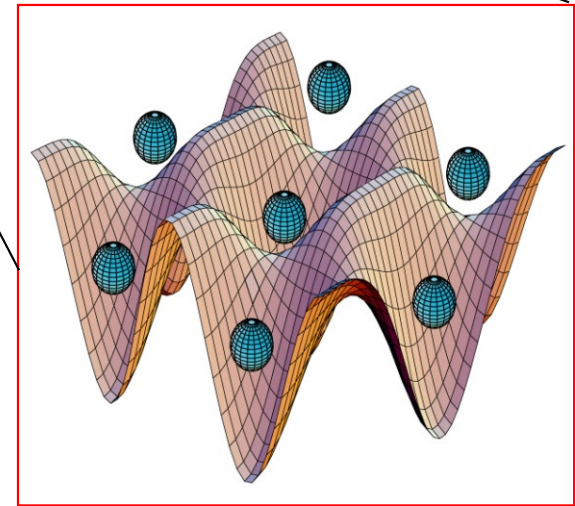
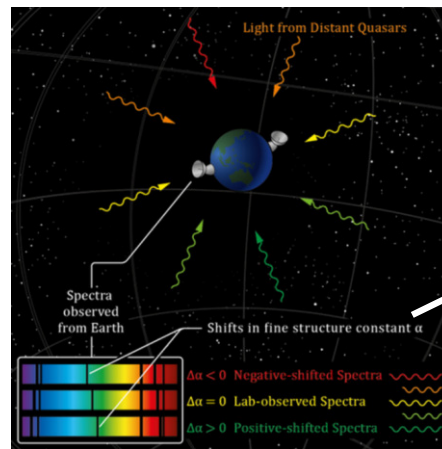
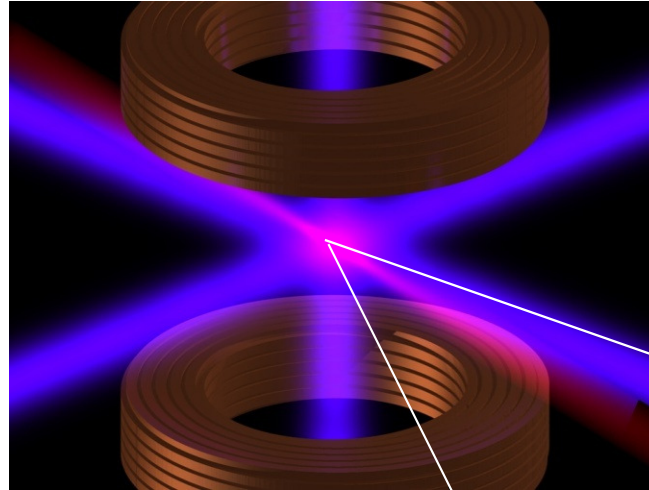
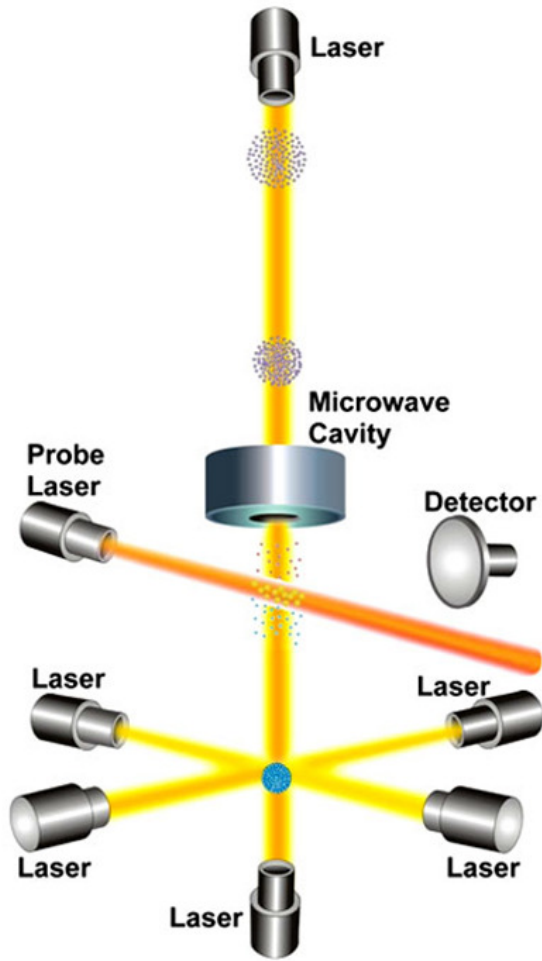
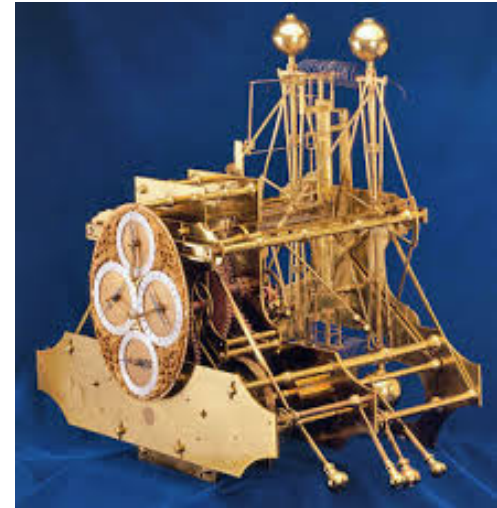


# Atomic clocks

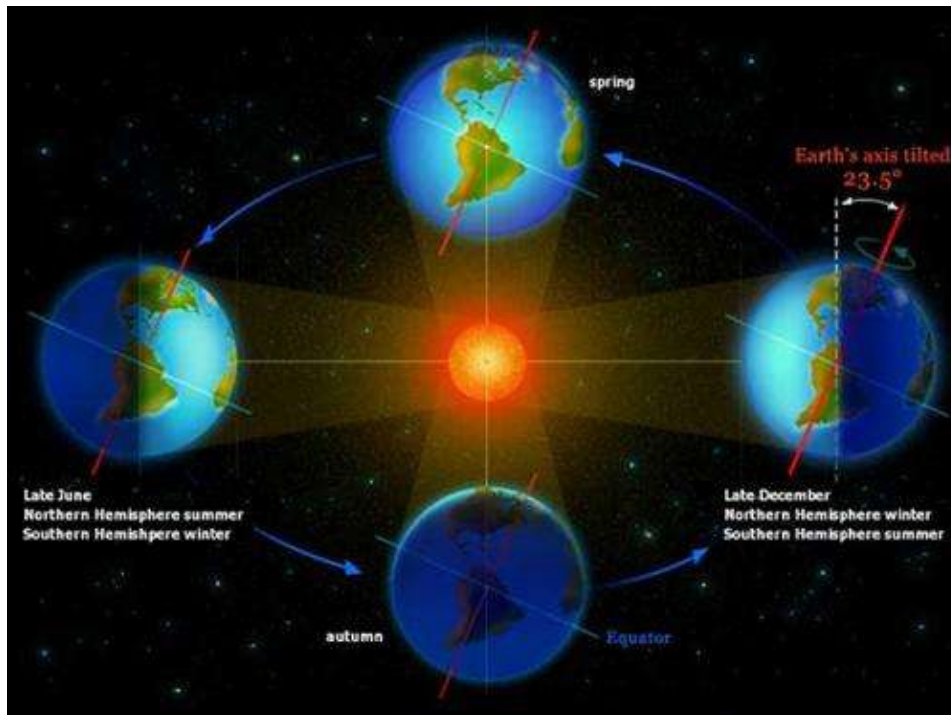


# Clocks



# Ingredients for a clock

1. Need a system with **periodic behavior**:  
it cycles occur at constant frequency

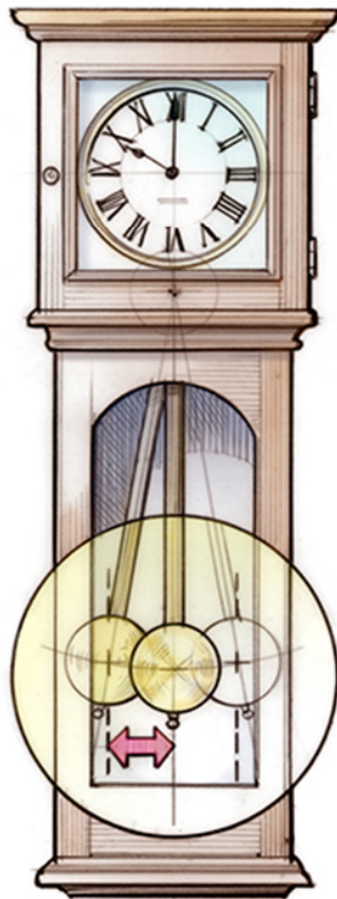


2. Count the cycles to produce time interval
3. Agree on the origin of time to generate a time scale

# QUARTZ CLOCK

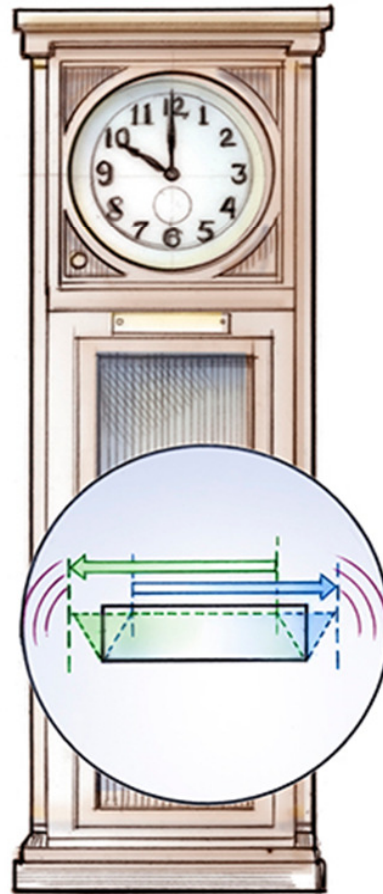
The quartz clock keeps better time than the best mechanical clocks. It contains a specially cut quartz crystal that vibrates at a particular frequency when voltage is applied. The vibrations can be sustained in an electrical circuit and will generate a signal of constant frequency that can be used to keep time.

PENDULUM CLOCK



$1/2$  SWING  
Per SECOND

QUARTZ CLOCK

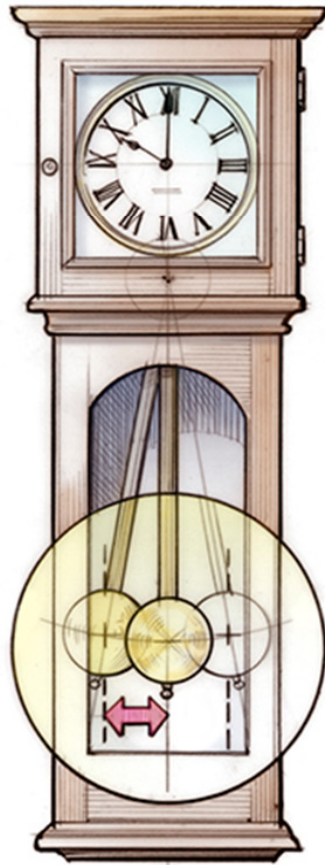


50,000 VIBRATIONS  
Per SECOND

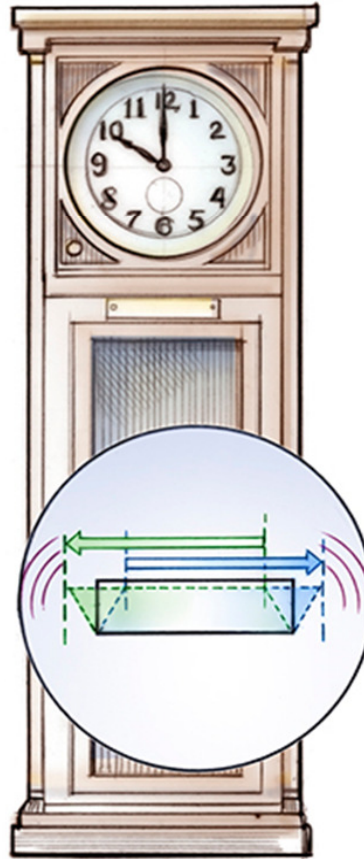
# QUARTZ CLOCK

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PENDULUM CLOCK      QUARTZ CLOCK

