of the detected photon count before and after cooling [Fig. 4(a)]. Without cooling, we observe a multipeak structure in the histogram, where the individual peaks are associated with one, two and more than two atoms in the trap. After cooling, a clean binary distribution with a one and a zero atom peak is observed. We find an approximately equal number of photon counts in the two peaks, i.e., about 50% filling with exactly one atom. In Fig. 4(b), we show how the probabilities for finding one (circles) and more than one (triangles) atom(s) in the trap evolve with the final detuning δ_f of the cooling ramp. Pairs of atoms are continuously lost with decreasing

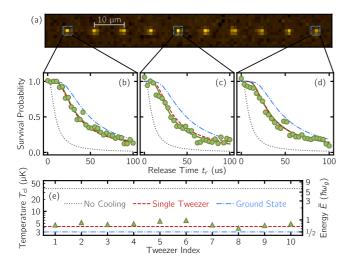


FIG. 5. Chirp-cooling in a one-dimensional tweezer array. (a) Averaged fluorescence image of a line of ten tweezers (10 µm spacing) after cooling chirp (including parity projection). [(b)–(d)] Release-and-recapture thermometry data (cf. Fig. 2) for the three tweezers indicated with boxes after a cooling chirp to $\delta_f = -1.2\omega_g$ on the transition to $|e_{\pm}\rangle$. Solid lines are fits of a classical particle trajectory simulation to extract the temperature $T_{\rm cl}$. The blue dashdotted line shows the prediction of a quantum mechanical simulation for an atom in the motional ground state. The red dashed line (gray dotted line) shows the classical fit to the single-tweezer data of Fig. 2 for the same cooling parameters (with no cooling applied). (e) Temperatures T_{cl} as a function of the tweezer index shown in (a). Again, the red dashed line depicts the single-tweezer result after cooling with the same cooling parameters, and the gray dotted line is the temperature measured in a single tweezer without cooling. The blue dash dotted line depicts the temperature-equivalent T_{gs} of the radial zero-point motion energy in the trap. Error bars show one standard deviation and are mostly smaller than the data points.

temperature and essentially vanish for $|\delta_f| \lesssim 2\omega_g$. Indeed, this is expected as the rate for light-assisted collisions, which arise from coupling to a weakly bound molecular state below the 1S_0 $^{-3}$ P_1 asymptote [14,33], strongly depends on the wavefunction overlap of the initial pair of atoms. Moreover, along with the decreasing multiatom signal, we find an increase in the single-atom probability, providing evidence that initial trap loading with an odd atom number $\geqslant 3$ results in a single atom after cooling. Thus the chirp-cooling directly delivers parity projection, an ideal starting point for a deterministic assembly of large atom arrays [23,24].

V. COOLING IN AN ARRAY OF TWEEZERS

Finally, we demonstrate the possibility to apply our chirp-cooling scheme to an array of multiple tweezers. To this end, we generate a one-dimensional line of ten equally spaced ($\approx 10\,\mu m$) traps [Fig. 5(a)], using an acousto-optical deflector in our optical tweezer path (see Appendix A). The traps are generated by applying ten RF tones to the modulator. We equalize the trap depths to a level of $\approx 2\%$ via tweezer-resolved measurements of light shifts and correction on the individual RF amplitudes. The procedure for tweezer loading and cooling is equivalent to the single-tweezer case.

