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Probing Sizes and Shapes of Nobelium Isotopes by Laser Spectroscopy

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(Received 2 March 2018; revised manuscript received 20 April 2018; published 8 June 2018)

Until recently, ground-state nuclear moments of the heaviest nuclei could only be inferred from nuclear spectroscopy, where model assumptions are required. Laser spectroscopy in combination with modern atomic structure calculations is now able to probe these moments directly, in a comprehensive and nuclearmodel-independent way. Here we report on unique access to the differential mean-square charge radii of ^{252,253,254}No, and therefore to changes in nuclear size and shape. State-of-the-art nuclear density functional calculations describe well the changes in nuclear charge radii in the region of the heavy actinides, indicating an appreciable central depression in the deformed proton density distribution in ^{252,254}No isotopes. Finally, the hyperfine splitting of ²⁵³No was evaluated, enabling a complementary measure of its (quadrupole) deformation, as well as an insight into the neutron single-particle wave function via the nuclear spin and magnetic moment.

DOI: 10.1103/PhysRevLett.120.232503

The heaviest elements owe their existence to a subtle balance between the attractive nuclear force and the Coulomb repulsion. The attractive force leads to strong shell effects that increase the binding energy, and thus the half-life, by more than 15 orders of magnitude compared to early expectations [1]. Coulomb rearrangement plays a key role in superheavy nuclei, resulting in a central depression in the density distribution, and may even result in bubble nuclei (see Ref. [2] and references therein). Unfortunately, measurements of charge or matter radii have stopped short of transfermium nuclei. The nuclei between the spherical ²⁰⁸Pb and a predicted island of enhanced stability in the region of the superheavy nuclei [3] are expected to be deformed [4]. Evidence for the deformation is provided by the observation of K-isomers [5,6] and from rotational bands in nuclear decay spectroscopy-for example, in ²⁵⁴No [7,8] or ²⁵⁶Rf [9]. The deformation parameters and other nuclear properties such as the magnetic moment are then derived based on a model-dependent interpretation of such rotational levels built on the nuclear ground state [10]. Laser spectroscopy, on the contrary, enables probing the nuclear ground state directly: the atomic spectra of different isotopes reveal information on the nuclear spin, nuclear moments, and differential nuclear mean-charge radii [11]. Atom-at-a-time laser spectroscopy of the heavy actinide element nobelium (No, Z = 102), in which the ${}^{1}S_{0} \rightarrow {}^{1}P_{1}$ transition at an excitation energy of $\bar{\nu}_{1} = 29961.457 \text{ cm}^{-1}$ was identified [12], was a prerequisite for our studies. Here, we report detailed laser spectroscopy on the nobelium isotopes 252,253,254 No from which, in combination with state-of-the-art atomic calculations, information on the underlying nuclear structure is obtained.