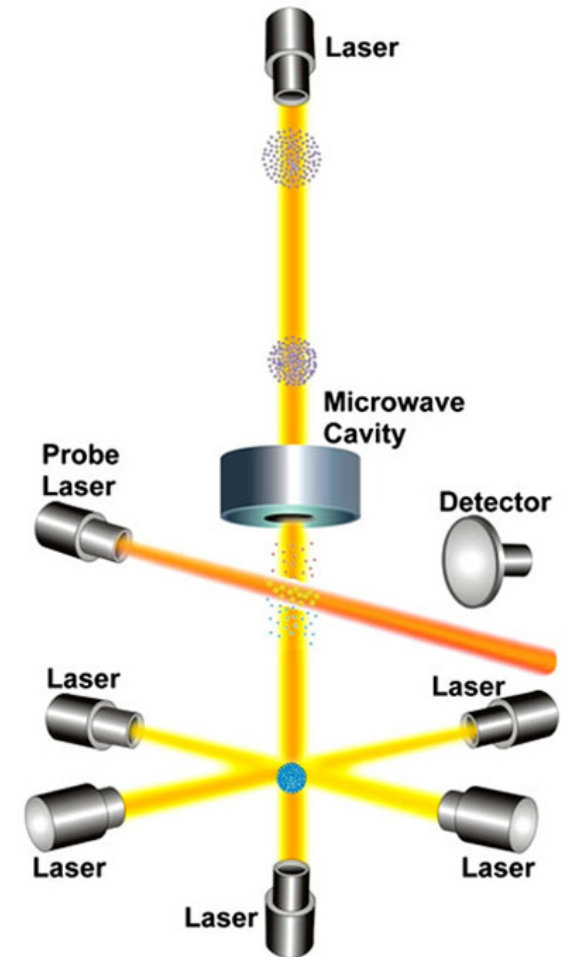


*1/2 SWING  
Per SECOND*



*50,000 VIBRATIONS  
Per SECOND*

## Cesium microwave atomic clock

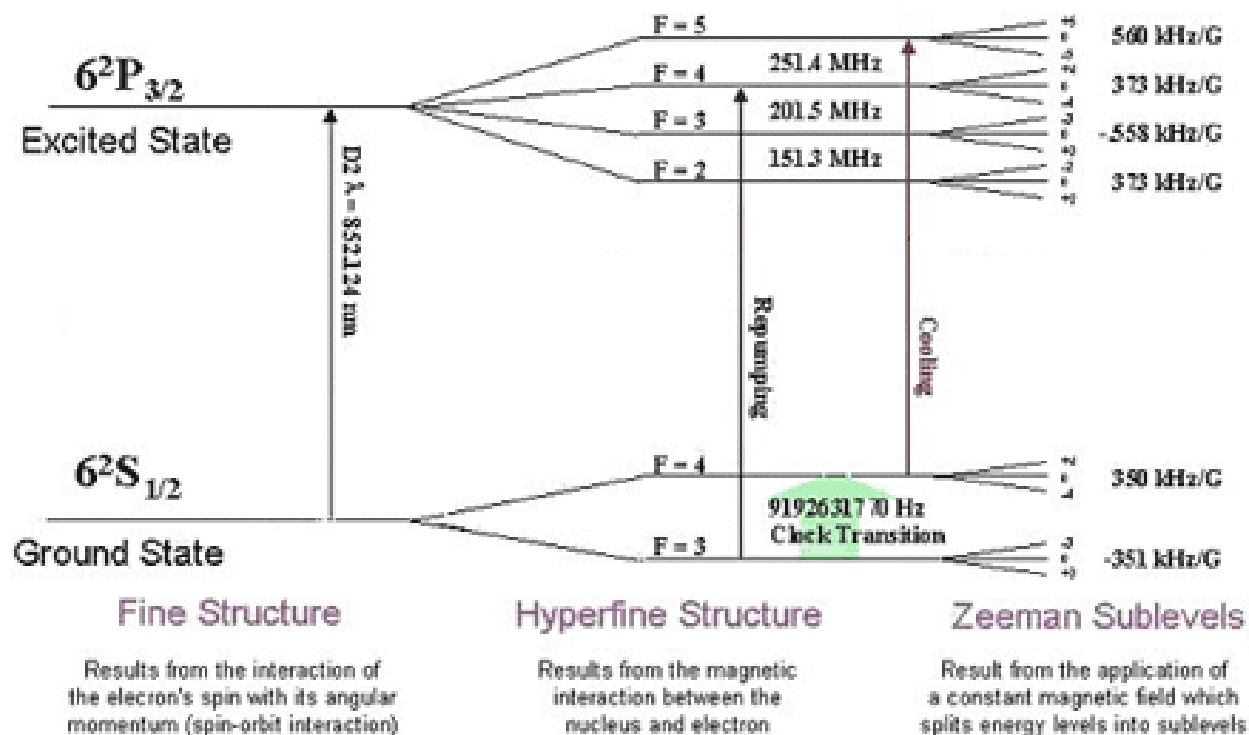


9 192 631 770 periods  
per second

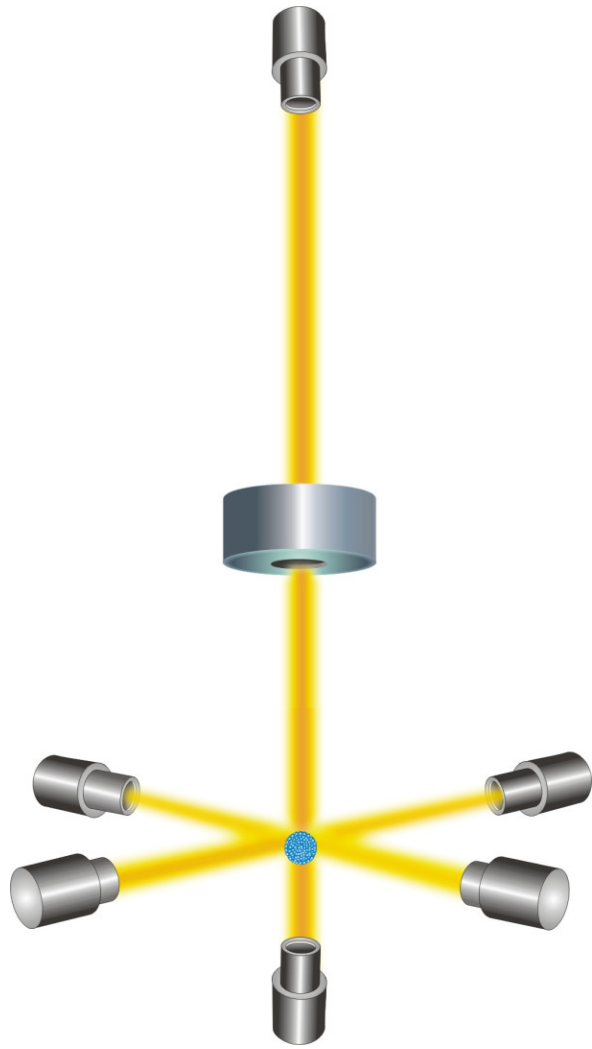
## Current definition of a second:

1967: the second has been defined as the duration of 9 192 631 770 periods of the radiation corresponding to the transition between the two hyperfine levels of the ground state of the cesium 133 atom.

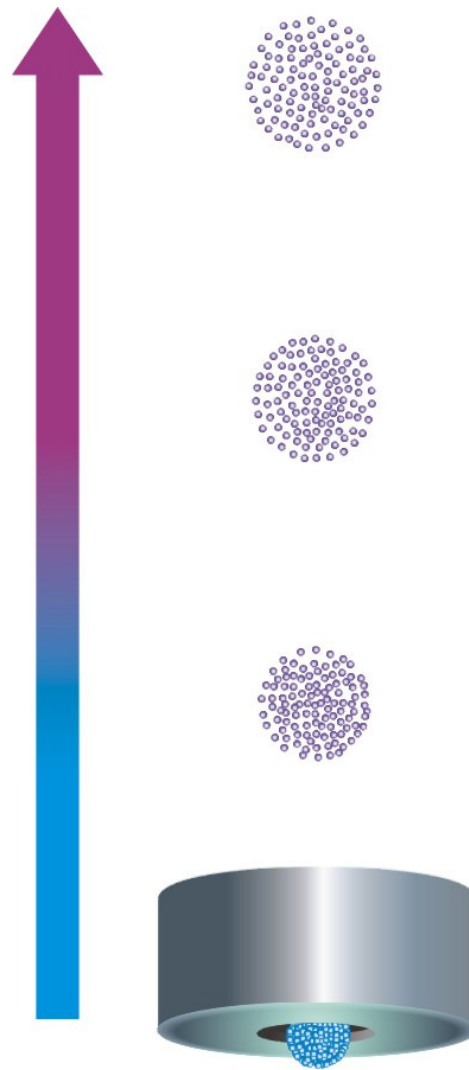
1997: the periods would be defined for a cesium atom at rest, and approaching the theoretical temperature of absolute zero (0 K).



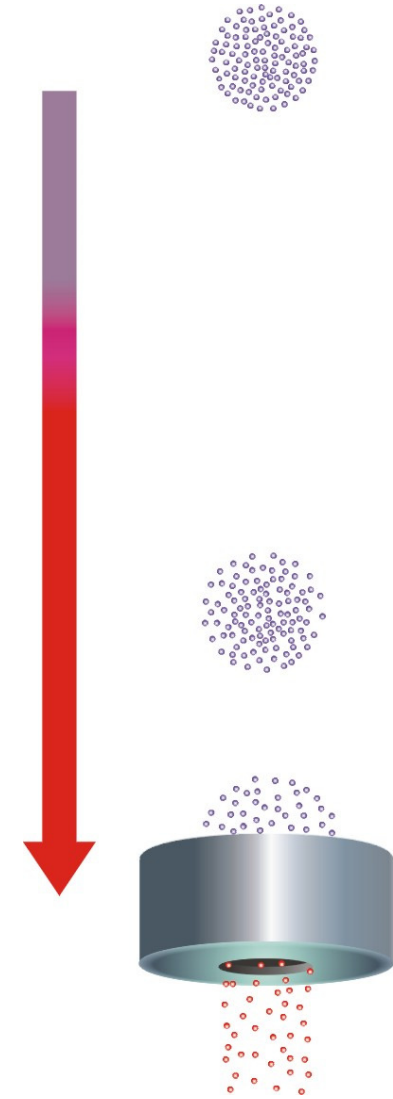
# Cesium atomic clock



A gas of cesium atoms enters the clock's vacuum chamber. Six lasers slow the movement of the atoms, cooling them to near absolute zero and force them into a spherical cloud at the intersection of the laser beams.

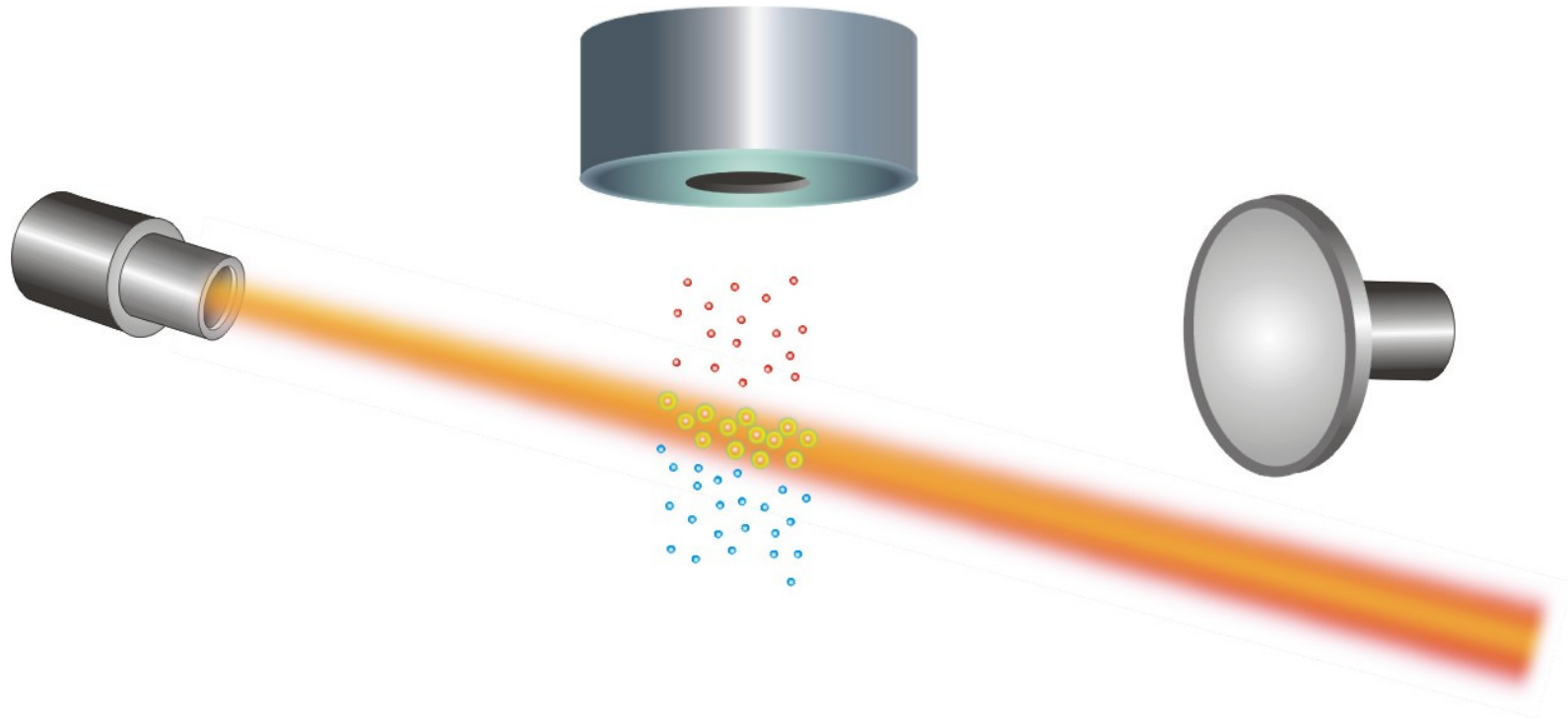


The ball is tossed upward by two lasers through a cavity filled with microwaves. All of the lasers are then turned off.