Exemplary release-and-recapture thermometry data for the two outermost and a central tweezer are shown in Figs. 5(b)– 5(d) when chirp-cooling on the transition to $|e_{\pm}\rangle$ with $\delta_f =$ $-1.2\omega_g$, i.e., close to the minimally achieved temperature obtained in a single tweezer (cf. Fig. 2). As before, the classical temperature $T_{\rm cl}$ is extracted from Monte-Carlo trajectory simulations (solid green lines), which for all ten tweezers fall almost on top of the simulation results of the singletweezer data (red-dashed line), reported above for the same parameters. The extracted values for T_{cl} , shown in Fig. 5(e), lie between $T_{\rm cl} = 3.8(2) \,\mu{\rm K}$ and $T_{\rm cl} = 5.7(2) \,\mu{\rm K}$, close to the single-tweezer result [$T_{cl} = 4.8(5) \,\mu\text{K}$] reported above for the same cooling parameters. The gray-dotted line again indicates the temperature without cooling. The small variations in $T_{\rm cl}$ across the array are attributed to residual differences in the trap depths. Indeed, the absolute value of δ_f required for optimal cooling depends approximately linearly on the trap depth, and in our case needs to be controlled on the percent level ($\hbar\omega_g/U_{\rm diff}\approx 2\%$).

VI. CONCLUSION AND OUTLOOK

In conclusion, we have demonstrated a novel, broadly applicable ground-state cooling method for trapped atoms in optical tweezer arrays, which heavily releases constraints on magic trapping conditions for future experiments. This opens new routes for tweezer-based quantum technologies, requiring trapping wavelengths that have been so far incompatible with efficient in-trap cooling, specifically in view of the rapid developments with alkaline-earth(like) atoms [5,34], i.e., strontium [14,15] or ytterbium [16]. For example, the tweezer wavelength selected in this work provides magic trapping of the two clock states ${}^{3}P_{0}$ and ${}^{3}P_{2}$, which enables new concepts for qubit encoding in a neutral atom quantum computer [18]. The cooling scheme also allows operating at wavelengths that offer additional magic trapping for Rydberg states, which mitigates decoherence and in-fidelity of two-body gates [17], and is also applicable to optical lattice systems [22]. When simultaneously applied during imaging on the narrow intercombination transition, the reported technique may also allow for reaching higher scattering rates, particularly for atom detection in the so far unexplored case of a more strongly trapped ground state [28]. Finally, we expect that applying individually controlled cooling beams along radial and axial direction in a pulsed sequence should allow for reaching the full threedimensional trap ground state, and leave a detailed investigation of the cooling dynamics along the weakly trapped tweezer axis for future work. In that context, it is also interesting to apply optimal control strategies on the frequency-chirped laser pulses to increase the cooling efficiency.

ACKNOWLEDGMENTS

We thank Johannes Zeiher, Jacob Covey, and the QRyd-Demo team for fruitful discussions. We acknowledge funding from the Federal Ministry of Education and Research (BMBF) under the grants CiRQus and QRydDemo, the Carl Zeiss Foundation via IQST, and the Vector Foundation. MSS acknowledges support by ONR Grant No. N00014-20-1-2513. This research was supported in part through the use of

University of Delaware HPC Caviness and DARWIN computing systems.

APPENDIX A: TWEEZER LOADING

Tweezer loading starts with the preparation of a six-beam blue magneto-optical trap (MOT) of ⁸⁸Sr atoms in a glass cell (Japan Cell), operated on the ${}^{1}S_{0} - {}^{1}P_{1}$ ($\lambda = 460.9 \,\mathrm{nm}$) transition. The MOT is loaded from an atomic beam source (AOSense, Inc.) comprising an oven, a Zeeman slower, and a 2D-MOT for transverse cooling. After 30 ms of MOT loading at a detuning of $-2\pi \times 46$ MHz and with a saturation parameter of s = 0.12, we decrease the detuning and saturation parameter to $-2\pi \times 21$ MHz and s = 0.01 within 10 ms to reduce temperature. The atoms are kept in this second stage of the blue MOT for another 50 ms, before they are loaded into a narrow-line red MOT on the ${}^{1}S_{0} - {}^{3}P_{1}$ ($\lambda = 689.5$ nm) intercombination transition. To this end, the magnetic field gradient is ramped from \approx 50 G/cm to \approx 2 G/cm. During the first part of the red MOT, the cooling laser is broadened to a frequency comb with a 5 MHz width and a regular 30 kHz spacing by periodically modulating the RF-frequency applied to an acousto-optical modulator (AOM) to increase the capture volume. The comb is subsequently ramped down to a single frequency with a final detuning of $-2\pi \times 150 \text{ kHz}$ while simultaneously reducing the laser intensity from $s \approx$ 3700 to \approx 45. After another 10 ms hold time, the MOT contains several 10⁴ atoms at an equilibrium temperature of \approx 1.4 μ K. This atom number is found to be well-suited for loading a single tweezer and also multitweezer arrays, so that each site is filled with one or more atoms while also avoiding too many atoms in a single trap. The latter may cause nonpairwise losses, ultimately leading to less than 50% filling after parity projection [28].