The radiation detected resonance ionization spectroscopy (RADRIS) technique [13,14] employs a two-step photoionization process along with an unambiguous identification via radioactive decay detection. The nobelium isotopes ^{252,253,254}No were produced in the two-neutron evaporation channel of the complete fusion of ⁴⁸Ca with 206,207,208 Pb with cross sections of 0.5 μ b (252 No), 1.3 μb (²⁵³No), and 2 μb (²⁵⁴No) [15]. The ⁴⁸Ca beam was provided by the linear accelerator (UNILAC) of GSI Helmholtzzentrum für Schwerionenforschung in Darmstadt with average beam currents of 0.7 particle μA (about 4.4×10^{12} particles per second). The fusion-evaporation products, recoiling from the PbS targets, with a thickness of about 440 μ g/cm², were separated in flight from the primary beam by the separator for heavy ion reaction products (SHIP) [16]. At best, four ions per second were injected into a buffer-gas stopping cell installed at the focal plane of SHIP. A 3.5-µm-thick, aluminized Mylar foil window separated the gas environment of the gas cell from the high vacuum of SHIP. The ions were thermalized in 95 mbar ultrahigh-purity argon gas (99.9999%), accumulated, and neutralized on a tantalum catcher filament. For a short time during every measurement, the primary beam was chopped out before the filament was heated to temperatures of about 1050 °C, at which neutral nobelium atoms are efficiently released [17]. For best performance, we varied the collection time with respect to the half-life of the isotope [18]: 3 s for ²⁵²No ($T_{1/2}$ = 2.4 s), 37 s for ²⁵³No ($T_{1/2}$ = 97 s), and 25 s for ²⁵⁴No ($T_{1/2}$ = 51.2 s). The released atoms were probed by two laser beams of suitable wavelengths in a two-step photoionization scheme (see inset in Fig. 1). The second step was set to a wavelength $\lambda_2 = 351$ nm such that the total excitation energy exceeded the first ionization potential (IP) for nonresonant ionization, with a pulse energy density of 2 mJ/cm^2 . This laser efficiently ionized atoms that were excited to the ${}^{1}P_{1}$ state, as well as the fraction of atoms where the population was subsequently transferred to a long-lived atomic state by gas collisions [19]. Ions created by resonant laser ionization were guided by electrostatic potentials to a silicon detector and identified by their characteristic α -decay energy or additionally by the detection of high energetic fission fragments in the case of ²⁵²No. This method enables a selective and efficient laser spectroscopy, resulting in a total efficiency of 3.3(1.0)% for ²⁵²No [12], 8.2(2.5)% for ²⁵³No,



FIG. 1. Measured excitation spectra of the ${}^{1}P_{1}$ level for the isotopes 254 No, 253 No, and 252 No with a best fit to the data (solid line). The dashed line represents the center of each resonance, while the solid vertical lines in the 253 No spectrum indicate the position and strength of the individual hyperfine structure components with total angular momentum F = 7/2, 9/2, and 11/2 at 3.99 GHz, 4.10 GHz, and 10.74 GHz, respectively. The inset shows a schematic ionization scheme.

and 6.4(1.0)% for ²⁵⁴No [12]. To probe nuclear properties of the nobelium isotopes, we scanned the first excitation step around the ${}^{1}P_{1}$ level with a resolution of about 4 GHz (FWHM) limited mainly by the laser bandwidth (1.2 GHz) and collisional broadening (4 GHz). For ²⁵²No, we operated the laser with an increased laser bandwidth of 5.5 GHz, which reduced the final resolution, but also reduced the number of scan steps for a more efficient beamtime usage. The measured spectra are shown in Fig. 1.

Besides a shift of the resonance centroid of the individual isotopes, the spectrum of the odd-mass isotope ²⁵³No additionally features a splitting. This originates from the hyperfine interaction that leads to a coupling of the electron angular momentum J with the nuclear spin I. The resulting splitting ΔE_{HFS} depends on the total angular momentum F and the hyperfine coupling constants $A_{\text{HFS}} = \mu(B_e/IJ)$ and $B_{\rm HFS} = eQ_{\rm s} \langle (\partial^2 V / \partial z^2) \rangle$, where μ and $Q_{\rm s}$ are the magnetic dipole moment and the spectroscopic quadrupole moment of the nucleus, respectively. The magnetic dipole moment μ couples to the magnetic field created by the electron orbital at the nucleus B_e , while Q_s links to the electric field gradient at the nucleus $\langle (\partial^2 V / \partial z^2) \rangle$ with the elementary charge e. These atomic parameters, which are isotope independent and connect atomic observables to nuclear properties, were obtained from state-of-the-art atomic calculations. Different theoretical approaches were applied to calculate these parameters for nobelium: configuration interaction (CI) with the single-double coupled cluster

TABLE I. Summary of the atomic calculations, the experimental results, and the extracted nuclear parameters for ^{252,253,254} No. The
values of the calculated HFS coupling parameters B_e/J and $\langle \partial^2 V/\partial z^2 \rangle$, the field shift constant F_s , and the mass shift constant M have
been calculated with different techniques in this work and are presented together with the spectroscopic results obtained in the
experiment. From these values the nuclear magnetic moment μ , the spectroscopic quadrupole moment Q_s , and the changes in mean
square charge radii $\delta \langle r^2 \rangle$ between the nuclei are extracted. μ_N denotes the nuclear magneton.