Gravity pulls the ball of cesium atoms back through the microwave cavity. The microwaves partially alter the atomic states of the cesium atoms.

# Cesium atomic clock



Cesium atoms that were altered in the microwave cavity emit light when hit with a laser beam.

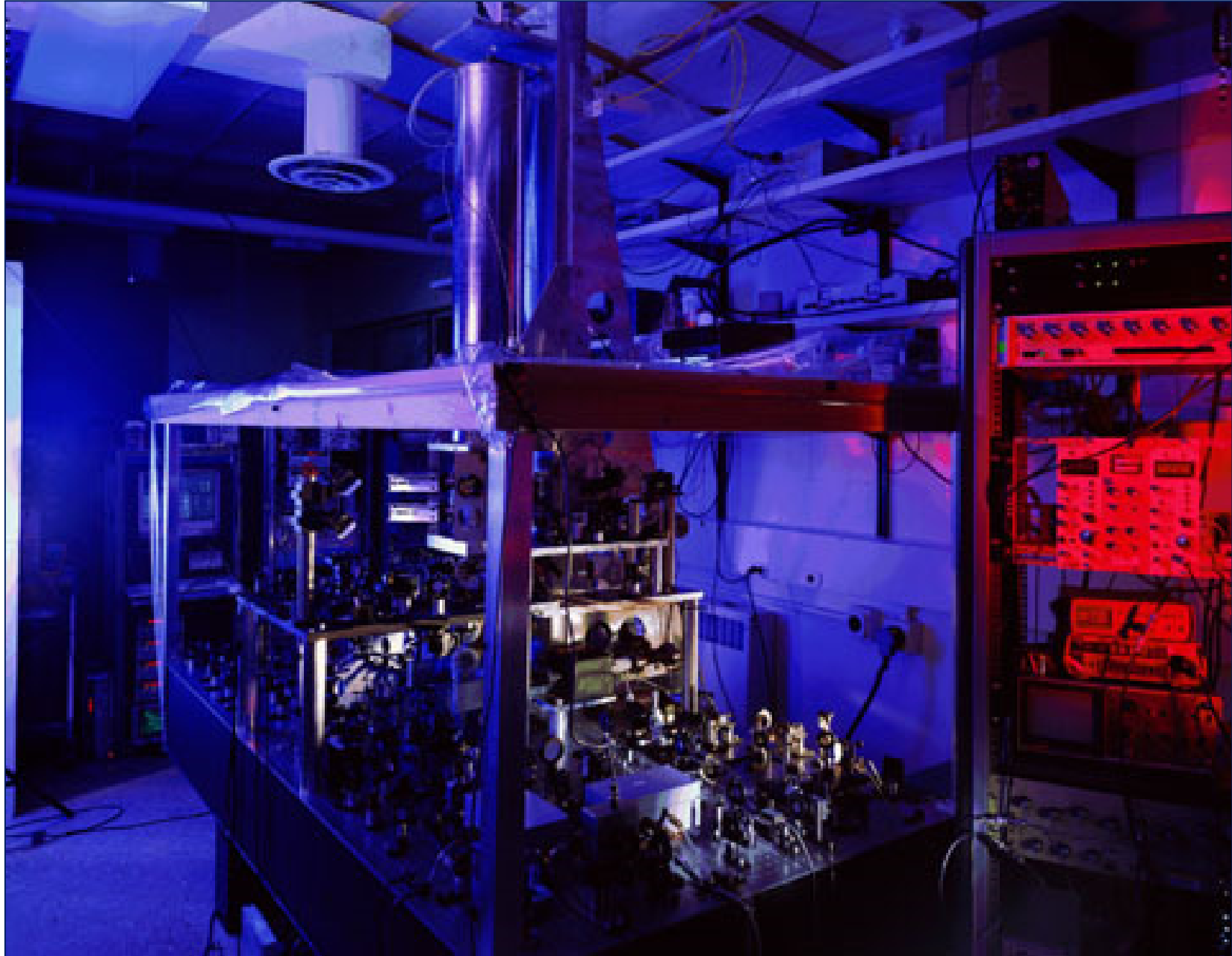
This fluorescence is measured by a detector (right).

The entire process is repeated many times while the microwave energy in the cavity is tuned to different frequencies until the maximum fluorescence of the cesium atoms is determined.

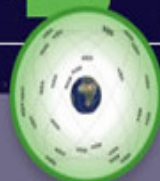
This point defines the natural resonance frequency of cesium, which is used to define the second.



# NIST Cs clock



# HOW GPS WORKS



## GPS

IS A CONSTELLATION OF 24 OR MORE SATELLITES FLYING 20,350 KM ABOVE THE SURFACE OF THE EARTH. EACH ONE CIRCLES THE PLANET TWICE A DAY IN ONE OF SIX ORBITS TO PROVIDE CONTINUOUS, WORLDWIDE COVERAGE.

{ $t_1$ }

1 GPS satellites broadcast radio signals providing their locations, status, and precise time { $t_1$ } from on-board atomic clocks.

{ $c$ }

2 The GPS radio signals travel through space at the speed of light { $c$ }, more than 299,792 km/second.

{ $t_2$ }

3 A GPS device receives the radio signals, noting their exact time of arrival { $t_2$ }, and uses these to calculate its distance from each satellite in view.

To calculate its distance from a satellite, a GPS device applies this formula to the satellite's signal:

**distance = rate x time**

where **rate** is { $c$ } and **time** is how long the signal traveled through space.

The signal's travel **time** is the difference between the time broadcast by the satellite { $t_1$ } and the time the signal is received { $t_2$ }.

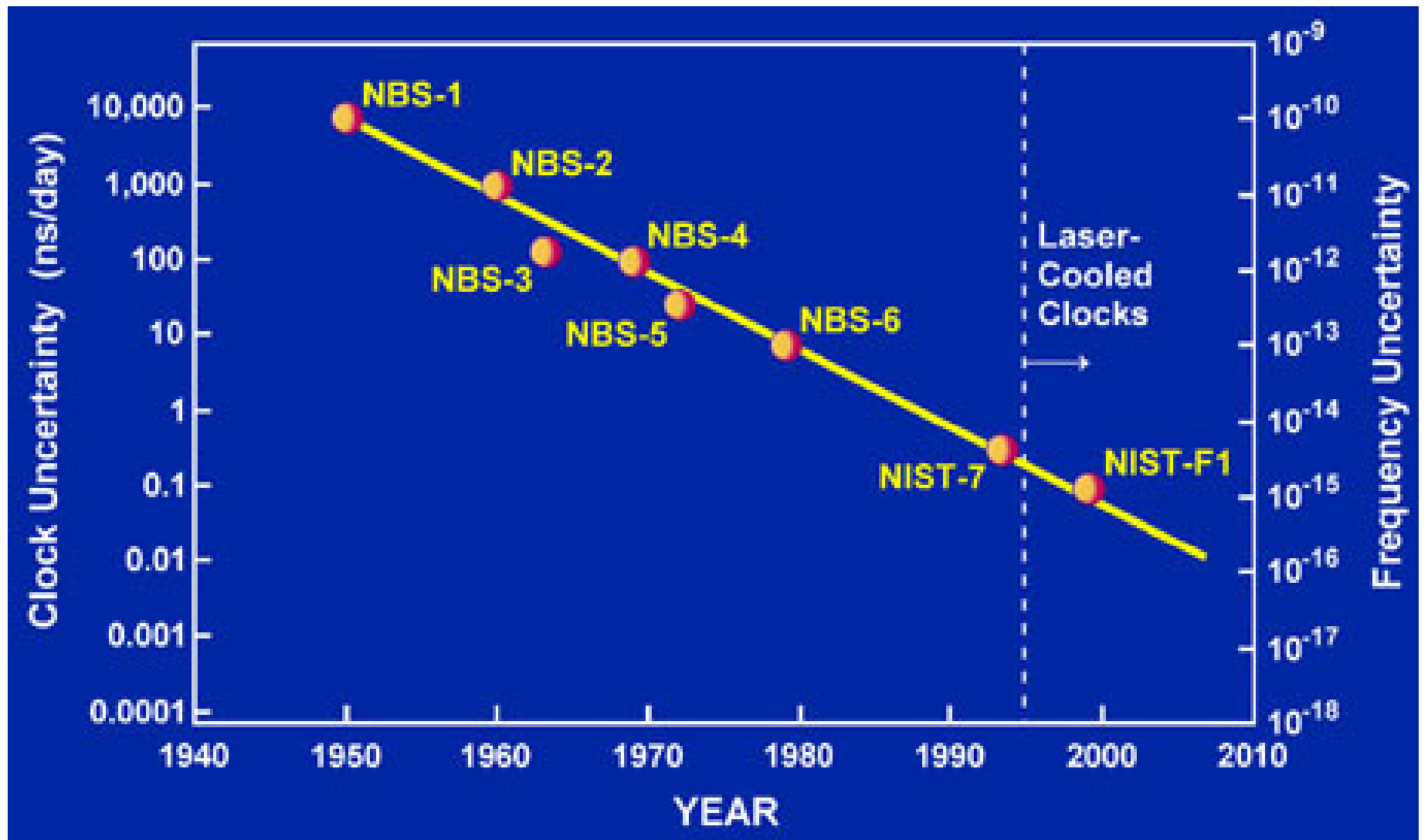
4 Once a GPS device knows its distance from at least four satellites, it can use geometry to determine its location on Earth in three dimensions.

The GPS Master Control Station tracks the satellites via a global monitoring network and manages their health on a daily basis.

Ground antennas around the world send data updates and operational commands to the satellites.

The Air Force launches new satellites to replace aging ones when needed. The new satellites offer upgraded accuracy and reliability.

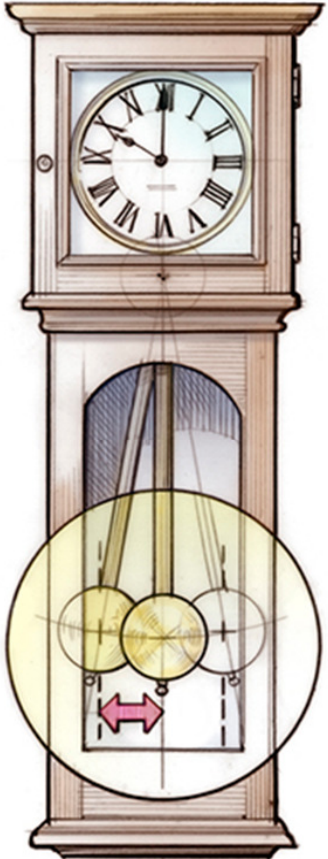
How does GPS help farmers? Learn more about the Global Positioning System and its many applications at



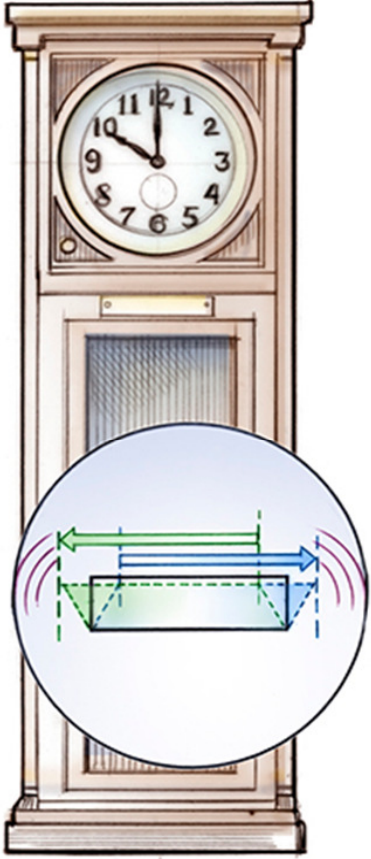
# How to build a better clock?