For generating tweezers, we employ a frequency-doubled fiber laser system providing 10 W output power at 540 nm (TOPTICA Photonics). We send the trapping light through a 2D acousto-optical deflector (AA Opto-Electronic DTSXY-400) before focusing into the MOT region with a high-NA (0.5) microscope objective (Mitutoyo G Plan Apo 50X) to a waist of 564(5) nm. This allows us to extend the studies of our cooling scheme also to multitweezer arrays (see Fig. 5). To achieve homogeneous loading over an extended array, we increase the MOT volume by a two-step ramp of the laser detuning from $-2\pi \times 150$ kHz to $-2\pi \times 280$ kHz within 25 ms and further to $-2\pi \times 560$ kHz within 15 ms [14]. During the second part of this detuning ramp, the tweezer intensity is ramped up to 0.85 mW for a single tweezer. Subsequently, the MOT beams and the magnetic quadrupole field are turned off, and the tweezer intensity is further ramped to its final value of 1.7 mW, at which we perform our chirp-cooling experiments. Note that we illuminate the atoms with two repumping beams resonant with the ${}^{3}P_{0} - {}^{3}S_{1}$ (679 nm) and ${}^{3}P_{2} - {}^{3}S_{1}$ (707 nm) transitions during the entire MOT and tweezer loading procedure.

APPENDIX B: ATOM IMAGING

For single-atom detection, we induce fluorescence on the ${}^{1}S_{0} - {}^{1}P_{1}$ transition using a separate imaging beam, pulsed

on for 75 ms with $s \approx 1.2 \times 10^{-3}$. Prior to this, the tweezer light intensity is increased to 3.4 mW. Fluorescence photons are collected via the same objective used to focus the optical tweezers and are imaged onto a 3×3 pixel area [compare inset of Fig. 4(a)] of a sCMOS camera (Teledyne KINETIX). The atoms are kept cold during imaging by using the red MOT beams with a fixed detuning of $+2\pi \times 1.2$ MHz from the $^1S_0 - ^3P_1$ free-space resonance, corresponding to a detuning from the trap-shifted transition to $|e_0\rangle$ of about $-2\pi \times 1.4$ MHz.

The images are classified into three categories depending on the number $N_{\rm ph}$ of detected photons: No atom ($N_{\rm ph} \leqslant 20$), single atom (20 < $N_{\rm ph} \le 65$), multiple atoms ($N_{\rm ph} > 65$). We quantify the accuracy of this classification in a similar way as reported in Ref. [14]. Taking consecutive images of the same single atom, we find a probability of p = 92.2(2)%to detect the atom in the second image conditioned on its detection in the first one, similar to the results reported in Refs. [14,15]. This atom loss during imaging also dictates the imaging fidelity. More specifically, realizations where an atom is lost from the trap result in a reduced number of detected photons, which may be below the lower threshold $N_{\rm th}$ set for identifying one atom. An upper bound for the probability of such false negative detection events may be estimated via $1 - \exp(\ln(p)N_{th}/\bar{N})$, where \bar{N} is the mean number of detected photons for one atom [14]. For the imaging parameters used throughout this work, we find a false negative rate of about 3.6(1) %. The false positive rate for identifying a single atom (0.00(2)%) is negligible.