Atomic calculations	Hyperfine splitting for ²⁵³ No		Isotope shift	
	B_e/J (GHz $\cdot I/\mu_N$)	$\langle \partial^2 V / \partial z^2 \rangle$ (GHz/eb)	F_s (GHz/fm ²)	M (GHz · amu)
CI + all orders	$-6.3(0.9)^{a}$	$0.486(70)^{a}$	$-95.8(7.0)^{a}$	
CI + MBPT	-7.1(1.0)	0.503(75)	-104(10)	
CIPT	-7.4(1.2)	0.624(90)	-94(25)	
FSCC		$0.465(70)^{a}$	-99(15)	
MCDF	-4.1(1.8)	0.444(75)	-113(25)	$-1044(400)^{a}$
Spectroscopic results	A _{HFS} (GHz)	$B_{\rm HFS}$ (GHz)	$\delta \nu^{254,253}$ (GHz)	$\delta \nu^{254,253}$ (GHz)
	0.734(46)	2.82(69)	6.72(18)	10.08(69)
Nuclear properties	$\mu(\mu_N)$	$Q_{\rm s}$ (eb)	$\delta \langle r^2 \rangle^{254,253}$ (fm ²)	$\delta \langle r^2 \rangle^{254,252}$ (fm ²)
	-0.527(33)(75)	+5.9(1.4)(0.9)	-0.070(2)(5)	-0.105(7)(7)

^aValues used to deduce nuclear ground-state parameters.

method (CI + all orders) [20], CI combined with manybody perturbation theory (MBPT) [21-23], and relativistic Fock space coupled cluster (FSCC) [24] as well as multiconfiguration Dirac-Fock (MCDF) calculations [25,26]. The results of these calculations are summarized in Table I. In general, the different methods agree with one another to within about 20%. By applying a newly developed method which is based on the CI technique but treats high-energy states perturbatively (CIPT method) [27], the influence of configuration mixing on the investigated ${}^{1}P_{1}$ level was evaluated at the cost of an increased uncertainty. This allowed us to verify and exclude a possible scenario of a strong mixing with core excitations. From systematic investigations of chemical elements with similar electronic configurations, the most accurate values for the hyperfine coupling parameter B_e/J and the isotope field shift constant F_s are expected for CI + all orders calculations. Thus, these results were taken for extracting the nuclear properties. CI + all orders calculations and FSCC calculations provide the same uncertainty for the parameter $\langle \partial^2 V / \partial z^2 \rangle$ for which an average value of 0.476(70) GHz/eb was used in the evaluation.

From a total of three HFS transitions to the ${}^{1}P_{1}$ state in 253 No, only two were resolved. The splitting of the hyperfine structure (HFS) levels depends on the nuclear spin. Under the assumption of a prolate shape of the 253 No nucleus, and by considering the sign of the extracted magnetic moment and the χ^{2} of the fit, a nuclear spin of $I({}^{253}$ No) = 9/2, which was used later on in the evaluation, is favored over $I({}^{253}$ No) = 7/2. This result independently substantiates conclusions from nuclear spectroscopy [28,29]. The hyperfine coupling constants $A_{\rm HFS} = 0.734(46)$ GHz and $B_{\rm HFS} = 2.82(67)$ GHz for 253 No were derived from a χ^2 minimization of a rate equation model to the experimental data which includes saturation effects from the pulsed laser excitation on the individual intensities [30]. For ²⁵³No, which features an even proton number, Z = 102, and an odd neutron number, N = 151, the nuclear magnetic properties arise mainly from the unpaired neutron. Our experimental determination of the magnetic dipole moment to $\mu(^{253}No) = -0.527(33)(75) \mu_N$ therefore enables probing nuclear shell model predictions of the underlying nuclear single-neutron wave function. The first parenthesis refers to the statistical uncertainty (1 σ), and the second parenthesis refers to the uncertainty from atomic calculations. The nuclear magnetic moment of the bandhead of a rotational band in a well-deformed nucleus, such as that expected in the case of ²⁵³No, can be written as

$$\mu/\mu_N = g_K \frac{I^2}{I+1} + g_R \frac{I}{I+1}.$$
 (1)