*PENDULUM CLOCK*

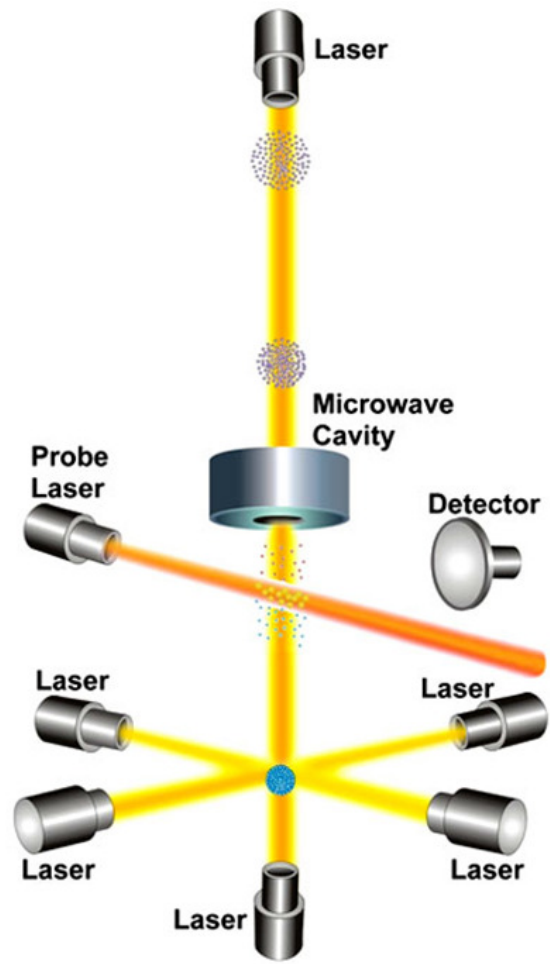
*QUARTZ CLOCK*



*1/2 SWING  
Per SECOND*



*50,000 VIBRATIONS  
Per SECOND*

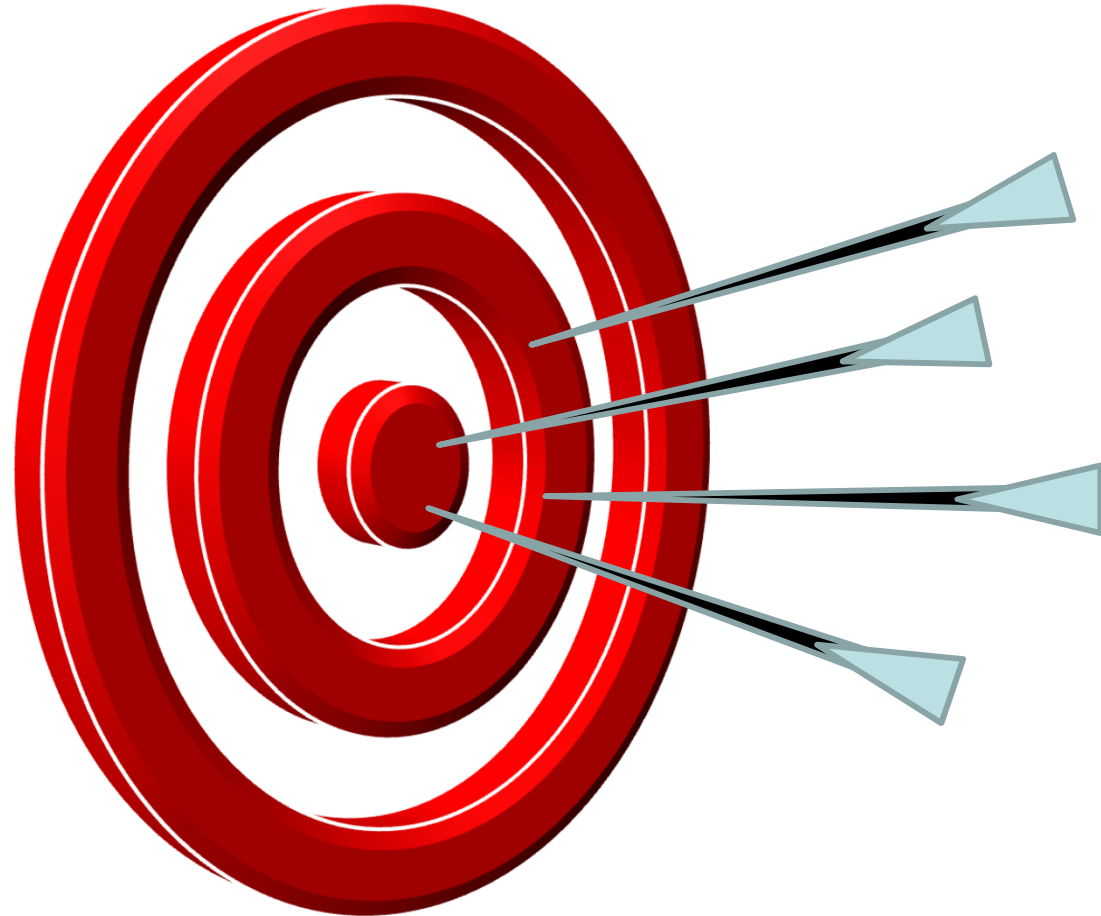


9 192 631 770 periods  
per second

# How good is a clock: stability

**Stability** is a measure of the precision with which we can measure a quantity.

It is a function of averaging time since for many noise processes the precision increases (i.e., the noise is reduced through averaging) with more measurements.



# How good is a clock: uncertainty

In contrast, the (absolute) **uncertainty** for an atomic clock tells us how well we understand the physical processes that can shift the measured frequency from its unperturbed ("bare"), natural atomic frequency.

Requires extensive evaluation of all known physical shifts (usually called "systematic effects").



# Clock instability

Let us first consider the formula for clock instability,  $\sigma_y$ , in the regime where it is limited by fundamental (as opposed to technical) noise sources, such as atomic statistics based on the number of atoms:

spectroscopic linewidth of the clock system

$$\sigma_y(\tau) \approx \frac{\Delta\nu}{\nu_0 \sqrt{N}} \sqrt{\frac{T_c}{\tau}}$$

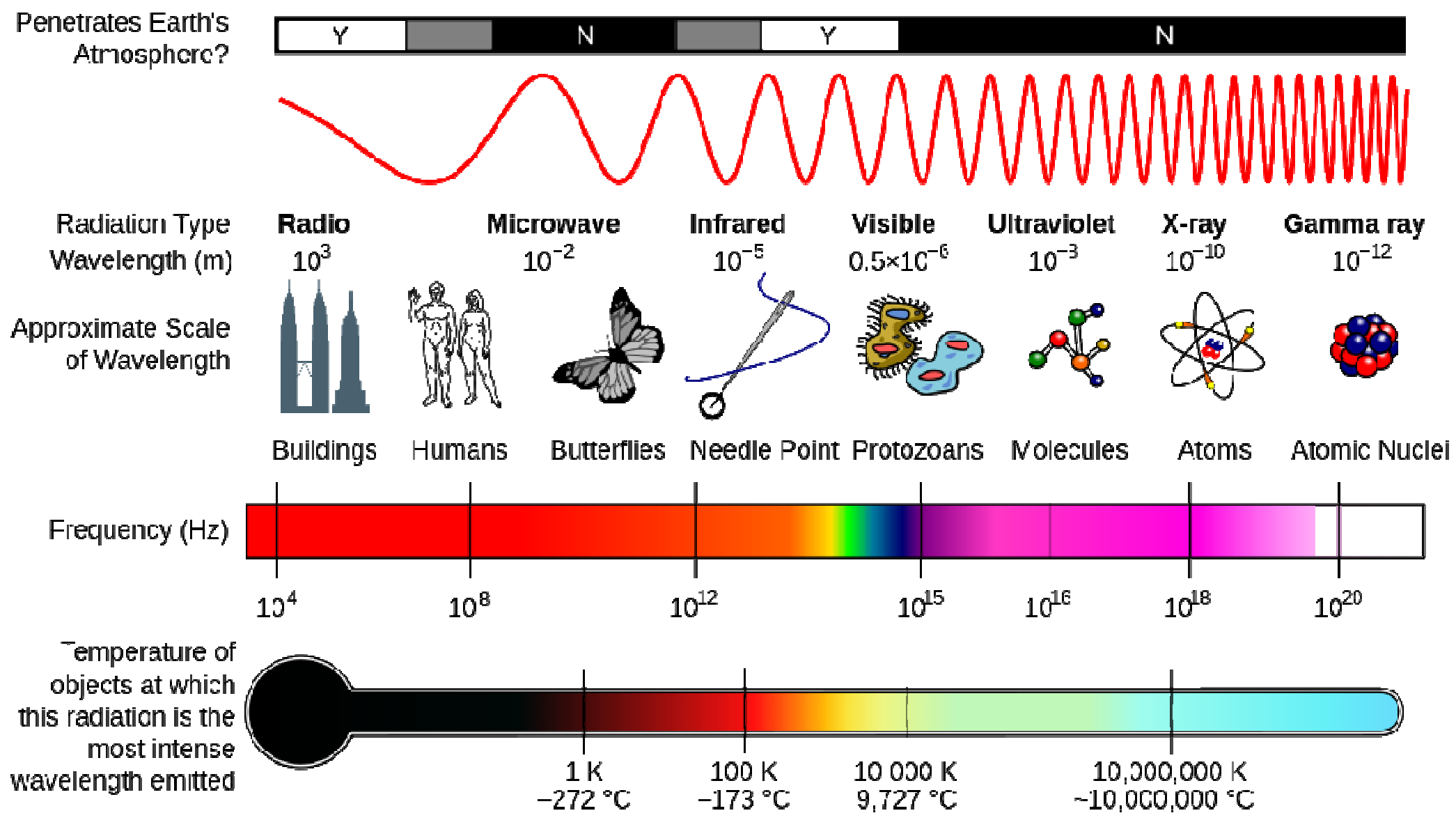
clock transition frequency

the time required for a single measurement cycle

the averaging period

the number of atoms or ions used in a single measurement

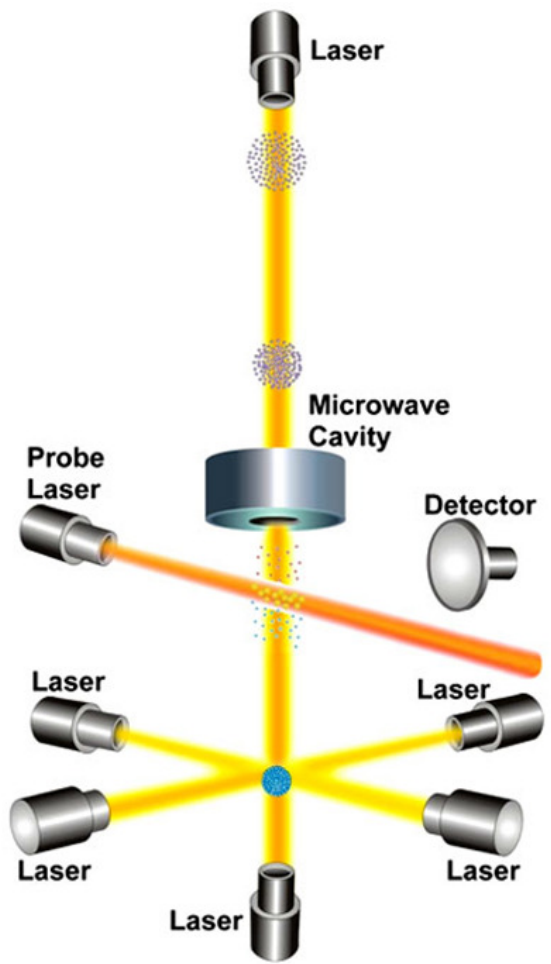
# How to build a better clock?