To extract the survival probability in Fig. 2(a) and the loss fraction in Fig. 3(b), a value ζ_c is assigned to each of the imaging classification outcomes: $\zeta_c = 0$ (no atom), $\zeta_c = 1$ (single atom), and $\zeta_c = 2$ for multiple atoms, which is then averaged for each data point. To improve the signal-to-noise ratio of the sideband spectroscopy data in Fig. 3(c), we take two consecutive images. The first one is taken after the shelving spectroscopy pulse. Before taking the second image, we return the shelved population from the long-lived 3P_0 and 3P_2 states back into the imaging cycle by applying the 679-nm and 707-nm repumping lasers. We then postselect on realizations where an atom is detected in the second image.

Finally, we note that the accuracy to distinguish between single and multiple atoms in the trap is much lower than between zero and one atom, since the corresponding signals in the histograms [Fig. 4(a)] strongly overlap. The characterization threshold for multiple atoms is chosen high enough that it does not affect the low-temperature measurements with a clean bimodal distribution, i.e., after successful parity projection.

APPENDIX C: DIFFERENTIAL AC-STARK SHIFTS

In Fig. 1(d), we plot the ratio of the AC polarizabilities (and hence the trap depths) between the 1S_0 electronic ground state and the trap-shifted sublevels $|e_0\rangle$ and $|e_\pm\rangle$ of the 3P_1 excited state. For our case of nominally zero magnetic field and a linearly polarized tweezer, the AC-Stark shift for 3P_1 can be readily expressed in terms of scalar (α_s) and tensor (α_t) polarizabilities (the contribution of the vector polarizability vanishes in the absence of magnetic field and for linear

polarization [14,35]). The polarizability of the ${}^{1}S_{0}$ ground state has only a scalar contribution.

More specifically, we consider the time-independent AC-Stark interaction Hamiltonian with an optical field $\vec{E}(t) = \vec{E}^+ e^{-i\omega t} + \vec{E}^- e^{+i\omega t}$, where $\vec{E}^+ = E_0 \vec{\epsilon}$, $\vec{\epsilon}$ being the polarization vector, and \vec{E}^- the complex conjugate of \vec{E}^+ . Omitting the vector term, the Hamiltonian reads

$$\mathcal{H} = -\alpha_s E_0^2 - \frac{3\alpha_t}{J(2J-1)} \left(\frac{\{\vec{E}^+ \cdot \vec{J}, \vec{E}^- \cdot \vec{J}\}}{2} - \frac{J(J+1)E_0^2}{3} \right). \tag{C1}$$

Here, $\vec{J} = (J_x, J_y, J_z)$ denotes the total angular momentum operator and J the associated angular momentum quantum number. In the absence of an external magnetic field, it is convenient to define the quantization axis along the tweezer polarization, which we set (without loss of generality) along the x direction. Accordingly, we label the bare Zeeman substates of the 3P_1 level as $|m_J=0,\pm 1\rangle$, where m_J is the magnetic quantum number associated with the projection of the total angular momentum along the tweezer polarization. The AC-Stark Hamiltonian then reduces to

$$\mathcal{H}_{\text{lin}} = -E_0^2 \left(\alpha_s + \alpha_t \frac{3J_x^2 - J(J+1)}{2(2J-1)} \right). \tag{C2}$$

Since the Hamiltonian above is diagonal in the $|m_J = 0, \pm 1\rangle$ basis defined along the *x* direction, the total polarizability reads [14]

$$\alpha = \alpha_s + \alpha_t \frac{3m_J^2 - J(J+1)}{J(2J-1)}.$$
 (C3)

For J=1 (3P_1) one finds $\alpha=\alpha_s-2\alpha_t$ for $|e_0\rangle=|m_J=0\rangle$ and $\alpha=\alpha_s+\alpha_t$ for $|e_\pm\rangle=|m_J=\pm 1\rangle$. Wavelength-dependent values for α_s and α_t are obtained from numerical calculations as follows.