It depends on the rotational g factor $0.7Z/A \le g_R \le Z/A$ [31] and the single-particle intrinsic g factor g_K , which so far was calculated from nuclear models. From our data on the magnetic moment, an average value of $g_K^{exp} = -0.22(5)$ is extracted, which considers the stated range of g_R . This result is consistent with a calculated value of $g_K = -0.25$ reported in Refs. [29,32] for the $I(^{253}No) = 9/2^{-}[734]$ ground-state configuration, while it disagrees with a different calculated value $g_K = -0.12$, reported in Ref. [33].

From the $B_{\rm HFS}$ value of the HFS splitting, a spectroscopic quadrupole moment of $Q_{\rm s}(^{253}{\rm No}) = +5.9(1.4)(0.9)$ eb is deduced, indicating a strong prolate deformation of the ²⁵³No nucleus, in agreement with the observation of *K*-isomers in nobelium isotopes [5]. From



FIG. 2. The change in the nuclear mean square charge radii $\delta \langle r^2 \rangle$, for ^{252–254}No and even Z actinide nuclei starting from thorium, is plotted as a function of the neutron number with arbitrary offset. For each element, the DFT calculations with two Skyrme energy density functionals, UNEDF1 [36] (dashed line) and SV-min [37] (solid line), are shown. The slope according to a schematic droplet model assuming a constant deformation for the actinide elements referenced to N = 138 is marked in gray.

our result, an intrinsic quadrupole moment of $Q_0(^{253}\text{No}) =$ +10.8(2.6)(1.7) eb is extracted. This value is comparable with the shell-model-dependent value of $Q_s(^{254}\text{No}) =$ +13.1 eb [32,33], obtained from the moment of inertia in the rotational band built on the ground state of ^{254}No [7,8]. These values indicate a constant deformation in the isotope chain of nobelium around the neutron shell closure N = 152.

Information on the deformation of the even mass nuclei ^{252,254}No with zero nuclear spin can be obtained from laser spectroscopic measurements through a complementary route. The change in deformation is manifested in the isotope shift (IS) of an atomic transition $\delta\nu^{A,A'} = \nu^{A'} - \nu^A$ between two isotopes *A* and *A'* with masses m_A and $m_{A'}$. IS values of $\delta\nu^{254,253} = 6.72(18)$ GHz and $\delta\nu^{254,252} = 10.08(69)$ GHz were measured in this work. The IS arises from a mass shift, with a mass-shift constant *M*, and a field shift, with a field-shift constant *F_s*. The latter is the dominant factor for heavy elements and is characterized by the density of the electron wave function inside the nucleus. The IS is related to the change in the nuclear mean square charge radius $\delta\langle r^2 \rangle^{A,A'}$ by

$$\delta\nu^{A,A'} = \frac{m^{A'} - m^A}{m^{A'}m^A}M + F_s\delta\langle r^2\rangle^{A,A'}.$$
 (2)