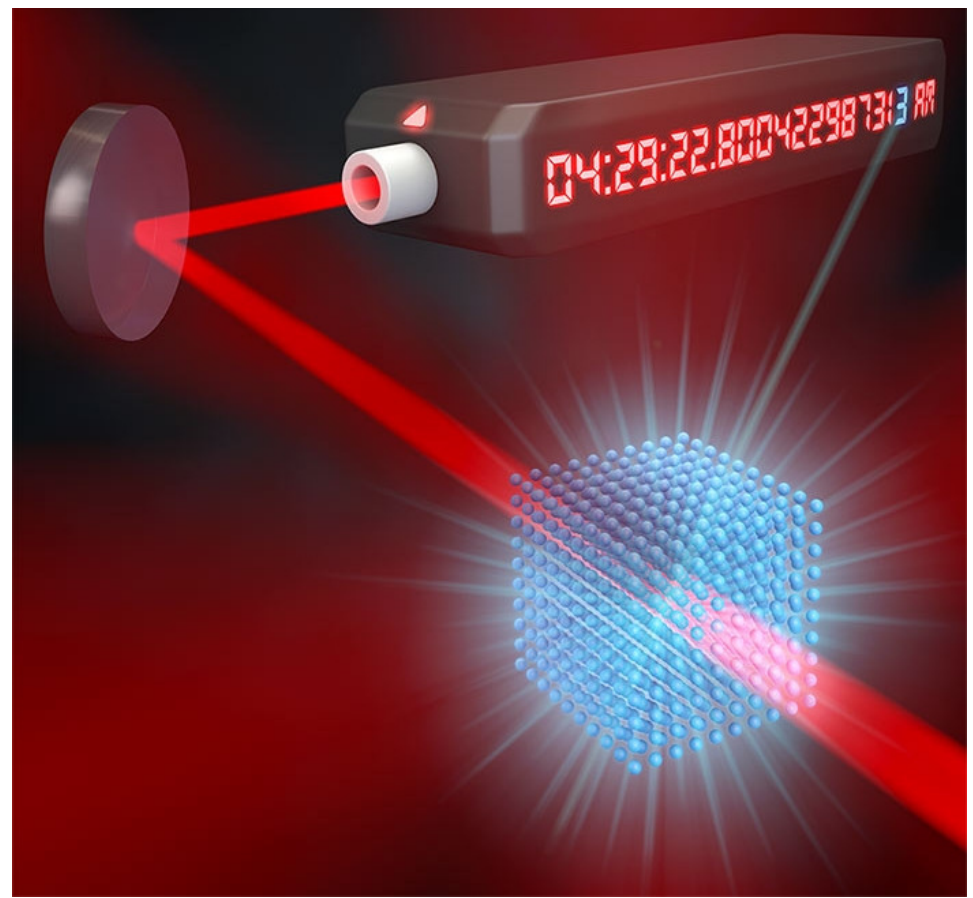
# From microwave to optical frequencies

## Cesium clock



$9 \times 10^9$  periods per second

## Strontium optical atomic clock

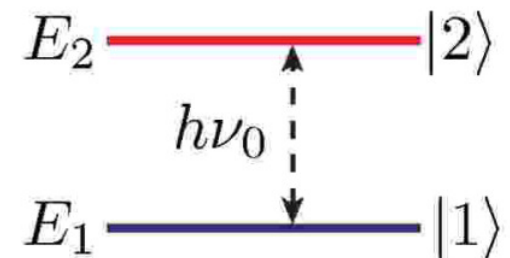
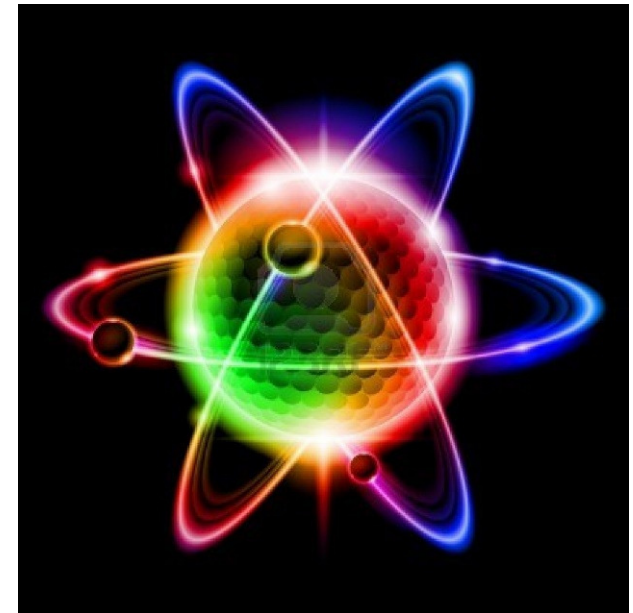


$4.3 \times 10^{14}$  periods per second

Image credit: Ye group and Steven Burrows, JILA

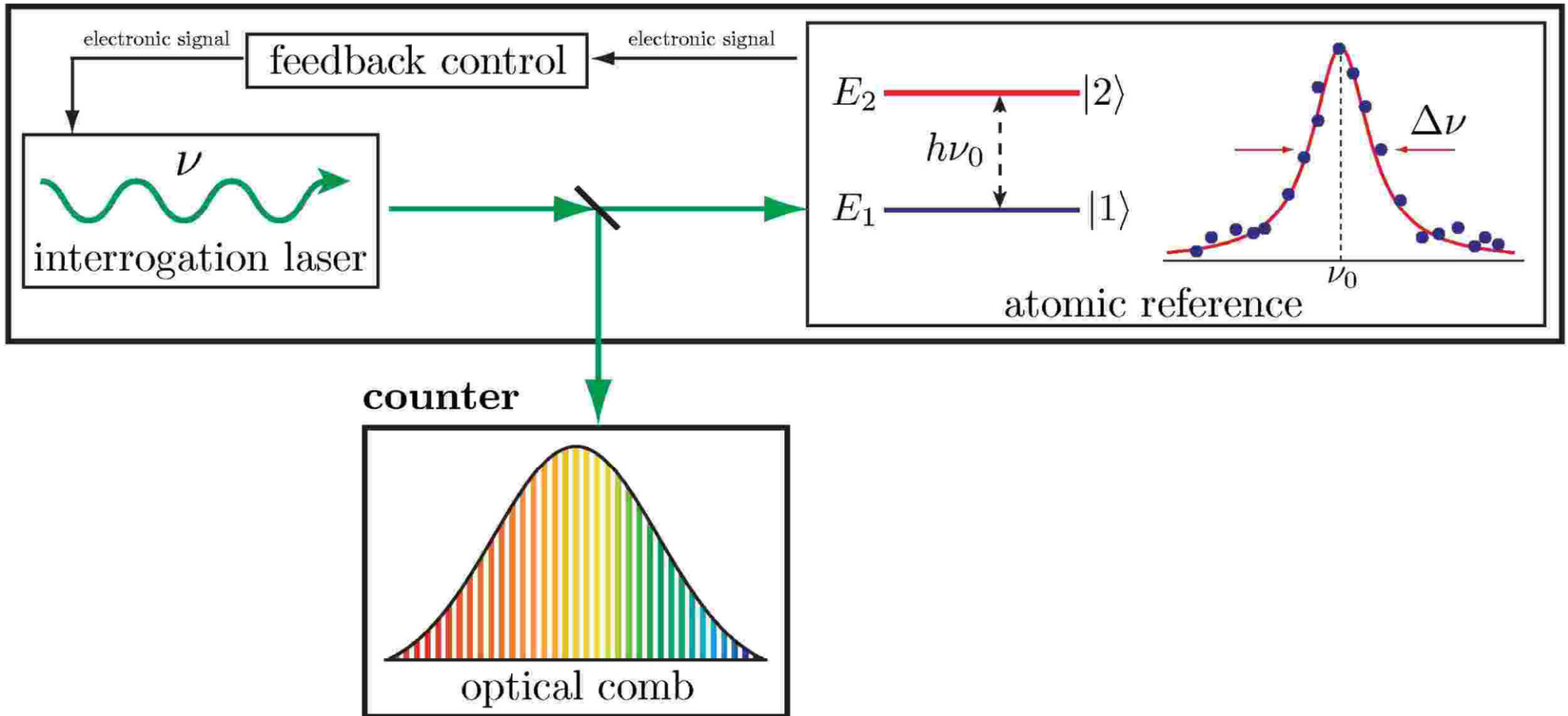
# Ingredients for an atomic clock

1. Atoms are all the same and will oscillate at exactly the same frequency (in the same environment): **you now have a perfect oscillator!**
2. Take a sample of atoms (or just one)
3. Build a device that produces oscillatory signal in resonance with atomic frequency
4. Count cycles of this signal



# What is a clock?

## atomic oscillator



Schematic view of an optical atomic clock: the local oscillator (laser) is resonant with the atomic transition. A correction signal is derived from atomic spectroscopy that is fed back to the laser. An optical frequency synthesizer (optical frequency comb) is used to divide the optical frequency down to countable microwave or radio frequency signals.

# Counting optical frequencies

Laser frequency (563 nm):  $f_{\text{Hg}}/2 \approx 5 \times 10^{14}$  Hz (!)

Interlock comparisons:

- Other optical standards (Al<sup>+</sup>, Ca, Yb, Sr, etc.)  
Difference frequency:  $\Delta f \sim 10^{14}$  Hz
- Microwave standards ( $f_0 \sim 10^{10}$  Hz)  
Difference frequency:  $\Delta f \sim 10^{14}$  Hz

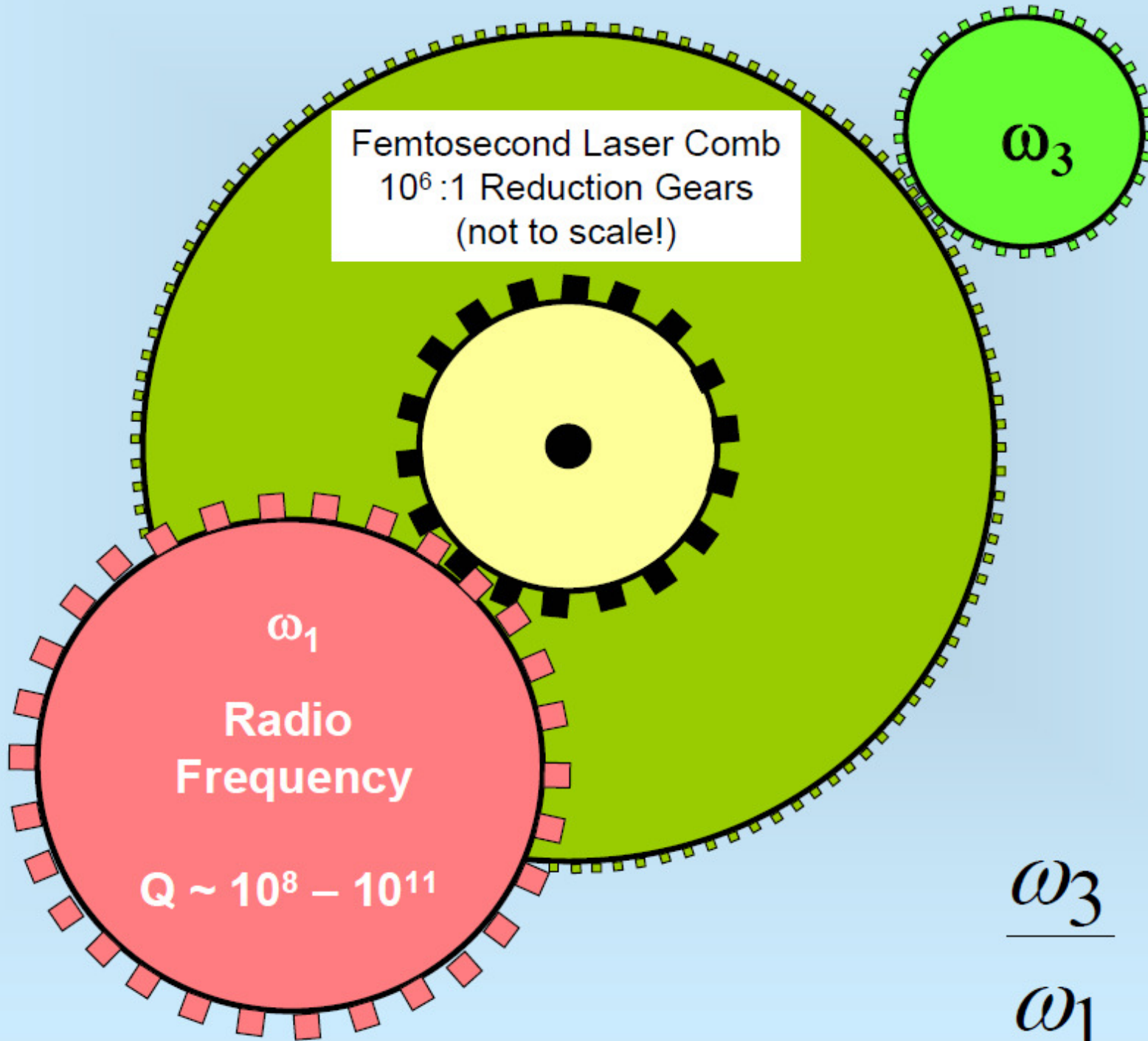
Problem:

Fastest electronic counters:  $\sim 100$  GHz ( $10^{11}$  Hz)

Solution:

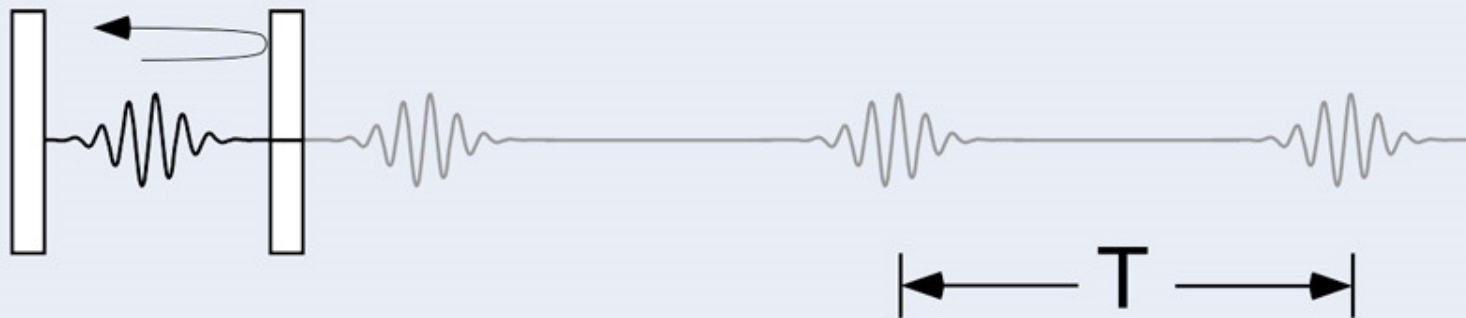
**Femtosecond laser frequency comb**

from John Hall's Nobel Lecture

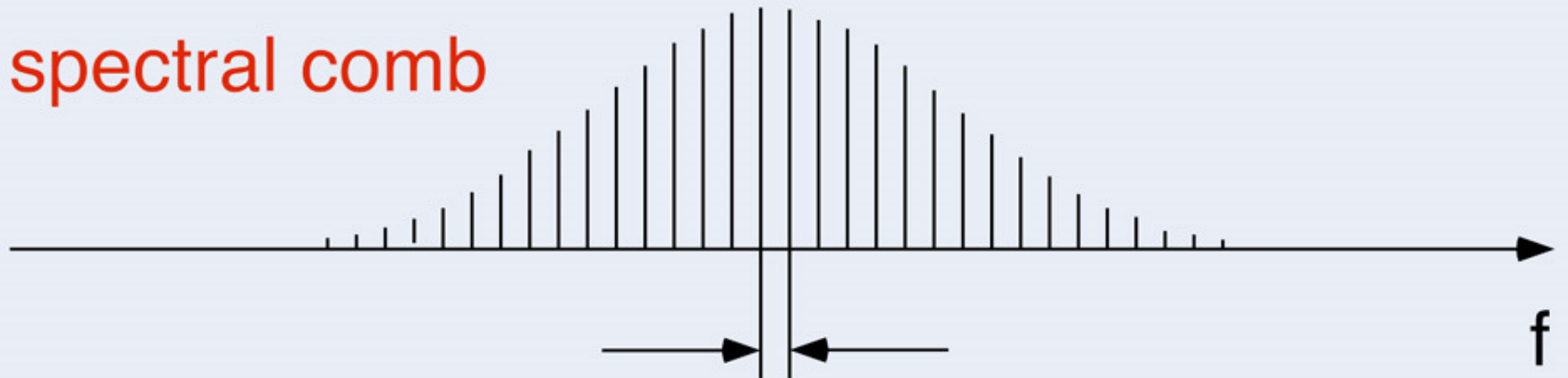


$$\frac{\omega_3}{\omega_1} \sim 10^6$$

pulse circulating inside cavity  
or emitted periodic pulse train  
= superposition of discrete modes



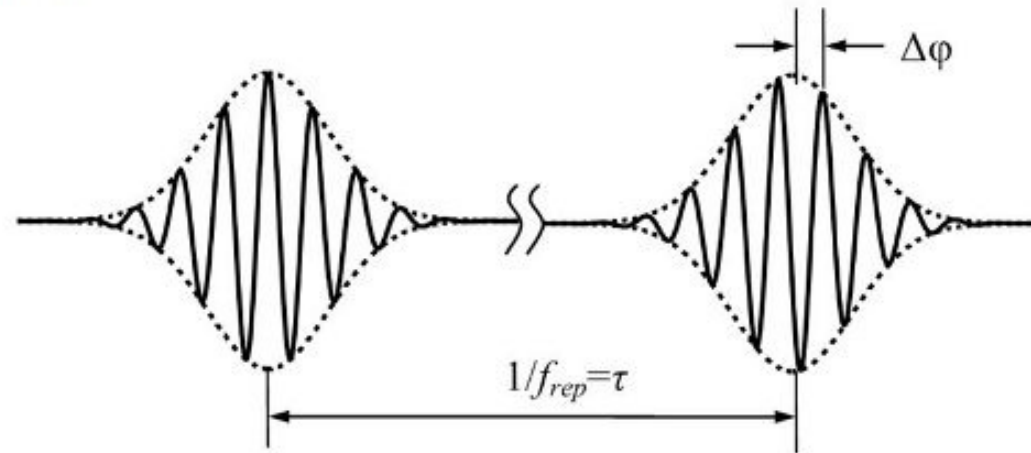
spectral comb



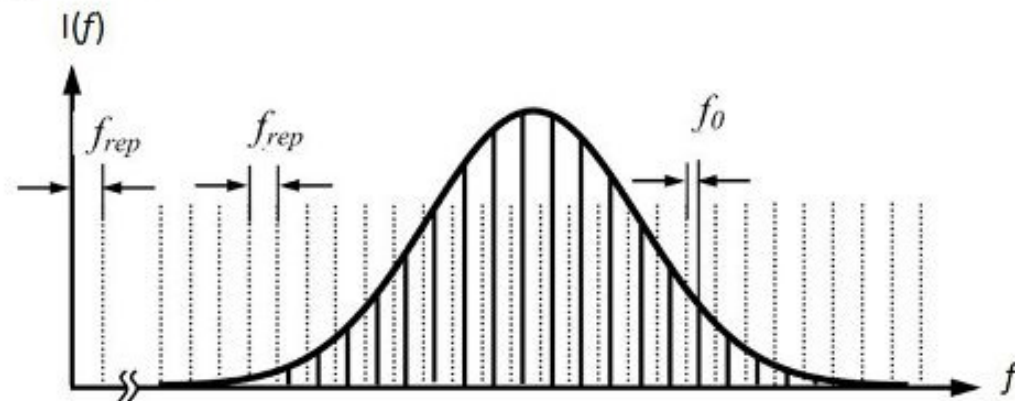
repetition rate =  $1/T$

# Femtosecond Ti:Sapphire Laser

(a) Time Domain



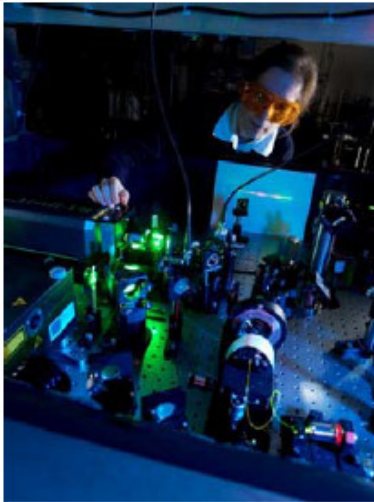
(b) Frequency Domain



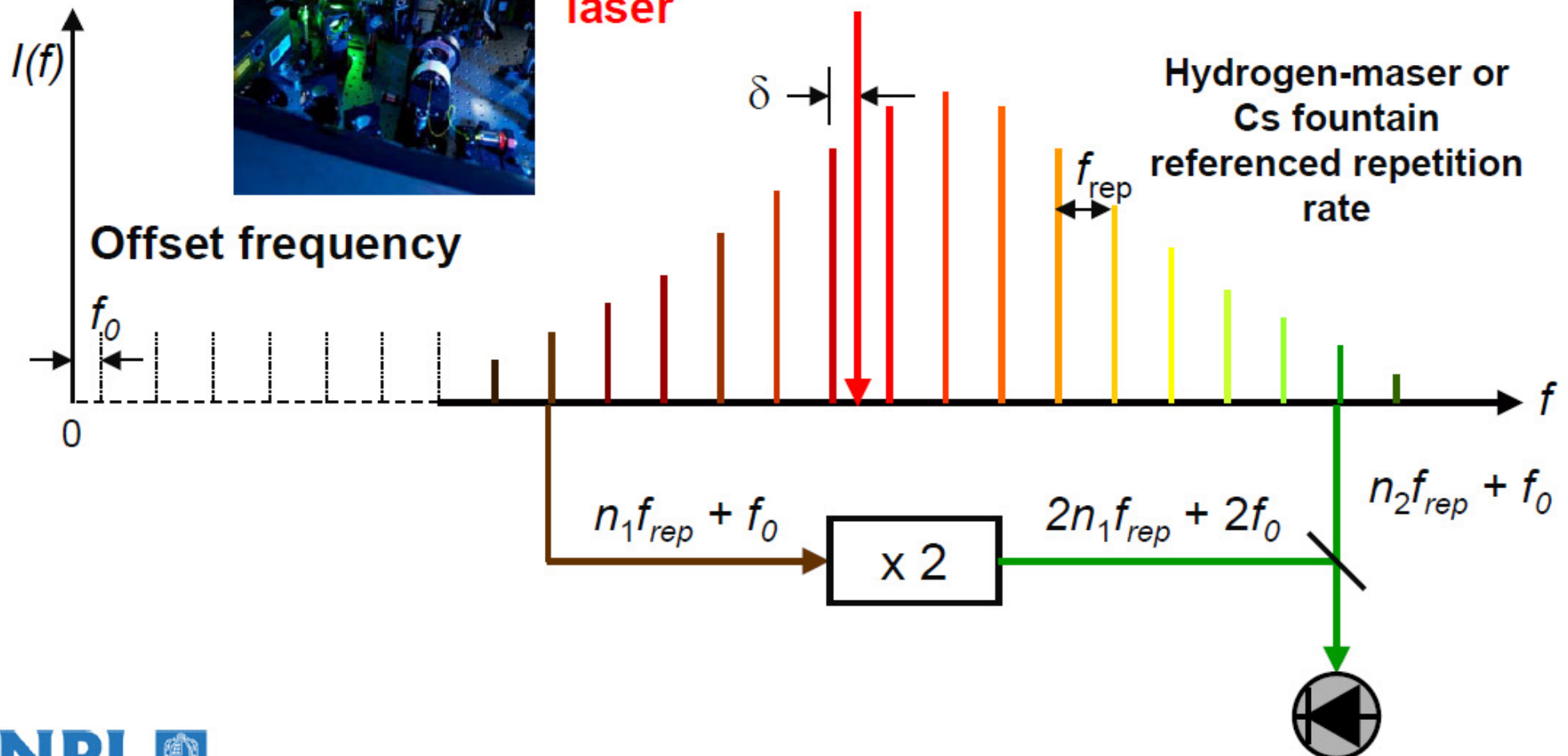
Pulse duration:  $\sim 10 \text{ fs } (10^{-14} \text{ s})$   
Repetition rate:  $f_{rep} \approx 1 \text{ GHz } (10^9 \text{ Hz})$