We evaluated the dynamic polarizabilities by solving the inhomogeneous equation in valence space [36] using the Dalgarno-Lewis [37] approach. This approach allows to account for both discrete states and the continuum. We find intermediate-state wave functions $\delta\psi_{\pm}$ from an inhomogeneous equation,

$$|\delta\psi_{\pm}\rangle = \frac{1}{H_{\text{eff}} - E_0 \pm \omega} \sum_{k} |\Psi_k\rangle\langle\Psi_k|D|\Psi_0\rangle$$
$$= \frac{1}{H_{\text{eff}} - E_0 \pm \omega} D|\Psi_0\rangle, \tag{C4}$$

where D is the z-component of the effective electric dipole operator \mathbf{D} , Ψ_0 is the wave function, and E_0 is the energy of the state of interest, either 1S_0 or 3P_1 in the present work.

The wave functions are computed using the relativistic high-precision hybrid method that combines configuration interaction and coupled-cluster approaches (CI+all order) [38,39]. In this method, the energies and wave functions are determined from the time-independent multiparticle Schrödinger equation

$$H_{\text{eff}}(E_k)\Psi_k = E_k\Psi_k,$$
 (C5)

where the effective Hamiltonian H_{eff} includes contributions of the core states constructed using the coupled-cluster method.

The polarizability is given by

$$\alpha_{\nu}(\omega) = \langle \Psi_0 | D_0 | \delta \psi_+ \rangle + \langle \Psi_0 | D_0 | \delta \psi_- \rangle, \tag{C6}$$

where v indicates that this method gives the valence contribution to the polarizability. The small core polarizability contribution is computed in the random-phase approximation. One of the challenges of the accurate polarizability computation for the 3P_1 state in the region below 600 nm is strong sensitivity to the accuracy of the energy levels. To resolve this problem, we developed a code to automatically replace the theoretical energy values for low-lying dominant contributions by exact experimental values as well as use improved recommended values of the reduced matrix element where available. The substitution is done for all data points using the sum-over-states formula

$$\alpha_v(\omega) = 2 \sum_k \frac{(E_k - E_0)|\langle \Psi_0 | D_0 | \Psi_k \rangle|^2}{(E_k - E_0)^2 - \omega^2},$$
 (C7)

improving the polarizability accuracy. The uncertainties are estimated for all polarizability values.

APPENDIX D: CLASSICAL AND QUANTUM MECHANICAL RELEASE-AND-RECAPTURE ANALYSIS

In this section, we provide details on the classical and quantum mechanical analysis of the release-and-recapture data shown in Fig. 2. Our classical analysis follows the procedure described in Ref. [30]. Specifically, we draw a Monte Carlo sample of spatial and velocity vectors from a thermal distribution of point particles in a 3D harmonic trap using our experimental parameters. For a given classical temperature $T_{\rm cl}$, the three spatial coordinates are Gauss-distributed with a standard deviation of $\sigma_i = \sqrt{k_B T_{\rm cl}/m\omega_i^2}$, where m is the mass of the ⁸⁸Sr atom, and ω_i the oscillator trap frequency in direction i = (x, y, z). The Gaussian velocity distribution in each direction has a standard deviation of $\sigma_v = \sqrt{k_B T_{\rm cl}/m}$. A simulated release-and-recapture trace is obtained by propagating this ensemble in free-space for a variable time t_r . The survival probability is then computed by evaluating the fraction of the ensemble that is trapped after instantaneous switch-on of the Gaussian tweezer potential. A particle is considered to be trapped, when its kinetic energy is smaller than the local (absolute) potential energy after the free propagation. Such simulated traces are then fit to the data via a chi-squared analysis with $T_{\rm cl}$ as fit parameter.