The constants M and F_s were determined by atomic calculations, as summarized in Table I. The obtained changes in mean square charge radii for the nobelium isotopes in comparison to experimental values for other actinides [34,35] are shown in Fig. 2. The experimental results for different actinide isotopes agree well with calculated values from self-consistent nuclear density functional theory (DFT) without any symmetry restrictions [38]

for even-even nuclides obtained with two Skyrme functionals. An alternative to the Skyrme functionals are the Fayans functionals, which recently have been optimized with a focus on charge radii [39]. However, those functionals overestimate the pairing correlations particularly in the actinide region, which could have a significant influence on the results. The proton density distribution for ²⁵⁴No predicted by UNEDF1 is shown in Fig. 3. The calculated distribution clearly indicates the deformation as well as a central depression, which originates from the strong Coulomb repulsion (see, e.g., Refs. [2,40,41]). The maximum in quadrupole deformation, defined by the deformation parameter β_2 , is predicted by the DFT calculations to be around N = 148, as shown in the upper panel in Fig. 3. For the nobelium isotopes, this results in a deformation parameter which only changes slightly for the investigated isotopes. This is in line with other calculations [4,42,43], experimental results from in-beam gamma spectroscopy of ^{252,254}No [7,44], and the spectroscopic quadrupole moment from our HFS measurements in ²⁵³No. The central depression of the proton distribution is displayed in the lower panel in Fig. 3. The relative depth of the central depression, defined as $(\rho_{\text{max}} - \rho_c)/\rho_{\text{max}}$ with the maximum proton density ρ_{max} and the proton density in the center ρ_c , increases with an increasing deformation parameter, which leads to an additional contribution to the charge radii. In general, our experimental results are in good agreement with DFT calculations. For comparison, the results of $\delta \langle r^2 \rangle$ from a parameterization of a droplet model (DM) [45,46] at a constant deformation, as typically done in laser spectroscopic investigations up to the lead region [11], are shown for Z = 90-102 in Fig. 2 in gray. Typically, a deviation from this slope is attributed to changes in deformation, but the experimental values for nuclei around the maximum in deformation continue to deviate. This indicates that the



FIG. 3. Upper panel: Deformation parameter β_2 for different even-even isotopes of Th, U, Pu, Cm, and No obtained from the DFT calculations with the UNEDF1 functional. The inset figure shows the calculated proton distribution of ²⁵⁴No from highest density (red) to low density (blue). Lower panel: Relative depth of the central depression.

increase in charge radii is underestimated by the DM in this region of high Z and strongly deformed nuclei. In summary, nuclear ground-state properties were obtained from laser spectroscopy for the nobelium isotopes ^{252,253,254}No. The results are the first of their kind in the transfermium region, where elements are available in single-atom-at-atime quantities only. Besides the first experimental determination of the magnetic dipole and spectroscopic quadrupole moment of ²⁵³No, the results of the isotope shift match well with changes in mean square charge radii calculated by nuclear DFT, which predict a strong central depression in the charge density of more than 12%. Laser spectroscopy, in combination with state-of-the art atomic calculations, can now also be employed to study the structure of K-isomers and the properties of deformed nuclei in the heavy-element region around nobelium, which forms the basis for a better understanding of the nuclear structure of the heaviest elements.

We thank the staff of the GSI ion source and accelerator for the preparation of a stable ⁴⁸Ca beam and the staff of the GSI target laboratory for providing high-quality targets. We acknowledge the technical support of J. Maurer, H.-G. Burkhard, D. Racano, L. Braisz, D. Reemts, B. Schausten, and I. Kostyuk. This work was supported by the German Federal Ministry of Education and Research under Contracts No. 06MZ169I, No. 06LM236I, FAIR No. 05P09RDFN4, No. 05P12RDFN8, NuSTAR No. 05P15SJCIA, and No. 05P15RDFN1; by the GSI; and by the Helmholtz-Institut Mainz. This project has also received funding from the European Union Horizon 2020 research and innovation program under Grant Agreement No. 654002 (ENSAR2). This work was supported by U.S. NSF Grant No. PHY-1620687, by the U.S. Department of Energy under Awards No. DOE-DE-NA0002847 (NNSA, the Stewardship Science Academic Alliances program), No. DE-SC0013365, No. DE-SC0018083 (Office of Science), the National Research Council (NRC) of Canada, and the Australian Research Council. D.A. acknowledges support by the European Commission in the framework of the CEA-EUROTALENT program. M. S. S. thanks the School of Physics at UNSW, Sydney, Australia for hospitality and acknowledges support from the Gordon Godfrey Fellowship UNSW program. A. B. would like to thank the Center for Information Technology of the University of Groningen for their support and for providing access to the Peregrine high-performance computing cluster.