# Self-referenced optical frequency comb

$$f_{\text{probe}} = m f_{\text{rep}} \pm f_0 \pm \delta$$



Trapped ion probe laser

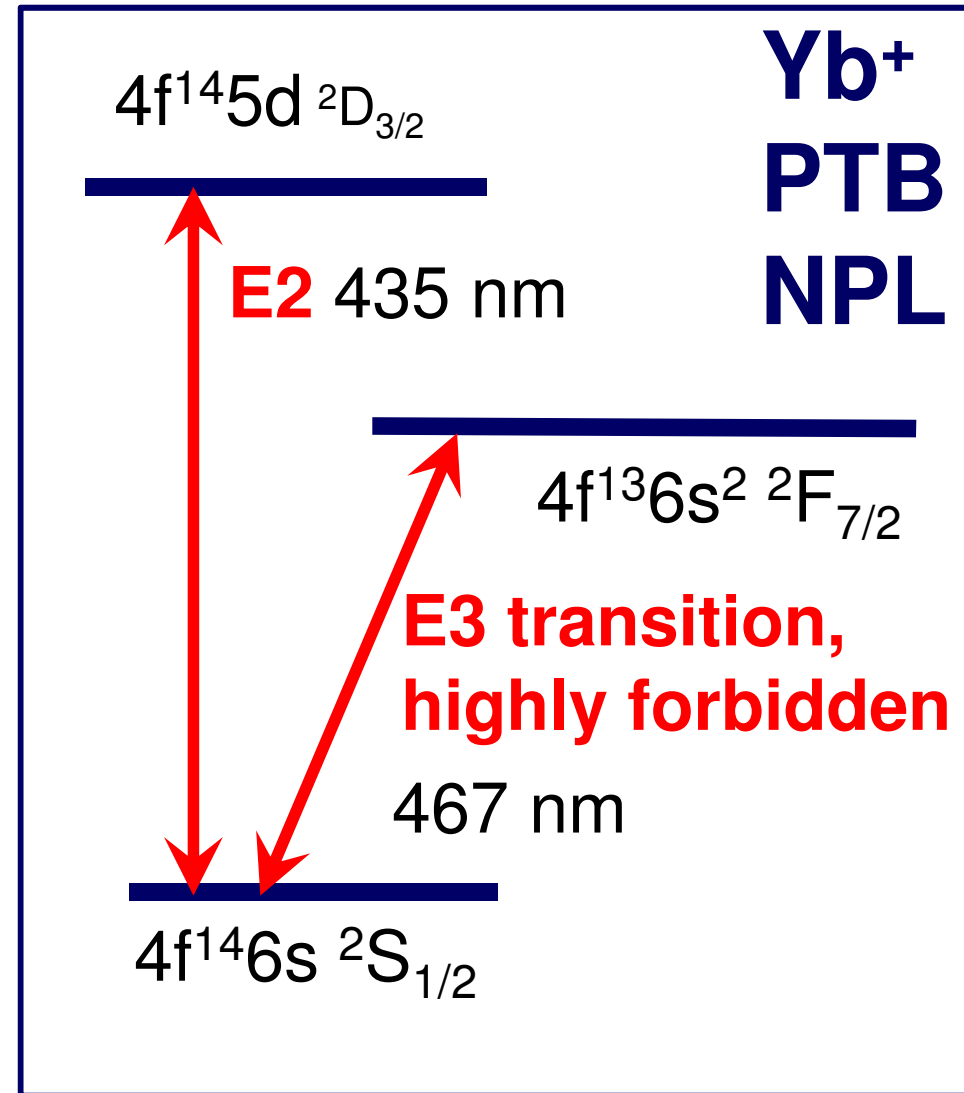
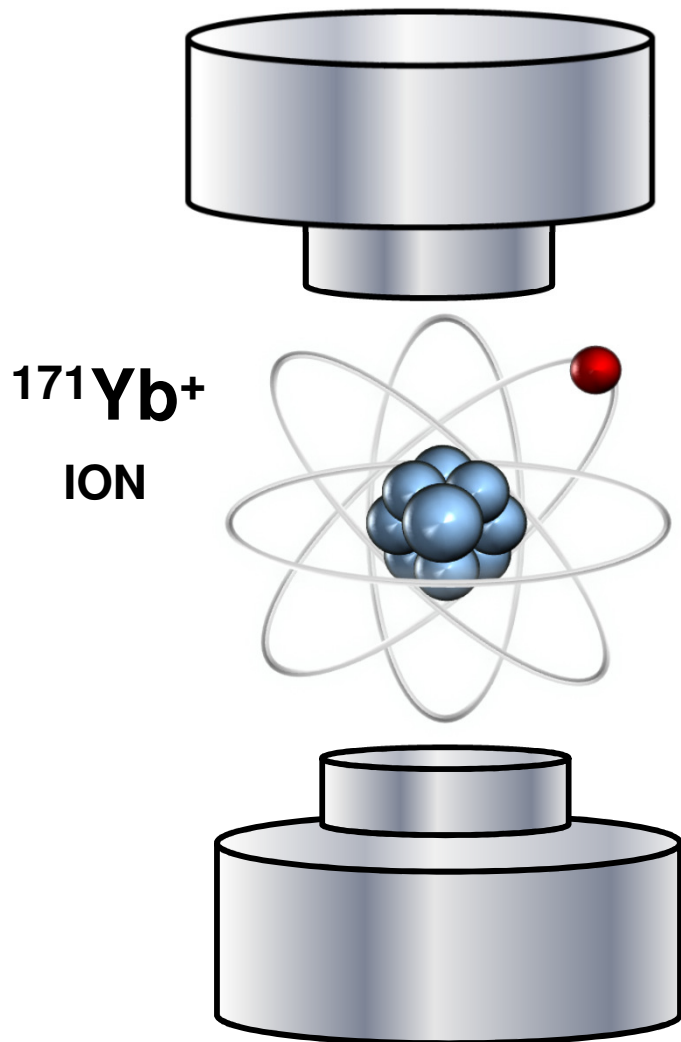




# Trapped **single** ion clocks

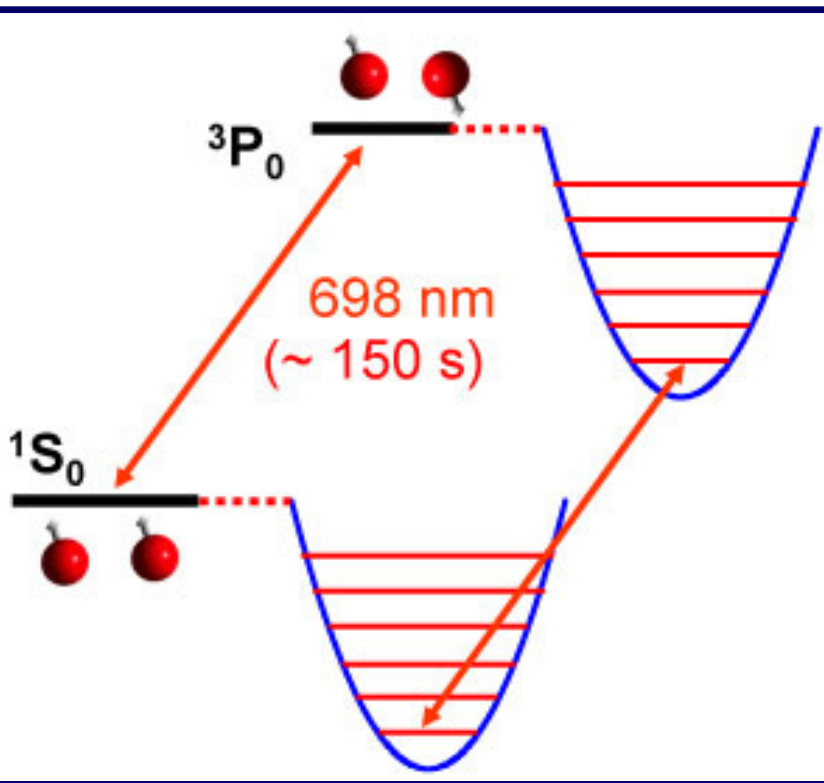
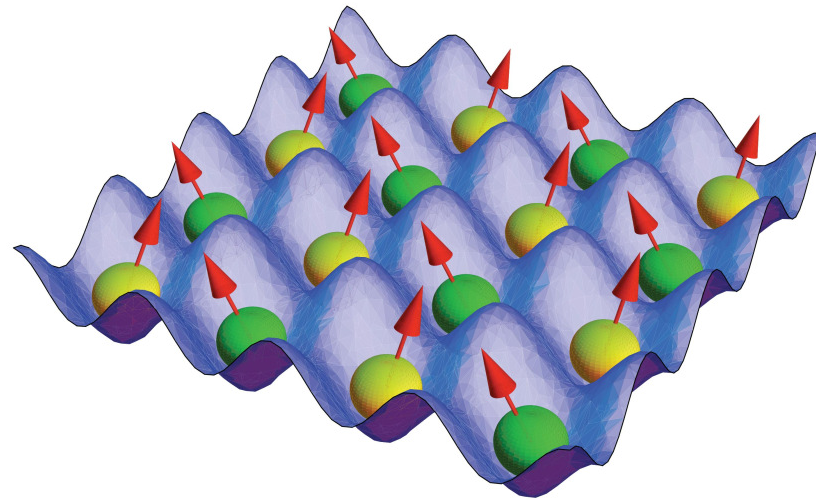
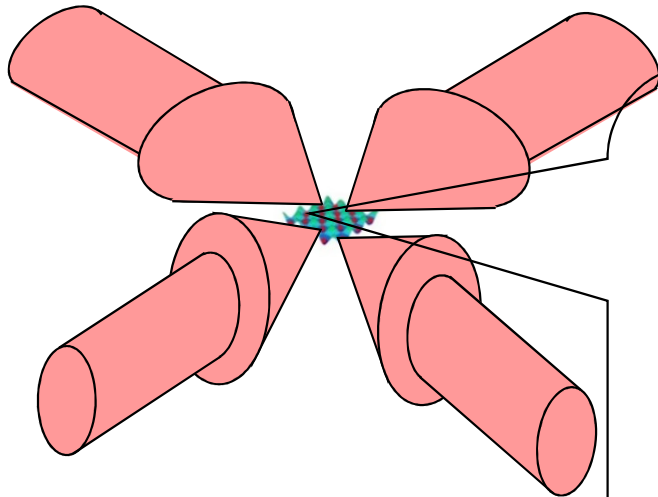
Requirements for an atomic clock

- (1) Long-lived upper clock state
- (2) Near optical transition



# Neutral atom optical lattice clocks

Optical Lattices: crystals of light



Mg  
Al<sup>+</sup>  
Cd  
Sr  
Yb  
Hg

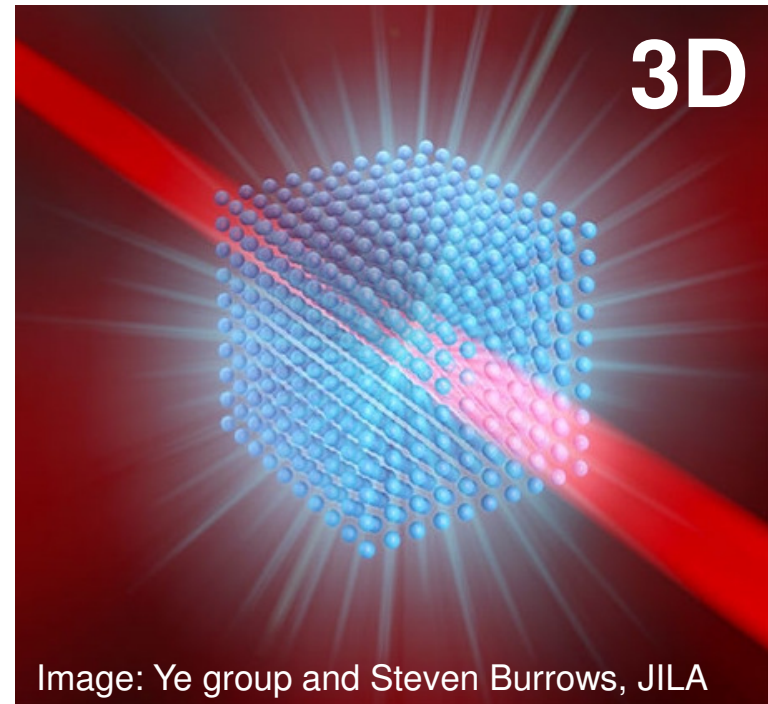
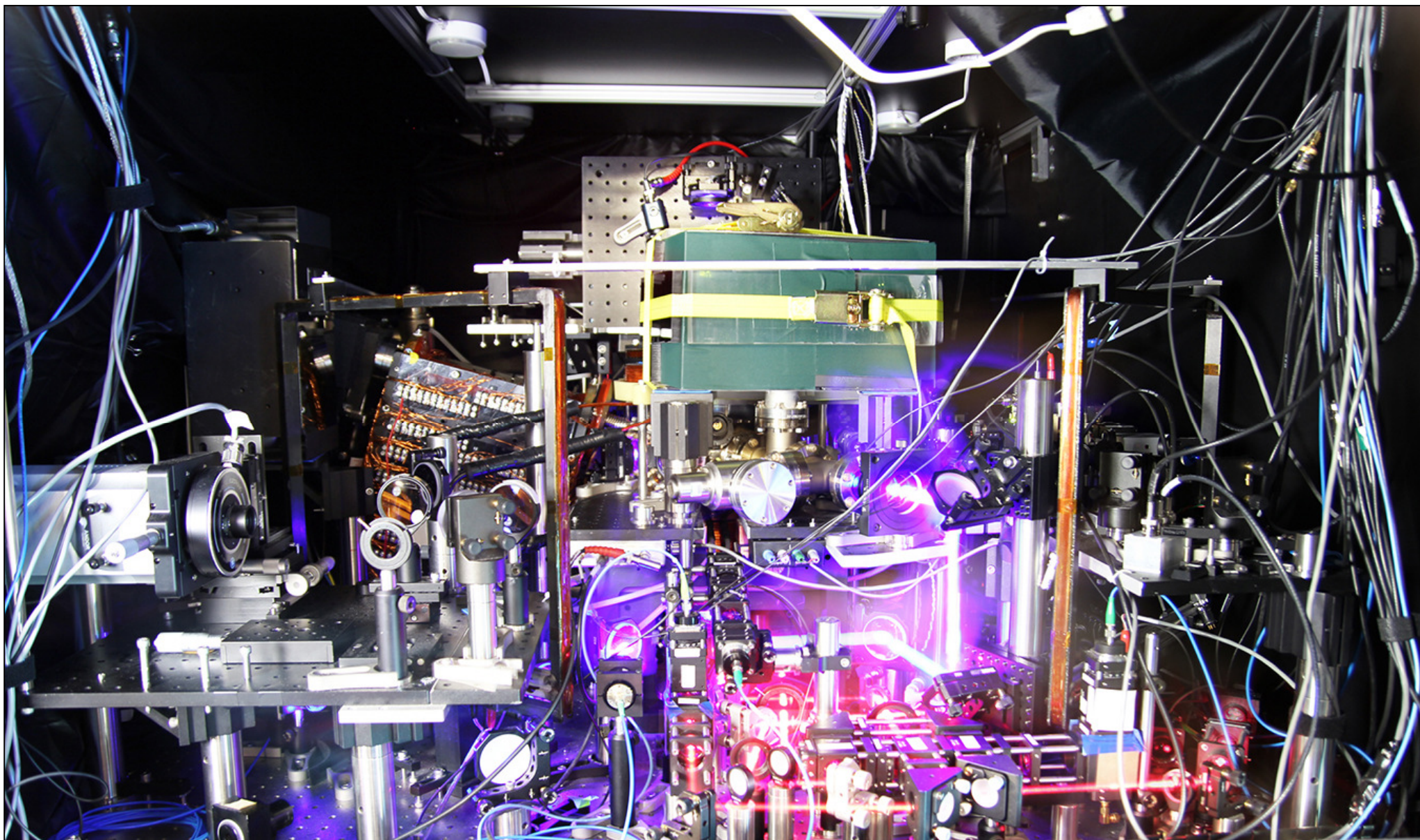