This analysis does not capture the zero-point motion energy of the trapped atom, and the fitted classical temperature $T_{\rm cl}$ overestimates the true quantum mechanical temperature. Effects of quantized motion in the trap are taken into account by our quantum mechanical analysis of the lowest energy data in Fig. 2(a). To this end, it is sufficient to consider only the radial dynamics, since the release-and-recapture technique is only weakly dependent on the longitudinal motion. First, we compute the free expansion of initial 2D harmonic oscillator wave functions with occupation numbers (ν_x, ν_y) , where x and y denote the cartesian coordinates of the radial tweezer direction. After a variable time t_r , the Gaussian tweezer potential is turned on instantaneously and the wave function is

evolved inside the potential for another 100 μ s. The fraction of the wave function that has remained inside the potential then yields the survival probability $p_{(\nu_x,\nu_y)}$. Assuming a thermal population of the 2D harmonic oscillator levels, the survival probability $p_{\rm qm}$ for an ensemble at a quantum mechanical temperature $T_{\rm qm}$ is finally obtained by weighting $p_{(\nu_x,\nu_y)}$ with the corresponding Boltzmann factor,

$$p_{\rm qm} = \frac{1}{Z} p_{(\nu_x, \nu_y)} e^{-\hbar \omega_{(x,y)}(\nu_x + \nu_y + 1)/(k_B T_{\rm qm})}.$$
 (D1)

Here, $\omega_{(x,y)}$ denotes the radial trap frequency and Z the partition function of the 2D harmonic oscillator. We fit the simulated $p_{\rm qm}$ to the data with $T_{\rm qm}$ as fit parameter. Finally, the fitted value for $T_{\rm qm}$ yields the ground-state population along one radial direction stated in the main paper.

APPENDIX E: NUMERICAL MODELING OF CHIRP-COOLING AND SIDEBAND SPECTROSCOPY DATA

In this section, we provide details of our method for describing the chirp-cooling and for modeling the sideband spectroscopy data. Our method is similar to the approach taken in Refs. [22,29]. To reduce the computational costs of our simulations, we neglect coupling between different spatial directions and restrict ourselves to one radial direction of the three-dimensional trap. Under this approximation, the system can be described as a driven two-level atom in a one-dimensional harmonic trap. The electronic ground state $|g\rangle$ is trapped with the frequency ω_g and the excited state $|e\rangle$ with ω_e . We use the levels of the harmonic oscillator with the frequency ω_q as a basis for the motional state of the atom. For our simulations, we take the 30 lowest oscillator levels into account. Using the creation and annihilation operators a^{\dagger} and a that act on these levels, the Hamiltonian of the system reads [29,40]

$$H = \hbar \omega_g \left(a^{\dagger} a + \frac{1}{2} \right) + H_{\text{atom}}(t) + H_{\text{int}}. \tag{E1}$$

To derive the electronic Hamiltonian $H_{\text{atom}}(t)$ of the laserdriven atom, we change into the rotating frame of the laser. Using the rotating wave approximation, we obtain

$$H_{\text{atom}}(t) = \frac{\hbar\Omega}{2} e^{i\eta(a^{\dagger} + a)} |e\rangle\langle g| + \frac{\hbar\Omega^*}{2} e^{-i\eta(a^{\dagger} + a)} |g\rangle\langle e| - \hbar\delta(t)|e\rangle\langle e|, \tag{E2}$$

with the time-dependent detuning $\delta(t)$, Rabi frequency Ω , Lamb-Dicke parameter $\eta = kx_0 = \frac{2\pi}{\lambda} \sqrt{\frac{\hbar}{2m\omega}}$, wavelength $\lambda = 689$ nm, and m being the mass of the 88 Sr atom.

The interaction $H_{\rm int}$ between the electronic and motional states of the atom emerges from the trap frequency being state-dependent and is given by

$$H_{\rm int} = \frac{\hbar \left(\omega_e^2 - \omega_g^2\right)}{4\omega_g} (a + a^{\dagger})^2 |e\rangle\langle e| + U|e\rangle\langle e|, \qquad (E3)$$

where U is chosen such that the transition from $|g\rangle$ to $|e\rangle$ is driven resonantly for $\delta(t)=0$ if the atom is in its motional ground state.