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- Z. Patyk, A. Sobiczewski, P. Armbruster, and K.-H. Schmidt, Nucl. Phys. A491, 267 (1989).
- [2] B. Schuetrumpf, W. Nazarewicz, and P.-G. Reinhard, Phys. Rev. C 96, 024306 (2017).

- [3] M.G. Mayer and J.H.D. Jensen, *Elementary Theory of Nuclear Shell Structure* (Wiley, New York, 1964).
- [4] P.-H. Heenen, J. Skalski, A. Staszczak, and D. Vretenar, Nucl. Phys. A944, 415 (2015).
- [5] R.-D. Herzberg, P. Greenlees, P. Butler, G. Jones, M. Venhart, I. Darby, S. Eeckhaudt, K. Eskola, T. Grahn, C. Gray-Jones *et al.*, Nature (London) 442, 896 (2006).
- [6] S. K. Tandel et al., Phys. Rev. Lett. 97, 082502 (2006).
- [7] P. Reiter et al., Phys. Rev. Lett. 82, 509 (1999).
- [8] M. Leino et al., Eur. Phys. J. A 6, 63 (1999).
- [9] P. T. Greenlees et al., Phys. Rev. Lett. 109, 012501 (2012).
- [10] C. Theisen, P. Greenlees, T.-L. Khoo, P. Chowdhury, and T. Ishii, Nucl. Phys. A944, 333 (2015).
- [11] P. Campbell, I. Moore, and M. Pearson, Prog. Part. Nucl. Phys. 86, 127 (2016).
- [12] M. Laatiaoui et al., Nature (London) 538, 495 (2016).
- [13] H. Backe, W. Lauth, M. Block, and M. Laatiaoui, Nucl. Phys. A944, 492 (2015).
- [14] F. Lautenschläger, P. Chhetri, D. Ackermann, H. Backe, M. Block, B. Cheal, A. Clark, C. Droese, R. Ferrer, F. Giacoppo, S. Götz, F. Heßberger, O. Kaleja, J. Khuyagbaatar, P. Kunz, A. Mistry, M. Laatiaoui, W. Lauth, S. Raeder, T. Walther, and C. Wraith, Nucl. Instrum. Methods Phys. Res., Sect. B 383, 115 (2016).
- [15] Y. T. Oganessian, V. K. Utyonkov, Y. V. Lobanov, F. S. Abdullin, A. N. Polyakov, I. V. Shirokovsky, Y. S. Tsyganov, A. N. Mezentsev, S. Iliev, V. G. Subbotin, A. M. Sukhov, K. Subotic, O. V. Ivanov, A. N. Voinov, V. I. Zagrebaev, K. J. Moody, J. F. Wild, N. J. Stoyer, M. A. Stoyer, and R. W. Lougheed, Phys. Rev. C 64, 054606 (2001).
- [16] G. Münzenberg, W. Faust, S. Hofmann, P. Armbruster, K. Güttner, and H. Ewald, Nucl. Instrum. Methods 161, 65 (1979).
- [17] M. Laatiaoui, H. Backe, M. Block, F.-P. Heßberger, P. Kunz, F. Lautenschläger, W. Lauth, M. Sewtz, and T. Walther, Eur. Phys. J. D 68, 71 (2014).
- [18] M. Laatiaoui, H. Backe, M. Block, P. Chhetri, F. Lautenschläger, W. Lauth, and T. Walther, Hyperfine Interact. 227, 69 (2014).
- [19] P. Chhetri et al., Eur. Phys. J. D 71, 195 (2017).
- [20] M. S. Safronova, M. G. Kozlov, W. R. Johnson, and D. Jiang, Phys. Rev. A 80, 012516 (2009).
- [21] V.A. Dzuba, Phys. Rev. A 90, 012517 (2014).
- [22] V. A. Dzuba, V. V. Flambaum, and M. G. Kozlov, Phys. Rev. A 54, 3948 (1996).
- [23] J. C. Berengut, V. V. Flambaum, and M. G. Kozlov, Phys. Rev. A 73, 012504 (2006).
- [24] E. Eliav, S. Fritzsche, and U. Kaldor, Nucl. Phys. A944, 518 (2015), special Issue on Superheavy Elements.
- [25] P. Jönsson, X. He, C. F. Fischer, and I. Grant, Comput. Phys. Commun. 177, 597 (2007).
- [26] I. P. Grant, *Relativistic Quantum Theory of Atoms and Molecules: Theory and Computation*, Vol. 40 (Springer Science & Business Media, New York, 2007).
- [27] V. A. Dzuba, J. C. Berengut, C. Harabati, and V. V. Flambaum, Phys. Rev. A **95**, 012503 (2017).
- [28] F. P. Heßberger, S. Hofmann, D. Ackermann, P. Cagarda, R. D. Herzberg, I. Kojouharov, P. Kuusiniemi, M. Leino, and R. Mann, Eur. Phys. J. A 22, 417 (2004).
- [29] A. K. Mistry et al., Eur. Phys. J. A 53, 24 (2017).