Image: Ye group and Steven Burrows, JILA

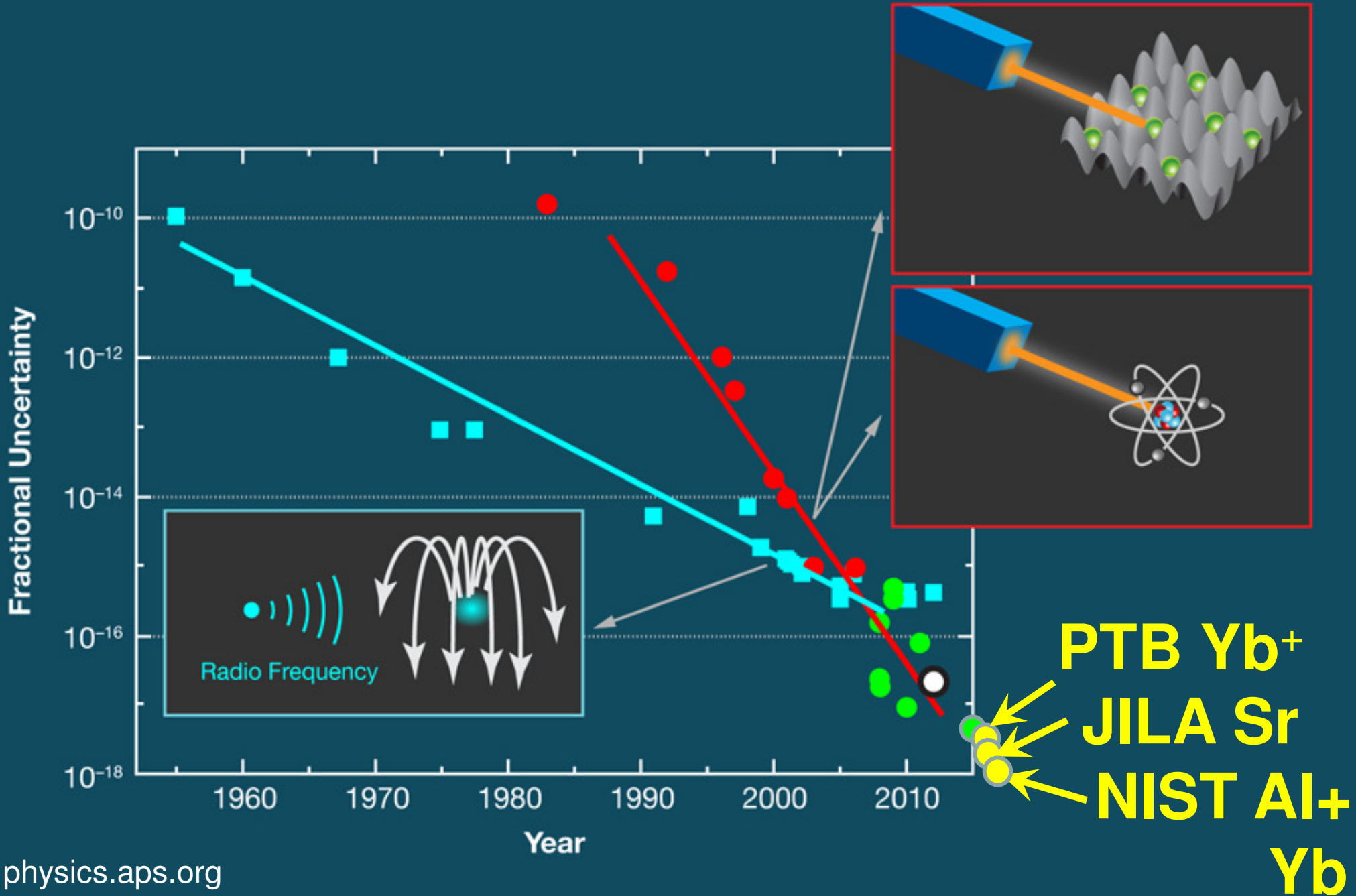
**Sr clock will lose 1 second in 15 billion years !**



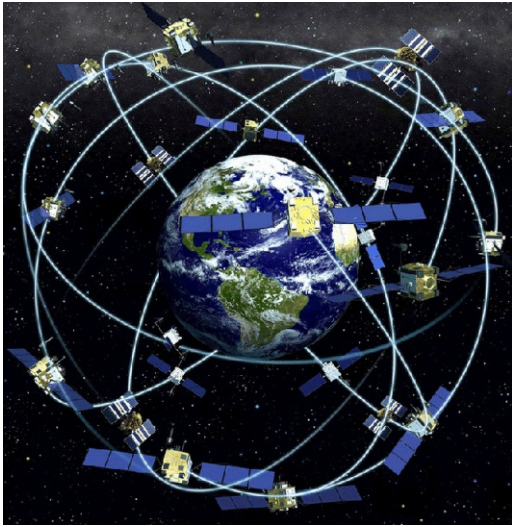
Nicholson et al., Nature Comm. 6, 6896 (2015) **Sr:  $2 \times 10^{-18}$**

[http://www.nist.gov/pml/div689/20140122\\_strontium.cfm](http://www.nist.gov/pml/div689/20140122_strontium.cfm)

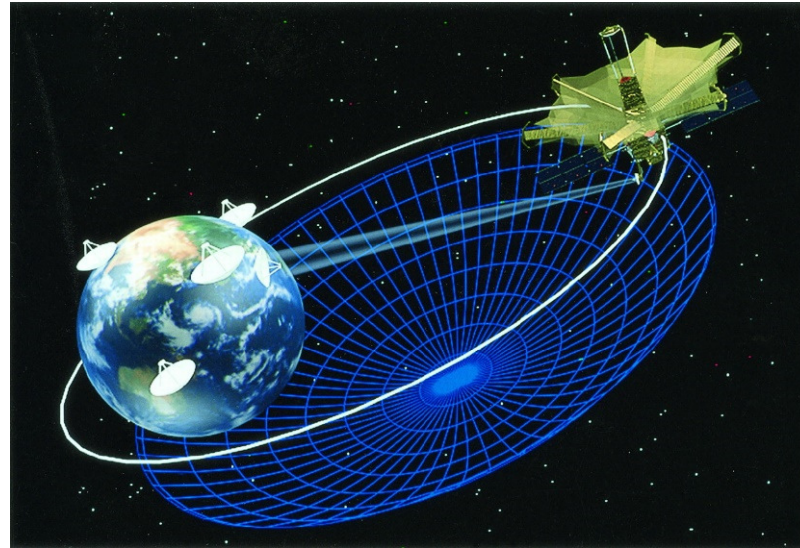
# Optical vs. microwave clocks



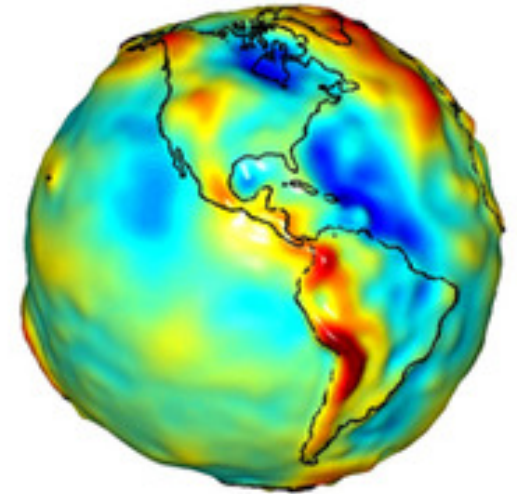
# Applications of atomic clocks



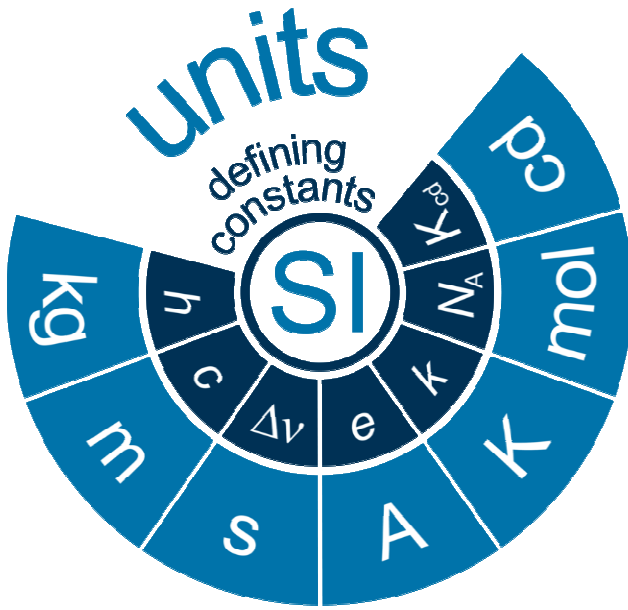
GPS



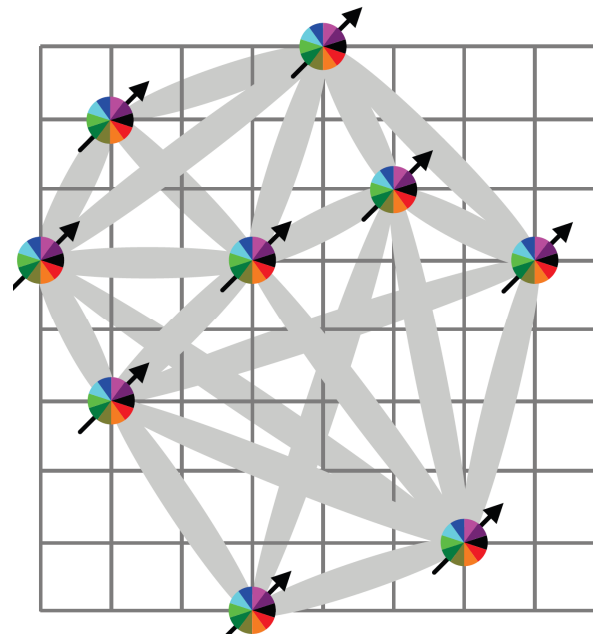
Very Long Baseline Interferometry



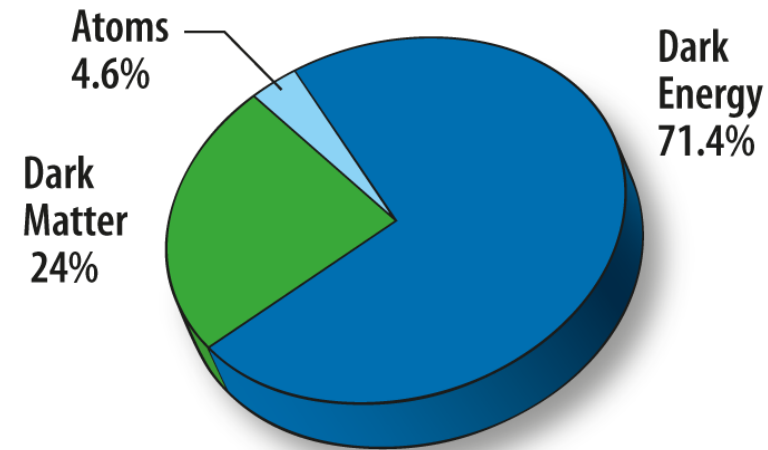
Relativistic geodesy



Definition of the second



Quantum simulation



Search for physics beyond the Standard Model

# Search for physics beyond the standard model with **atomic clocks**

Atomic clocks can measure and compare frequencies to exceptional precisions!

If fundamental constants change (now) **due to for various “new physics” effects** atomic clock may be able to detect it.