To incorporate the decay of the excited state with rate $\gamma = 2\pi \times 7.4$ kHz, we describe the system with a Lindblad

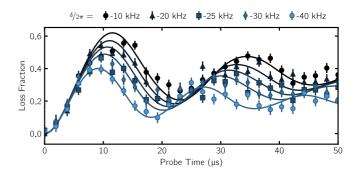


FIG. 6. Measurement of the probe Rabi frequency Ω used for sideband spectroscopy. Measured loss fraction from 1S_0 due to shelving as a function of probe time for different detunings from the carrier transition, i.e., $\nu_e = \nu_g$, to $|e_0\rangle$. Solid lines show numerical simulations fit to the data, which yield $\Omega = 2\pi \times 44.9(5)\,\text{kHz}$.

master equation, $\dot{\rho}=-i(H_{\rm eff}\rho-\rho H_{\rm eff})+\mathcal{L}\rho$. The decay enters the non-Hermitian Hamiltonian $H_{\rm eff}=H-\frac{i\hbar\gamma}{2}|e\rangle\langle e|$ and the term

$$\mathcal{L}\rho = \frac{\hbar \gamma}{2} \int_0^{\pi} e^{-i\eta(a^{\dagger} + a)\cos\theta} |g\rangle\langle e|\rho|e\rangle\langle g|$$

$$\times e^{i\eta(a^{\dagger} + a)\cos\theta} \sin\theta \ d\theta. \tag{E4}$$

This term accounts for the population returning into the ground state and for the recoil of the emitted photon projected onto the direction of the trap.

To illustrate the chirp-cooling approach [Fig. 1(b)], we apply a Rabi frequency of $\Omega = 2\pi \times 20\,\mathrm{kHz}$ and a time-dependent detuning $\delta(t)$ that is ramped linearly from $-3.7\,\omega_g$ to $-1\,\omega_g$ within 10 ms. The trap frequencies are set to $\omega_g = 2\pi \times 150\,\mathrm{kHz}$ and $\omega_e = 2\pi \times 110\,\mathrm{kHz}$. To demonstrate the cooling mechanism, we use the motionally excited state $|g,4\rangle$ as the initial state. The resulting Lindblad master equation is solved using QuTiP [41].

For modeling the sideband spectroscopy data, we extend our model by introducing an effective dark state. The sideband spectroscopy is a two-step process. First, we apply a probe pulse with Rabi frequency Ω and detuning δ for 75 µs. Second, we transfer the resulting population in $|e\rangle$ to the dark state with a success probability p_s . The probe pulse is again simulated using OuTiP, using a thermal density matrix with temperature T as initial state. In the experiment, the shelving signal is increased by repeating the spectroscopy sequence three times before imaging. To account for this in our simulation, we also compute the pulse sequence three times, and take the populations of oscillator states after each pulse (with the atom measured in $|g\rangle$) as the initial condition for the next pulse. In doing so, we include the influence of the probe pulse on the population of motional states, which is experimentally relevant since the lifetime of $|e\rangle$ (1/ γ = 21.5 µs) is comparable to the probe pulse length. Repeating this procedure for various values of δ yields the simulated sideband spectra. Finally, we fit the simulation results to the experimentally measured data with free parameters T, ω_g , and p_s . The Rabi frequency $\Omega = 2\pi \times 44.9(5)$ kHz is measured independently (see Fig. 6 and text below), and the excited state trap frequency ω_e is computed from the calculated polarizability ratio of the transition to $|e_0\rangle$. The fit yields $\omega_g = 2\pi \times 126(5)\,\mathrm{kHz}$, i.e., the trap frequency stated in the main paper and $p_s = 0.33$. The range of ground-state fraction reported in the main text reflects the set of simulated sideband spectra when varying T that are compatible with the data within the experimental error bars.

Finally, we discuss briefly the independent measurement of Ω , for which we apply our sideband spectroscopy sequence as before but now vary the length of the probe pulses. Measured shelving data as a function of probe time exhibits damped Rabi oscillations (see Fig. 6). To extract Ω , we fit the data with the same numerical simulations as described above, but now vary the time of the probe pulses for different values of δ .

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