- [30] H. Backe, A. Dretzke, S. Fritzsche, R. G. Haire, P. Kunz, W. Lauth, M. Sewtz, and N. Trautmann, Hyperfine Interact. 162, 3 (2006).
- [31] A. Bohr and B. R. Mottelson, Nuclear Structure, Volume I: Single-Particle Motion; Volume II: Nuclear Deformations (World Scientific, Singapore, 1998).
- [32] R. D. Herzberg et al., Eur. Phys. J. A 42, 333 (2009).
- [33] P. Reiter et al., Phys. Rev. Lett. 95, 032501 (2005).
- [34] I. Angeli and K. Marinova, At. Data Nucl. Data Tables 99, 69 (2013).
- [35] A. Voss, V. Sonnenschein, P. Campbell, B. Cheal, T. Kron, I. D. Moore, I. Pohjalainen, S. Raeder, N. Trautmann, and K. Wendt, Phys. Rev. A 95, 032506 (2017).
- [36] M. Kortelainen, J. McDonnell, W. Nazarewicz, P.-G. Reinhard, J. Sarich, N. Schunck, M. V. Stoitsov, and S. M. Wild, Phys. Rev. C 85, 024304 (2012).
- [37] P. Klüpfel, P.G. Reinhard, T.J. Bürvenich, and J.A. Maruhn, Phys. Rev. C **79**, 034310 (2009).

- [38] J. A. Maruhn, P.-G. Reinhard, P. D. Stevenson, and A. S. Umar, Comput. Phys. Commun. 185, 2195 (2014).
- [39] P.-G. Reinhard and W. Nazarewicz, Phys. Rev. C 95, 064328 (2017).
- [40] W. D. Myers and W. J. Swiatecki, Ann. Phys. (N.Y.) 55, 395 (1969).
- [41] P. Möller, J. Nix, W. D. Myers, and W. J. Swiatecki, Nucl. Phys. A536, 61 (1992).
- [42] P. Möller, J. Nix, W. Myers, and W. Swiatecki, At. Data Nucl. Data Tables 59, 185 (1995).
- [43] A. Sobiczewski, I. Muntian, and Z. Patyk, Phys. Rev. C 63, 034306 (2001).
- [44] R.-D. Herzberg *et al.*, Phys. Rev. C **65**, 014303 (2001).
- [45] W. D. Myers and K.-H. Schmidt, Nucl. Phys. A410, 61 (1983).
- [46] D. Berdichevsky and F. Tondeur, Z. Phys. A 322, 141 (1985).